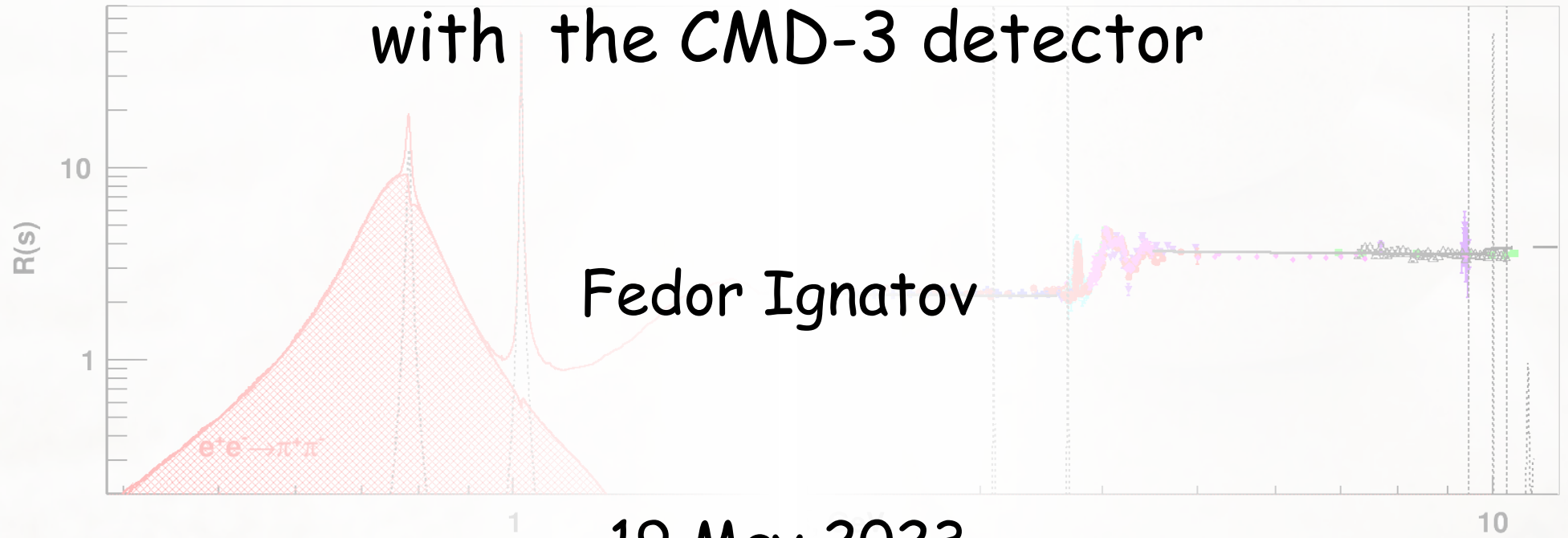


# Recent $e^+e^- \rightarrow \pi^+\pi^-$ measurement with the CMD-3 detector



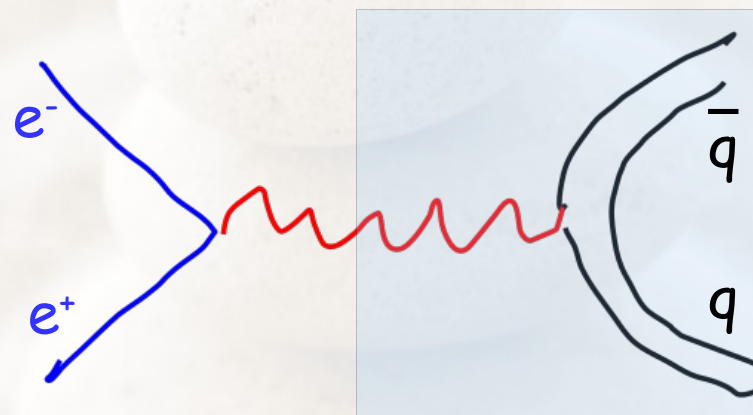
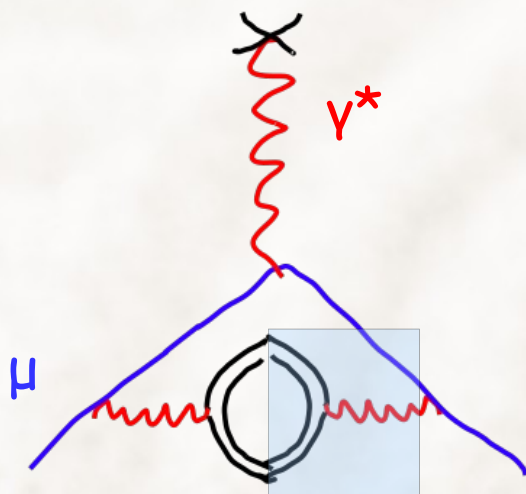
19 May 2023

Particle Physics Annual Meeting  
Liverpool

# $g-2$ and $e^+e^- \rightarrow \text{hadrons}$



Muon precession anomaly  $(g-2)/2$  via vacuum polarization is related to  $e^+e^-$  to hadrons production

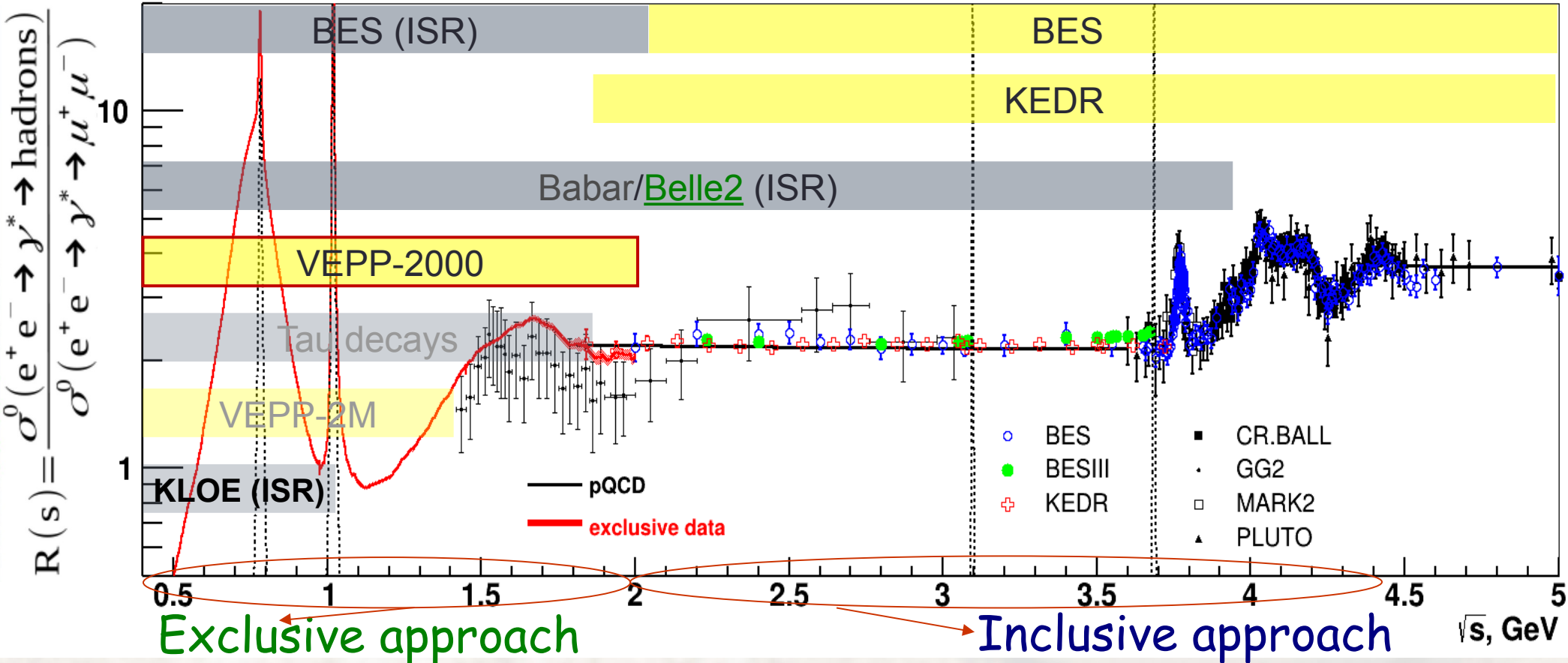


$$a_{\mu}^{had,LO} = \frac{m_{\mu}^2}{12\pi^3} \int_{4m_{\pi}^2}^{\infty} \frac{\sigma_{e^+e^- \rightarrow \gamma^* \rightarrow hadrons}(s) K(s)}{s} ds$$

Dispersion relation is based on analyticity and the optical theorem

# R(s) measurement

Two techniques: ISR vs Energy scan

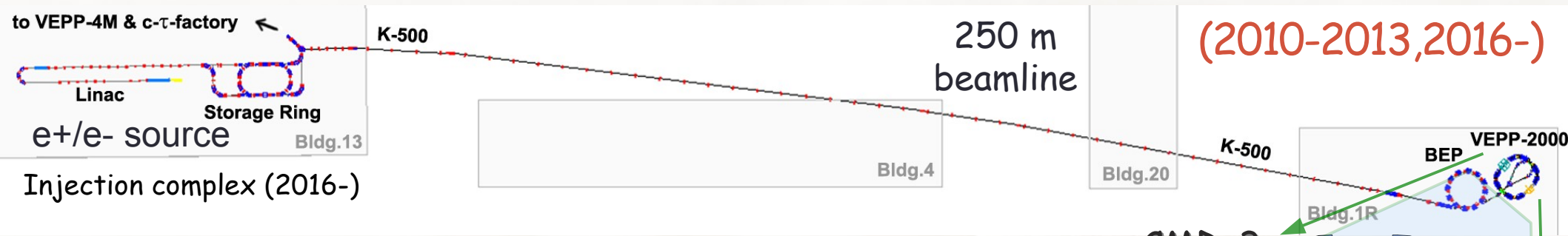


- x Two techniques : Energy scan vs Initial State Radiation (ISR)
- x Two approaches : Exclusive (each channel measured separately) vs Inclusive (total hadronic cross section)

VEPP-2000: Only one working these days on scanning below <2 GeV

with world-best luminosity per single bunch at this energies

# VEPP-2000 e+e- collider



VEPP-2000: direct exclusive measurement of  $\sigma(e+e- \rightarrow \text{hadrons})$

Only one working this days on scanning  $2E = 0.32-2 \text{ GeV}$

Unique optics, "round beams" to reach higher L

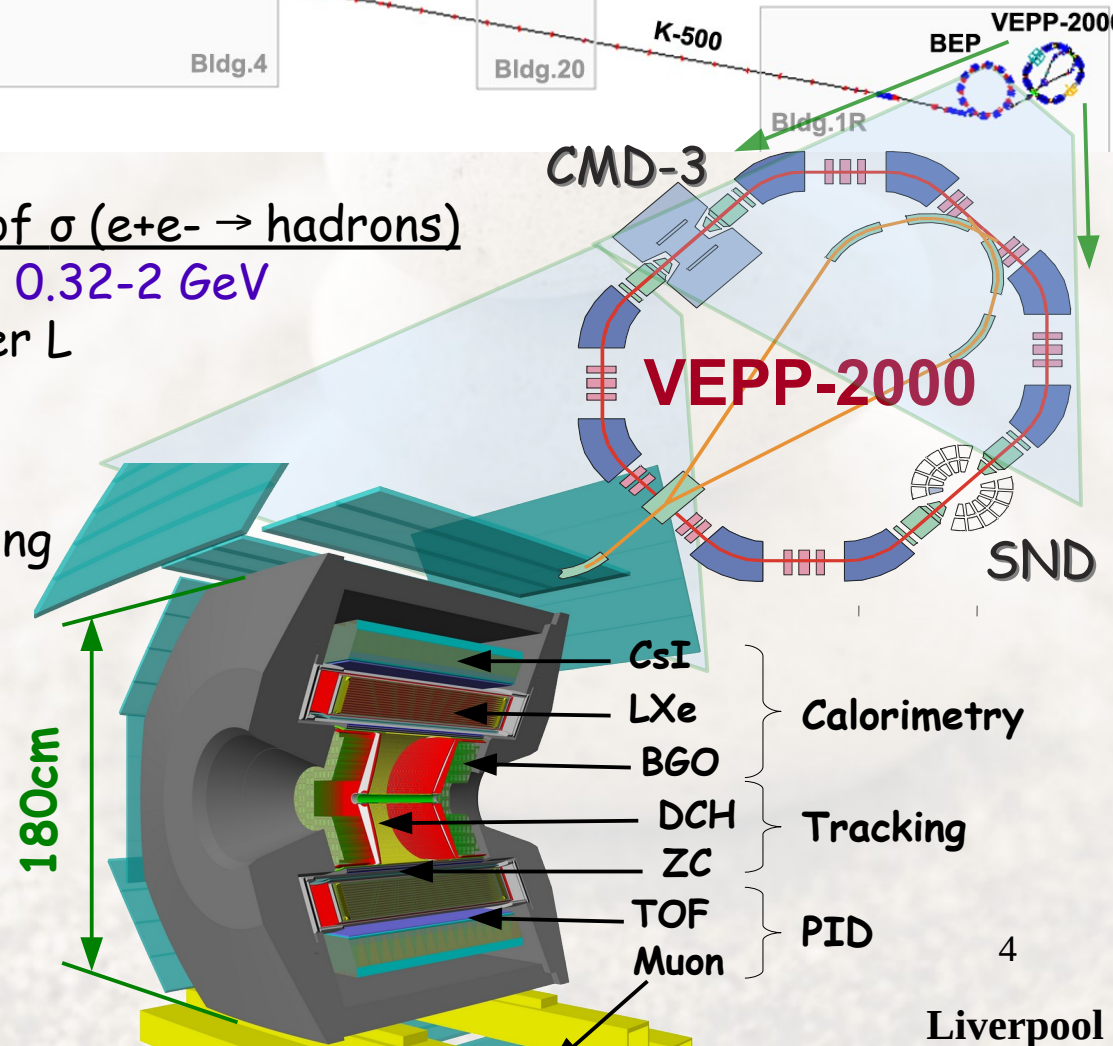
$$L = 0.9 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1} \text{ at } 2E = 2 \text{ GeV}$$

Energy monitoring by Compton backscattering

$$\sigma_{fs} \approx 0.1 \text{ MeV}$$

Two detectors: CMD-3 and SND

started by the end of 2010

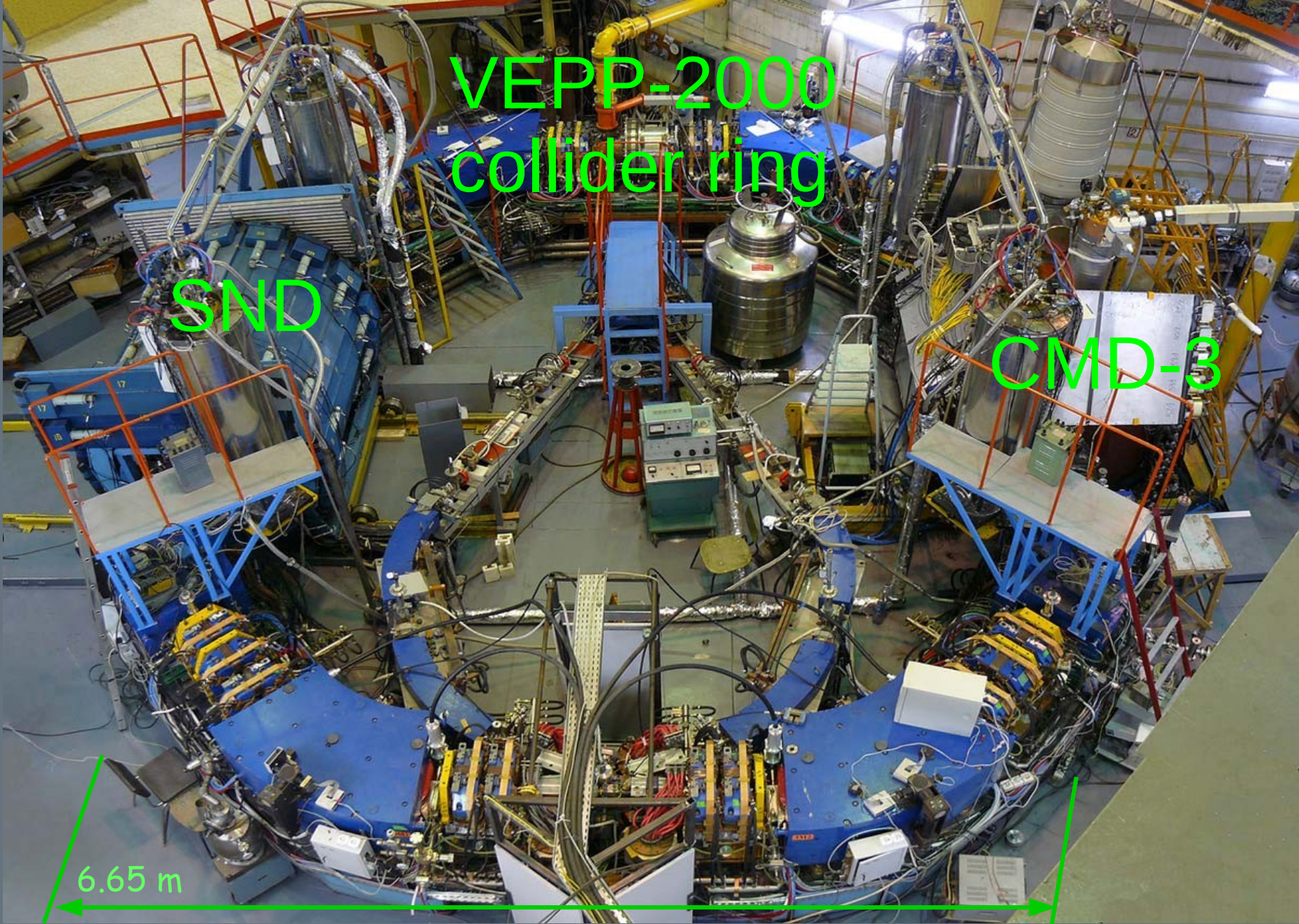


VEPP-2000  
collider ring

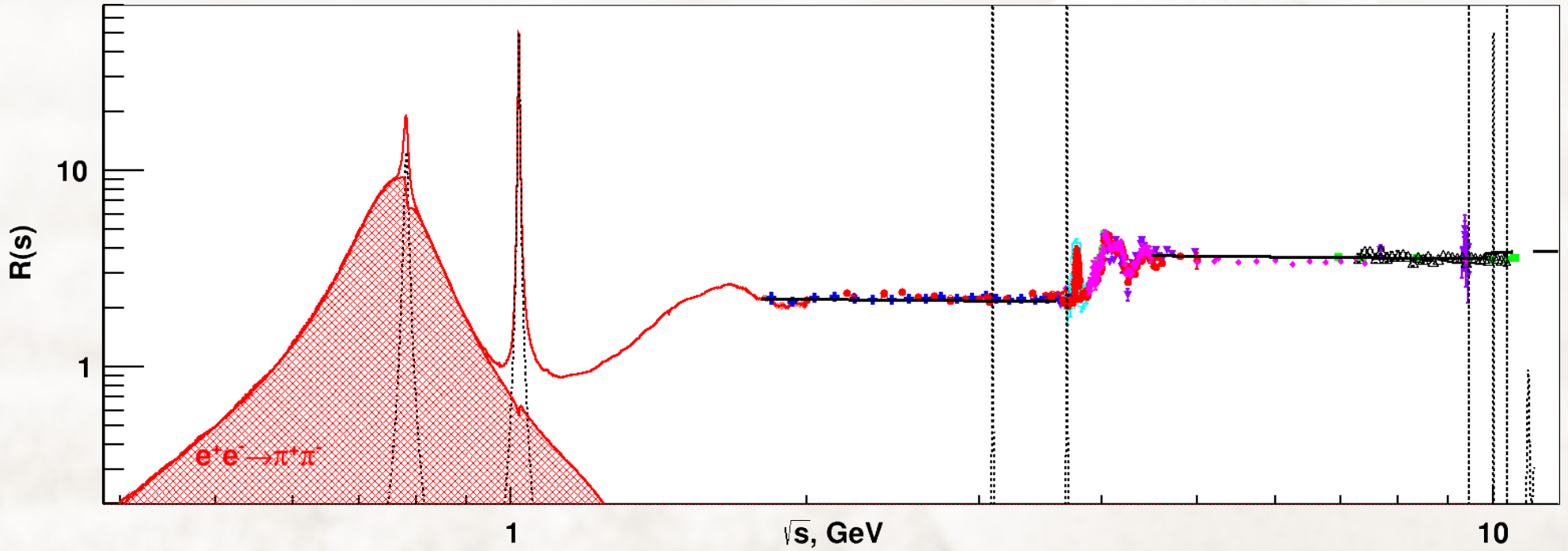
SND

CMD-3

6.65 m



$$R(s) = \frac{\sigma^0(e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$

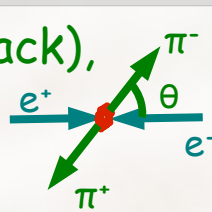


$e^+e^- \rightarrow \pi^+\pi^-$  gives main contribution to  $R(s)$  at  $\sqrt{s} < 1$  GeV  
and this channel is most important for muon  $(g-2)/2$

# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD3



Very simple topology (just 2 tracks back to back),  
but the most challenging channel  
due to high precision requirement.



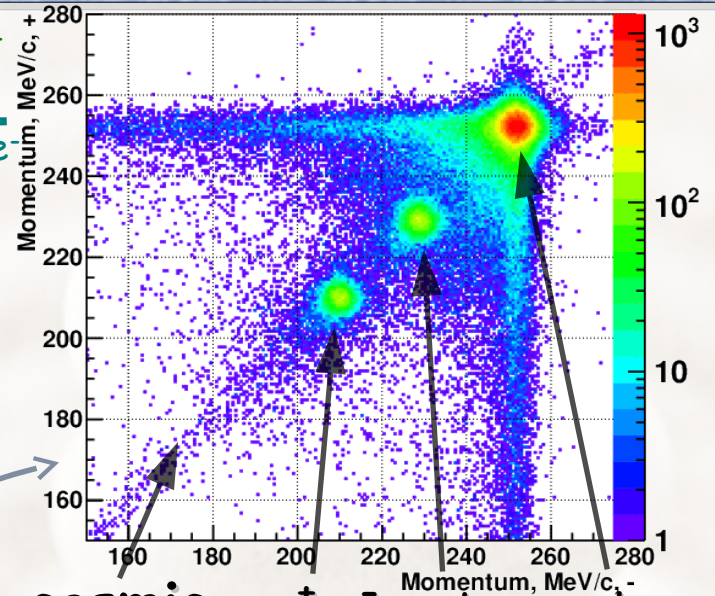
Analysis was performed trying to reach systematic  
~0.35-0.5%

## Crucial pieces of analysis:

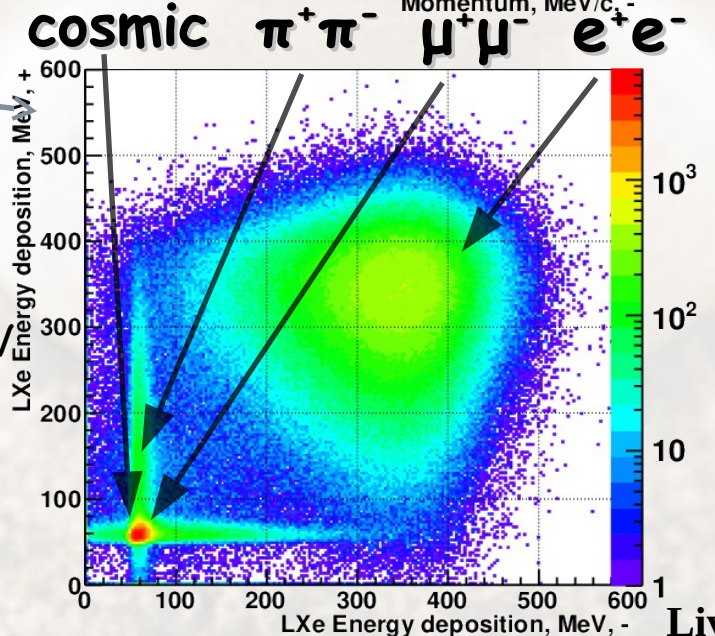
- x  $e/\mu/\pi$  separation
- x radiative corrections
- x precise fiducial volume
- x ...

- events separation either
- 1) by momentum
  - 2) or by energy deposition
  - 3) additional cross-check by angle distribution

4) using shower profile at >1GeV



$P^+ \times P^-$   $E_{beam} = 250 \text{ MeV}$



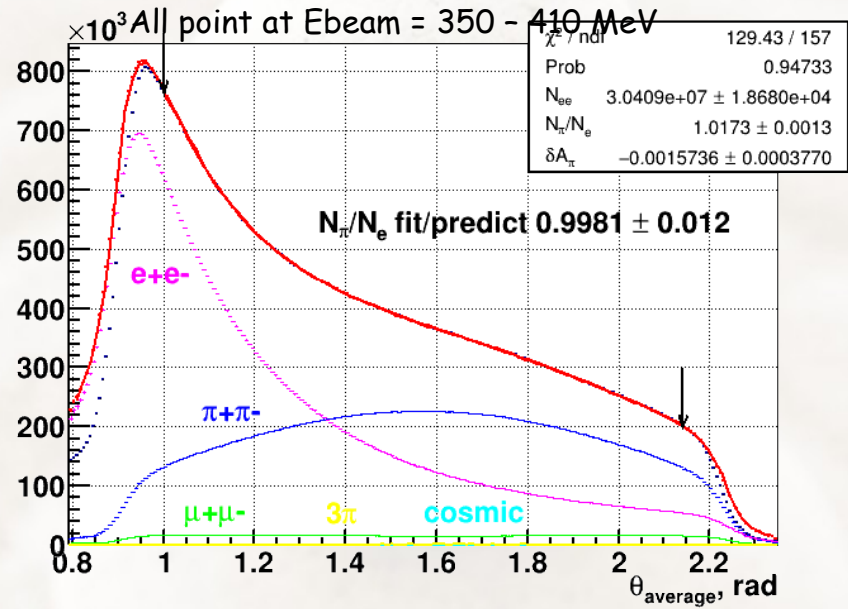
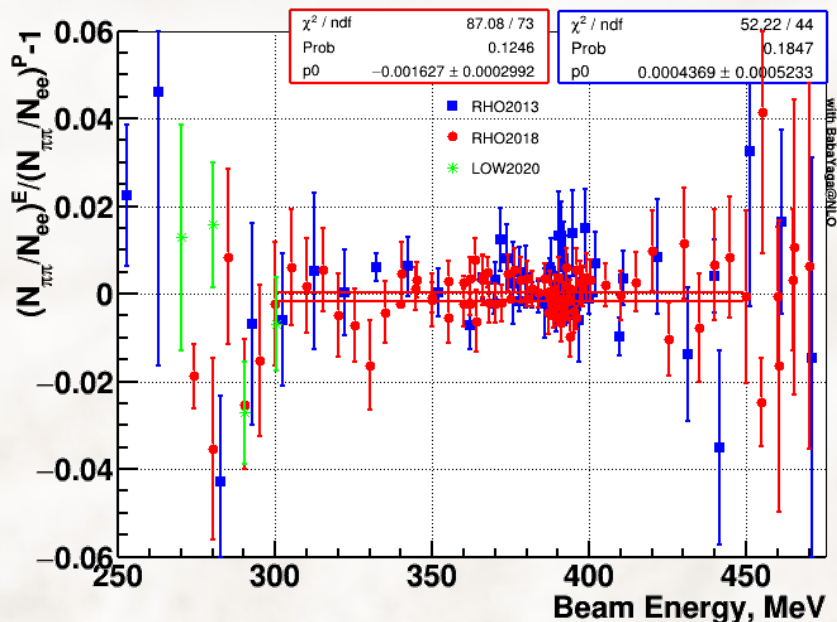
$E^+_{LXe} \times E^-_{LXe}$   $E_{beam} = 480 \text{ MeV}$

# e/ $\mu$ / $\pi$ separation

3 methods for  $N_{\pi\pi} / N_{ee}$  determination based on independent informations:

- 1) Momentum from DCH
- 2) Energy deposition in LXe
- 3) angles in DCH

E vs P separations



Fit by  $\theta$  distribution

For sum of  $\sqrt{s} = 0.7 - 0.82$  GeV points  
by momenta in DCH:  $N_{\pi\pi} / N_{ee} = 1.0193 \pm 0.00030$   
by energies in LXe  $\Delta N_{\pi\pi} / N_{ee} = -0.09 \pm 0.024\%$   
from theta with free  $\delta A$ :  $= -0.20 \pm 0.12\%$   
 with fixed  $\delta A=0$ :  $= +0.21 \pm 0.07\%$

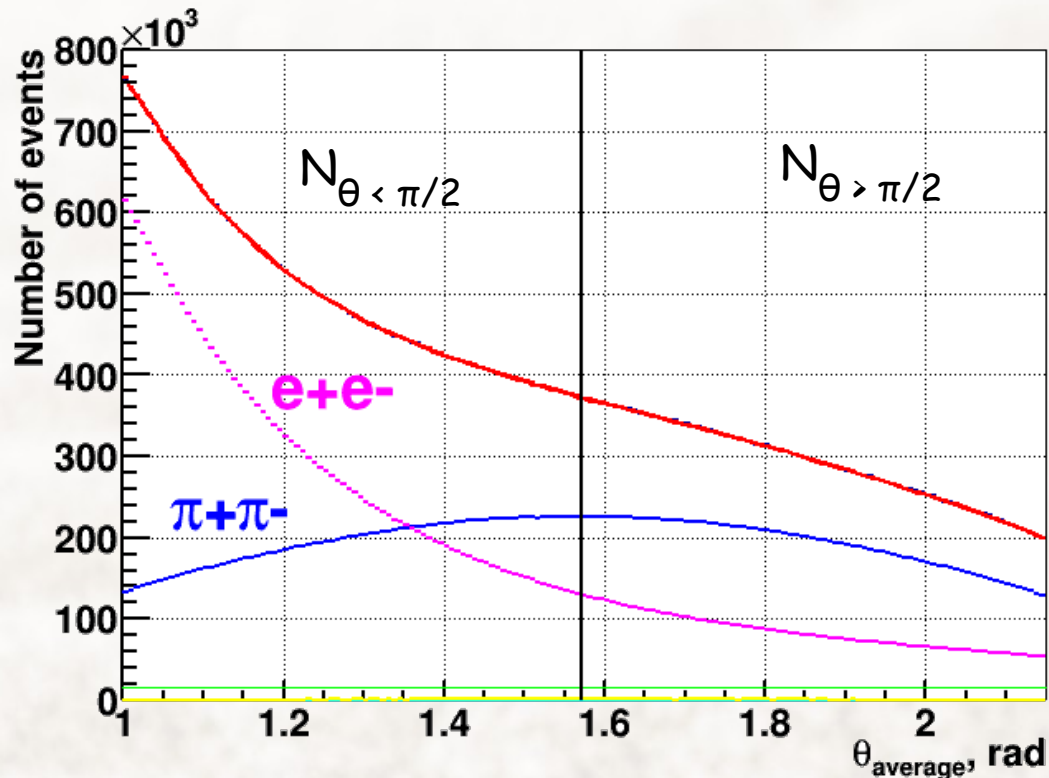
consistency at  $\sim 0.2\%$

Common stat from  $\sqrt{N}$ :  
0.026%



# Forward backward charge asymmetry

## $d\sigma/d\theta$ spectra



Asymmetry definition:

$$A = (N_{\theta < \pi/2} - N_{\theta > \pi/2})/N$$

Sensitive to:

× angle-related systematics

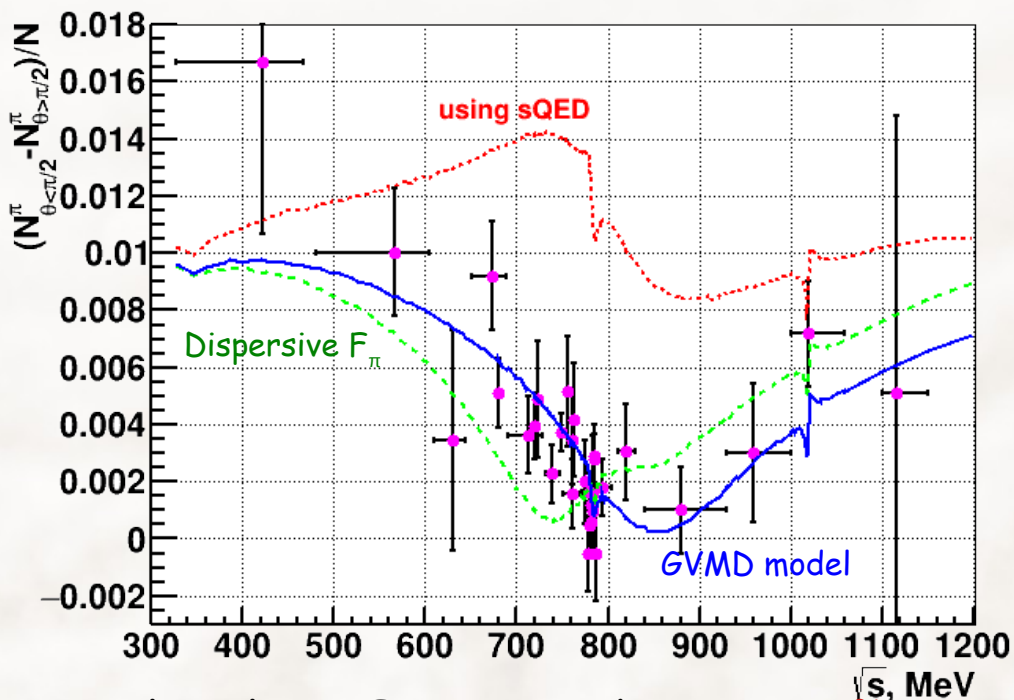
× used model of  $\gamma$ - $\pi$  interaction

At first try:

1% inconsistency for  $\pi^+\pi^-$  was observed between data and MC prediction

# Charge asymmetry in $e^+e^- \rightarrow \pi^+\pi^-$

$$A = (N_{\theta < \pi/2}^\pi - N_{\theta > \pi/2}^\pi) / N$$



Conventional scalar QED approach gives  $\sim 1\%$  inconsistency

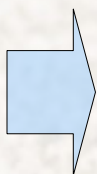
The theoretical model within **GVMD** was introduced, describes well the CMD-3 data R.Lee et al., Phys.Lett.B 833 (2022) 137283 was confirmed by calculation in **dispersive formalism**

M.Hoferichter et al., JHEP 08 (2022) 295

Average at  $\sqrt{s} = 0.7\text{-}0.82$  GeV:

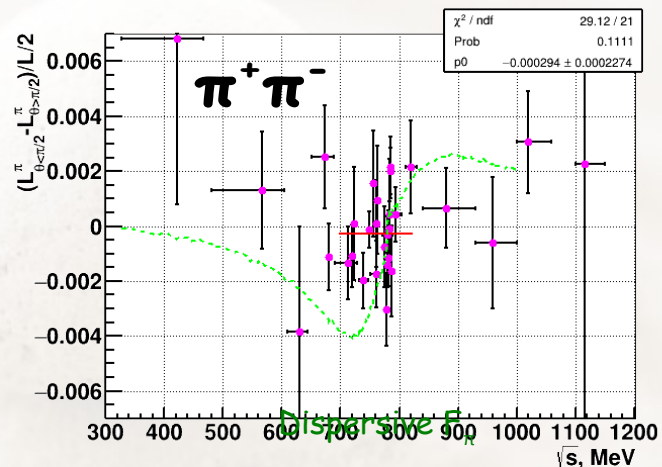
$$\pi^+\pi^-: \langle \delta A \rangle = -0.029 \pm 0.023 \%$$

$$e^+e^-: \langle \delta A \rangle = -0.060 \pm 0.026 \%$$

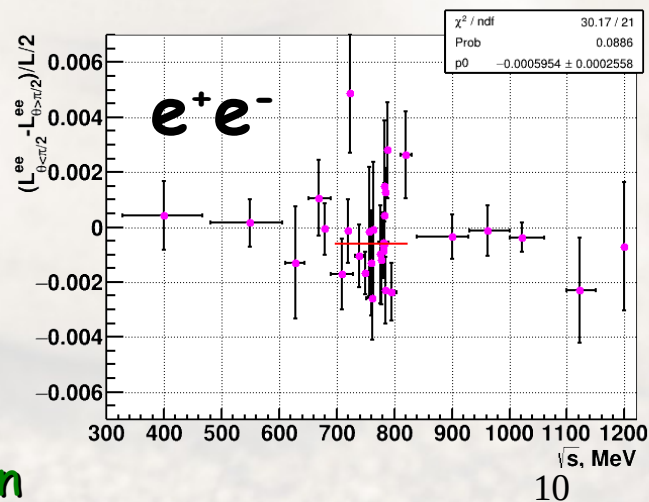


Ensure our  $\theta$  angle systematics estimation for  $|F_\pi|^2$

Relative to GVMD prediction



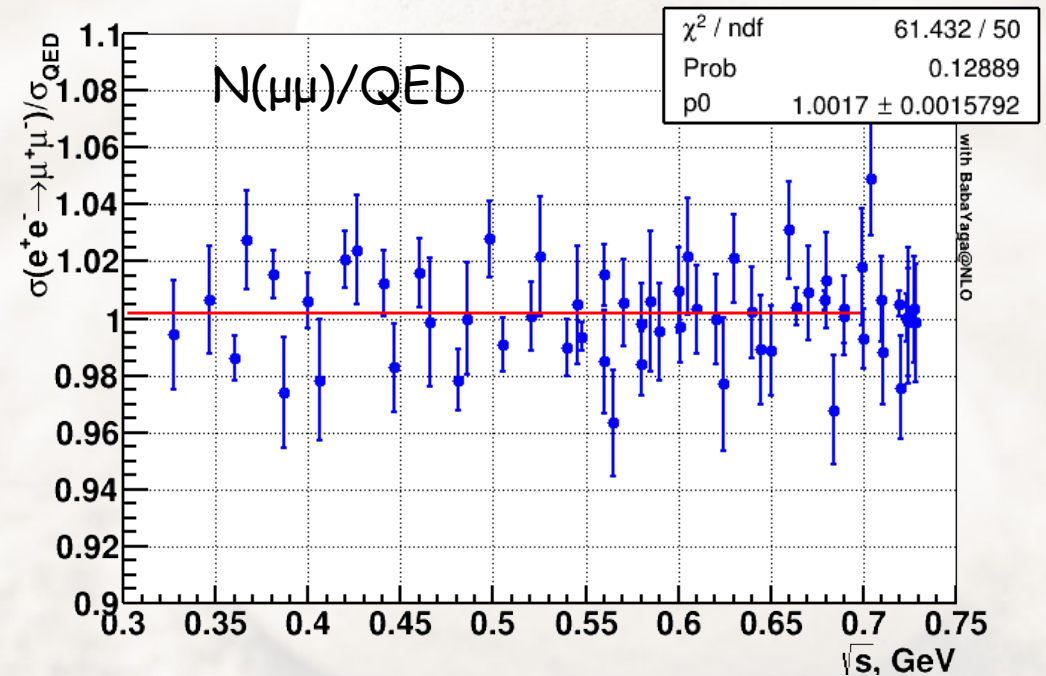
to BaBaYaga@NLO



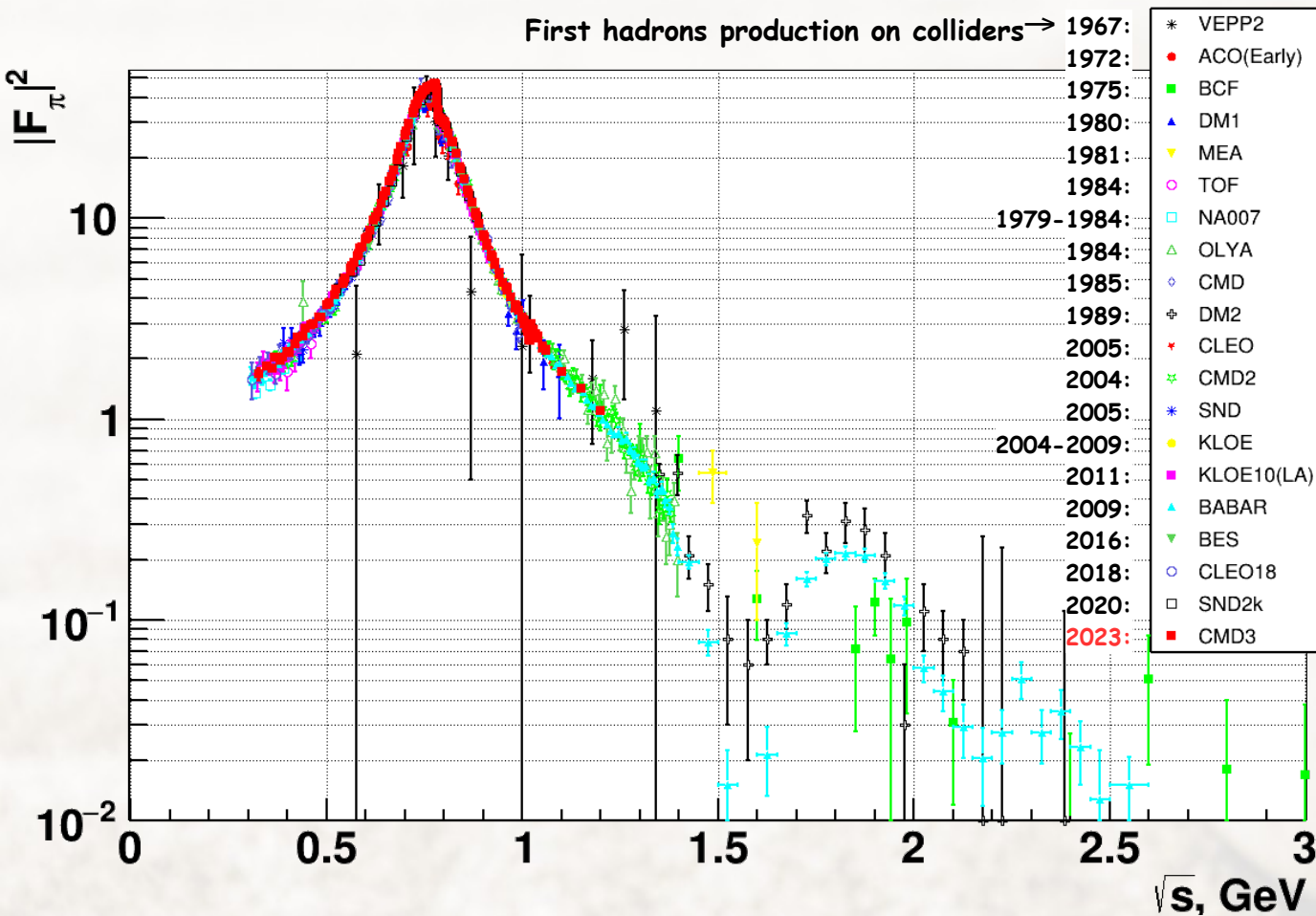
# $e^+e^- \rightarrow \mu^+\mu^-$ cross section

One of consistency checks for  $e^+e^- \rightarrow \pi^+\pi^-$  is provided by comparison of measured  $e^+e^- \rightarrow \mu^+\mu^-$  cross section vs QED prediction

$$N_{\mu\mu}/\text{QED} : \Delta = +0.17 \pm 0.16 \%$$



# $e^+ e^- \rightarrow \pi^+ \pi^-$ today



## Before 1985

Low statistical precision

Systematics >10%

NA7 A few points with >1-5%

## 1985 - VEPP-2M

with more detailed scan

OLYA systematics 4%

CMD 2%

## 2004 with CMD2 at VEPP-2M

was boost to systematics: 0.6%

(near same total statistic)

The uncertainty in  $a_\mu(\text{had})$  was improved by factor 3 as the result of VEPP-2M measurements

## New ISR method

$e^+e^- \rightarrow \gamma + \text{hadrons}$  (limited only by systematics):

KLOE: 0.8%

BaBar: 0.5%

BES: 0.9%

CLEO: 1.5%

## New direct data:

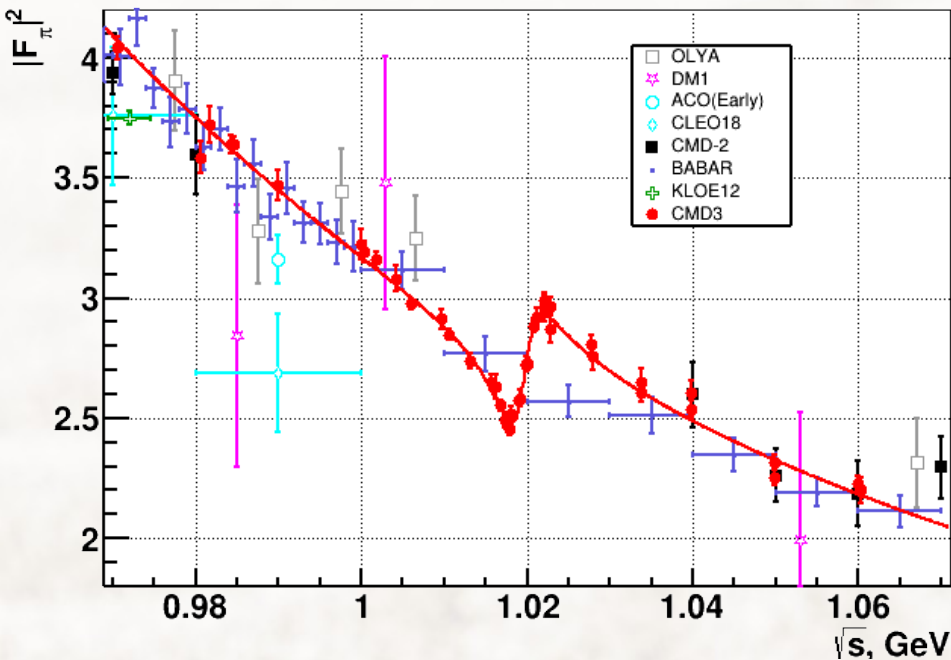
SND2k : 0.8% (with 1./10 of available Data)

**CMD-3: 0.7%**

New  $g-2$  experiments and future  $e^+e^-$  as ILC, FCC-ee require average precision  $\sim 0.2\%$

$$\varphi \rightarrow \pi^+\pi^-$$

## First direct $|F_\pi|^2$ measurement around $\varphi$ resonance



$$\psi_\pi = (-21.3 \pm 2.0 \pm 10.0)^\circ$$

$$B(\varphi \rightarrow e^+e^-)B(\varphi \rightarrow \pi^+\pi^-) = (3.51 \pm 0.33 \pm 0.24) \times 10^{-8}$$

CMD-3

Previous measurement using detected  $N_{\pi^+\pi^-}$  or visible cross-section by OLYA, ND, SND (Sergey Burdin et al, Phys.Lett.B474:188-193,2000)

$$\psi_\pi = (-34 \pm 5)^\circ$$

$$B(\varphi \rightarrow e^+e^-)B(\varphi \rightarrow \pi^+\pi^-) = (2.1 \pm 0.4) \times 10^{-8}$$

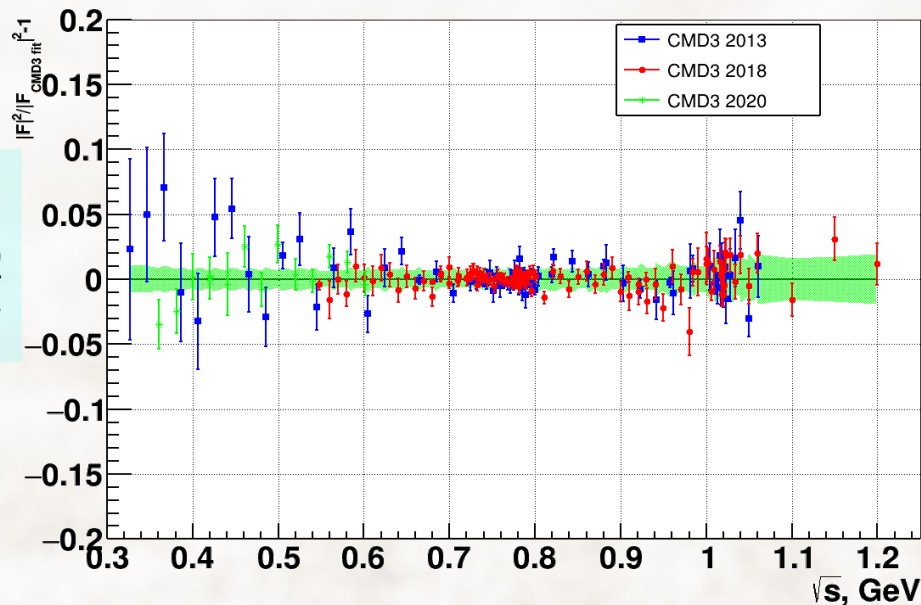
SND

**N.B.** radiative correction uncertainty (from  $F_\pi$  parametrisation)

gives **~1.5 scale factor of total statistical and systematic errors** (both for Br and  $\psi_\pi$ )

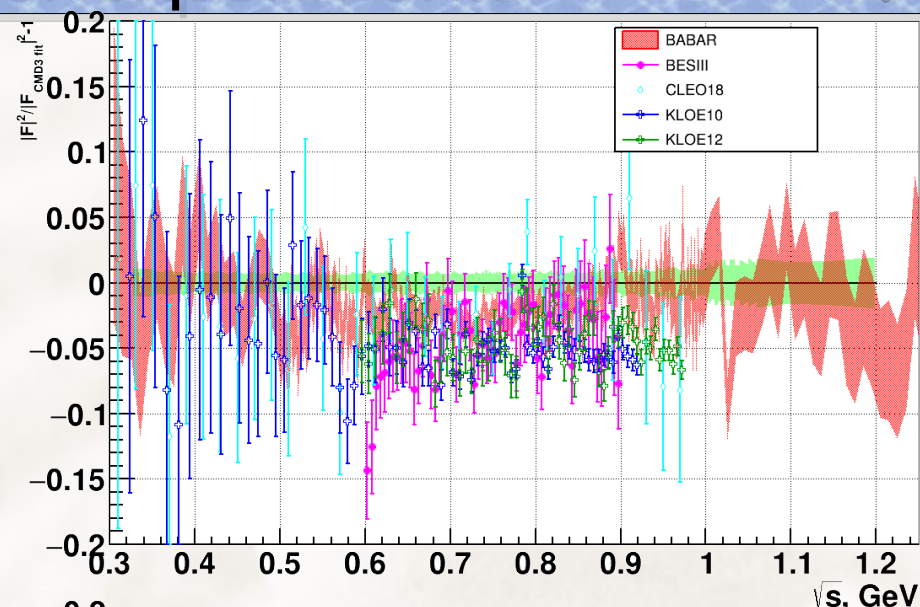
# CMD-3 vs other experiments

Relative to CMD-3 fit,  
**green** band - systematic value

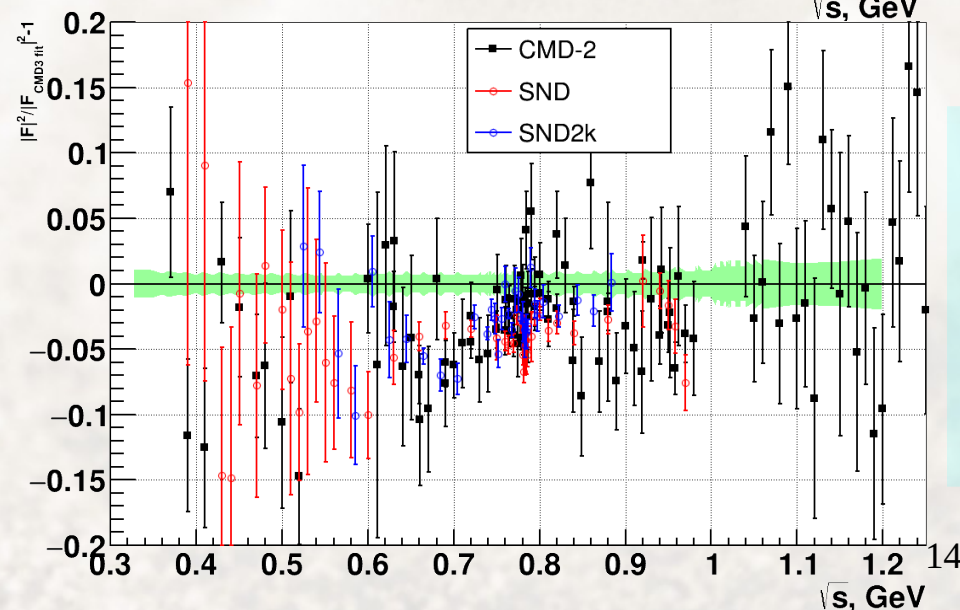


CMD-3

- × Statistical precision is a few times better than any other experiments
- × Cross section is higher by  $\sim 2-5\%$



vs ISR



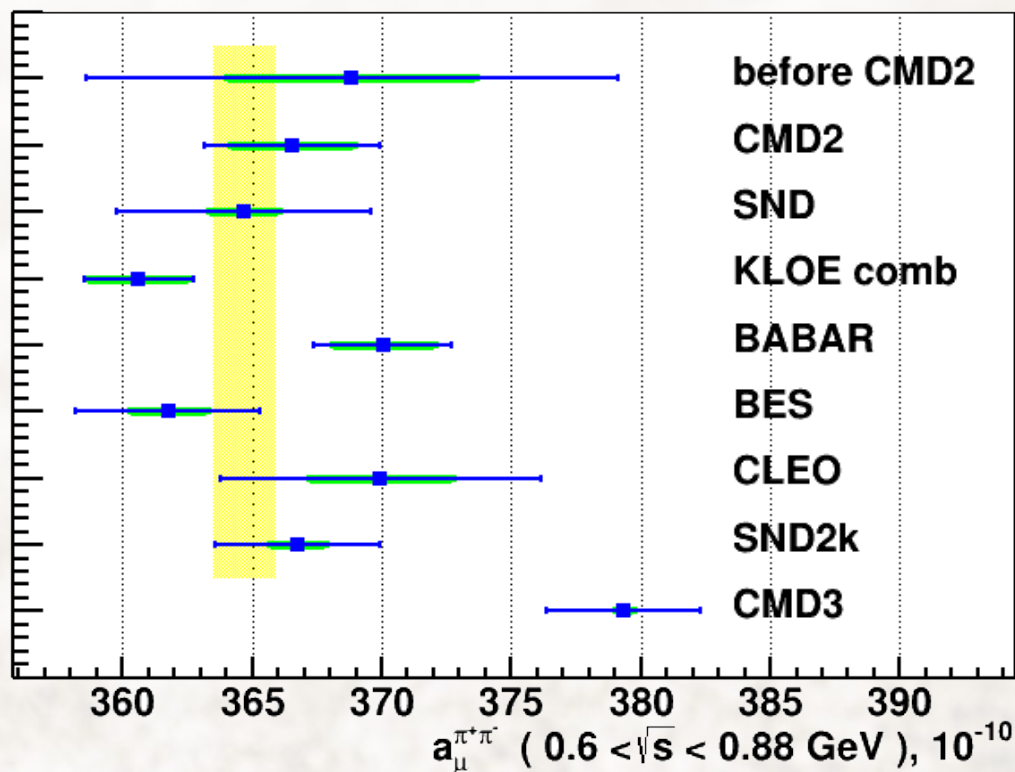
vs direct scan

# The $\pi^+ \pi^-$ contribution to $a_\mu^{\text{had}}$



$$a_\mu^{\text{had,LO}} = \frac{m_\mu^2}{12\pi^3} \int_{4m_\pi^2}^{\infty} \frac{\sigma_{e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons}}(s) K(s)}{s} ds$$

$0.6 < \sqrt{s} < 0.88 \text{ GeV}$



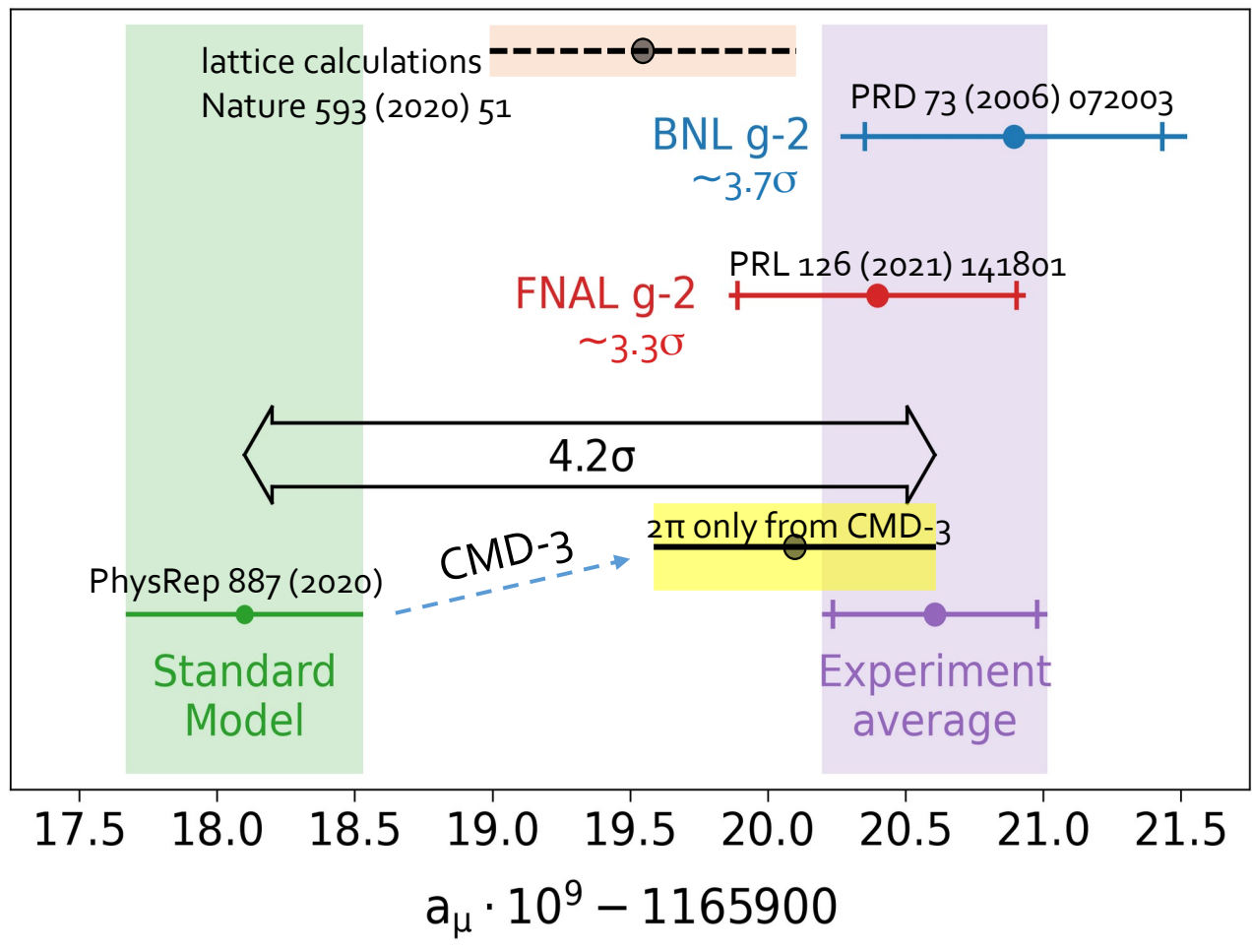
$a_\mu^{\pi\pi, \text{LO}}, 10^{-10}$

|             |                  |
|-------------|------------------|
| before CMD2 | $368.8 \pm 10.3$ |
| CMD2        | $366.5 \pm 3.4$  |
| SND         | $364.7 \pm 4.9$  |
| KLOE        | $360.6 \pm 2.1$  |
| BABAR       | $370.1 \pm 2.7$  |
| BES         | $361.8 \pm 3.6$  |
| CLEO        | $370.0 \pm 6.2$  |
| SND2k       | $366.7 \pm 3.2$  |
| CMD3        | $379.3 \pm 3.0$  |

|         |  |
|---------|--|
| RHO2013 | $380.06 \pm 0.61 \pm 3.64$                 |
| RHO2018 | $379.30 \pm 0.33 \pm 2.62 \times 10^{-10}$ |
| Sum     | $379.35 \pm 0.30 \pm 2.95$                 |

15

# The impact of CMD-3 on SM prediction of $a_\mu^{\text{had}}$



If it will be only CMD-3 than SM will be solved.  
But CMD-3 is only one now over many other experiments (BaBar, KLOE, BES, CMD-2, SND, ...)

**Unfortunately at the moment, we don't know the reasons of the disagreement between different experiments.**



# Puzzles in puzzle

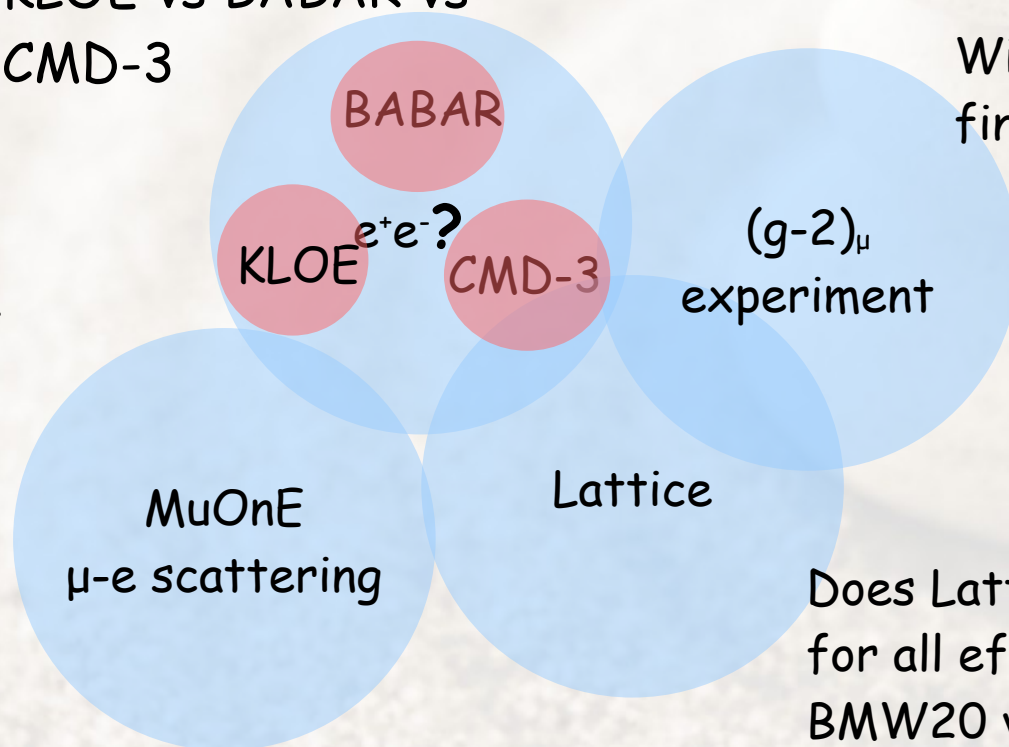


Question of comparison:  
 $e^+e^-$  vs  $(g-2)_\mu$  vs lattice

Where difference  
comes from:  
KLOE vs BABAR vs  
CMD-3

Will it be confirmed?  
final FNAL vs J-PARC

Hard effort  
against  
systematics



Does Lattice account  
for all effects?  
BMW20 vs others



# backups

More details:

Presentation at the TI seminar, 27 March 2023:

<https://indico.fnal.gov/event/59052/>

E-Print: [2302.08834](https://arxiv.org/abs/2302.08834) [hep-ex]

# 55 years of hadron production at colliders

## INVESTIGATION OF THE $\rho$ -MESON RESONANCE WITH ELECTRON-POSITRON COLLIDING BEAMS

V. L. AUSLANDER, G. I. BUDKER, Ju. N. PESTOV, V. A. SIDOROV, A. N. SKRINSKY and A. G. KHABAKHPASHEV

*Institute of Nuclear Physics, Siberian Branch of the USSR Academy of Sciences, Novosibirsk, USSR*

Received 1 September 1967

Preliminary results on the determination of the position and shape of the  $\rho$ -meson resonance with electron-positron colliding beams are presented.

When experiments with electron-positron colliding beams were planned [1, 2] investigation of the process

$$e^- + e^+ \rightarrow \pi^- + \pi^+$$

$$e^- + e^+ \rightarrow K^- + K^+$$

con-  
ter  
ide  
of  
cha-  
col-

Detector was made from different layers of Spark chambers, readouts by photo camera

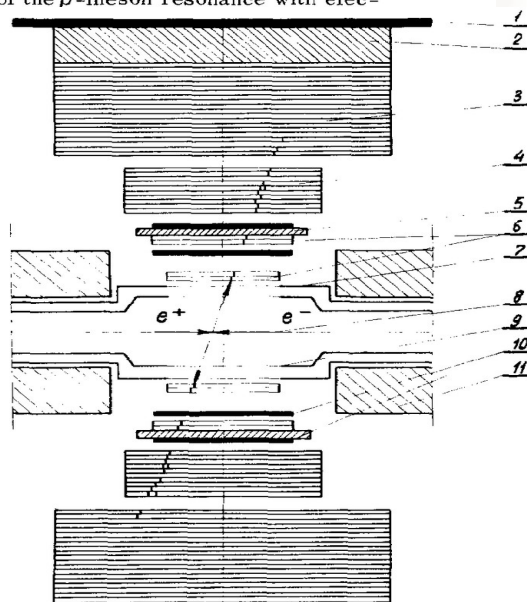


Fig. 1. Spark chambers system:  
1) Anticoincidence scintillation counter  
2) Lead absorber 20 cm thick  
3) "Range" spark chamber  
4) "Shower" spark chamber  
5) Duraluminium absorber 2 cm thick  
6) Thin-plate spark chambers

1 September 1967

Start of  $e^+e^- \rightarrow$  hadrons measurements

Phys.Lett. 25B (1967) no.6, 433-435

VEPP-2, Novosibirsk

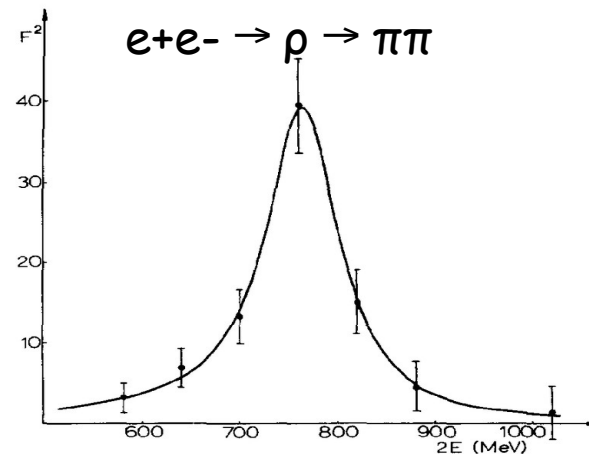


Fig. 2. Experimental values of  $F^2(E)$  approximated by the Breit-Wigner formula.

ment geometry and  $F$ - modulus of the form factor for pion pair production [1]. In the case of QED with no other forces  $F=1$ . If the particles are produced at the angle  $90^\circ$  with respect to the beam axis then  $a=18$ . Integration over the solid angle gives  $a=20.4$ .

# SM prediction for muon g-2

White Paper 2020 (e-Print: 2006.04822)

e-Print: 2203.15810

Experimental world average (E821+E989)

$$a_\mu = 11\,659\,206.1 \pm 4.1 \times 10^{-10}$$

Theoretical prediction data driven

$$a_\mu = 11\,659\,181.0 \pm 4.3 \times 10^{-10} \quad (\text{WP20})$$

$$\Delta a_\mu = 25.1 \pm 5.9 \times 10^{-10}$$

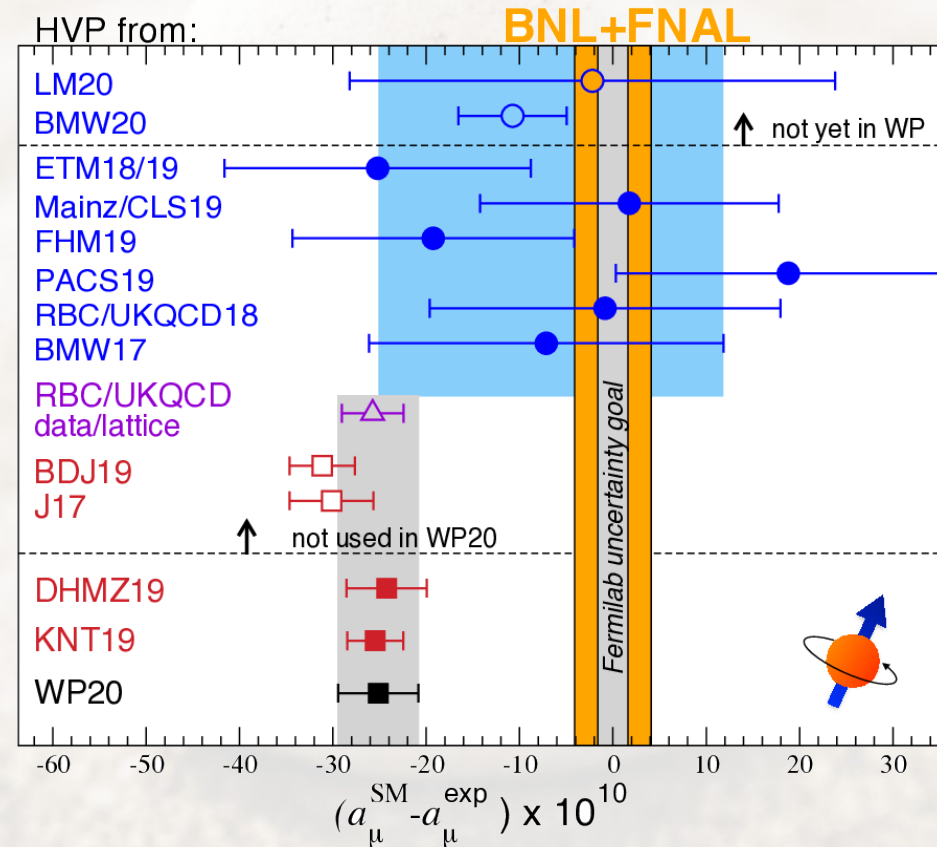
Hadronic part from  $e^+e^- \rightarrow \text{hadrons}$ :

$$a_\mu(\text{had}) = 693.1 \pm 4.0 \times 10^{-10}$$

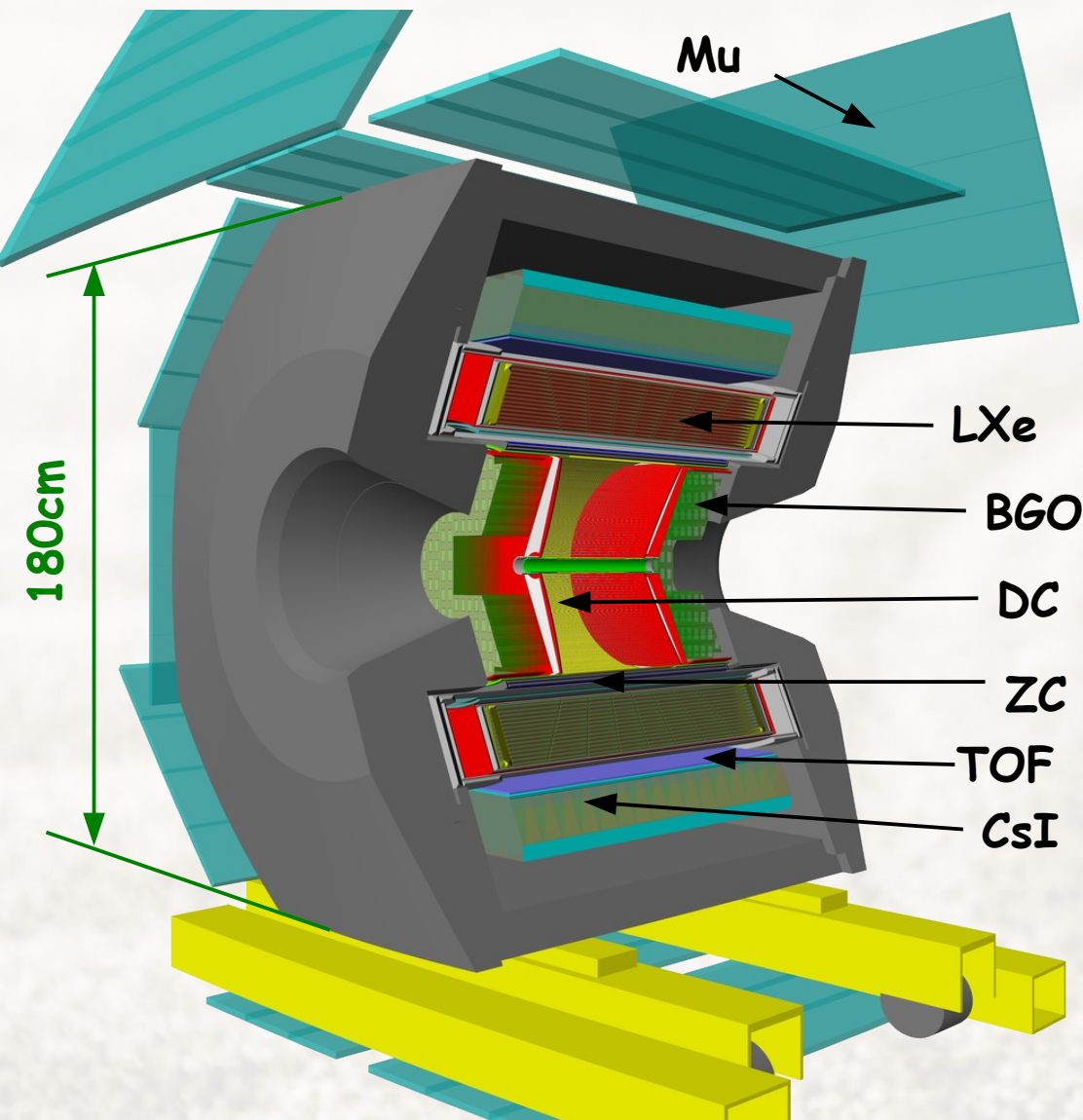
$$\pi^+\pi^- \quad 506.0 \pm 3.4$$

.....

$\pi^+\pi^-$  gives the main contribution (73%) to  $a_\mu^{\text{HAD}}$



# CMD-3 detector



## Tracking:

x Drift Chamber in 1.3 T magnetic field

$$\sigma_{R\phi} \sim 100 \mu\text{m}, \sigma_z \sim 2.5\text{mm}$$

$$\sigma_p/P \sim \sqrt{0.6^2 + (4.4 \cdot p[\text{GeV}])^2}, \%$$

x ZC-chamber worked until summer 2017

$$\sigma_z \sim 0.7\text{mm by strip readout}$$

## Calorimetry:

x Combined EM calorimeter (LXe, CsI, BGO)

13.5  $X_0$  in barrel part

$$\sigma_E/E \sim 0.034/\sqrt{E [\text{GeV}]} \oplus 0.020 - \text{barrel}$$

$$\sigma_E/E \sim 0.024/\sqrt{E [\text{GeV}]} \oplus 0.023 - \text{endcap}$$

x LXe calorimeter with 7 ionization layers  
with strip readout

~2mm measurement of conversion point,  
tracking capability,  
shower profile (from 7 layers + CsI)

## PID:

x TOF system ( $\sigma_T \sim 0.4 \text{ nsec}$ )

particle id mainly for p, n

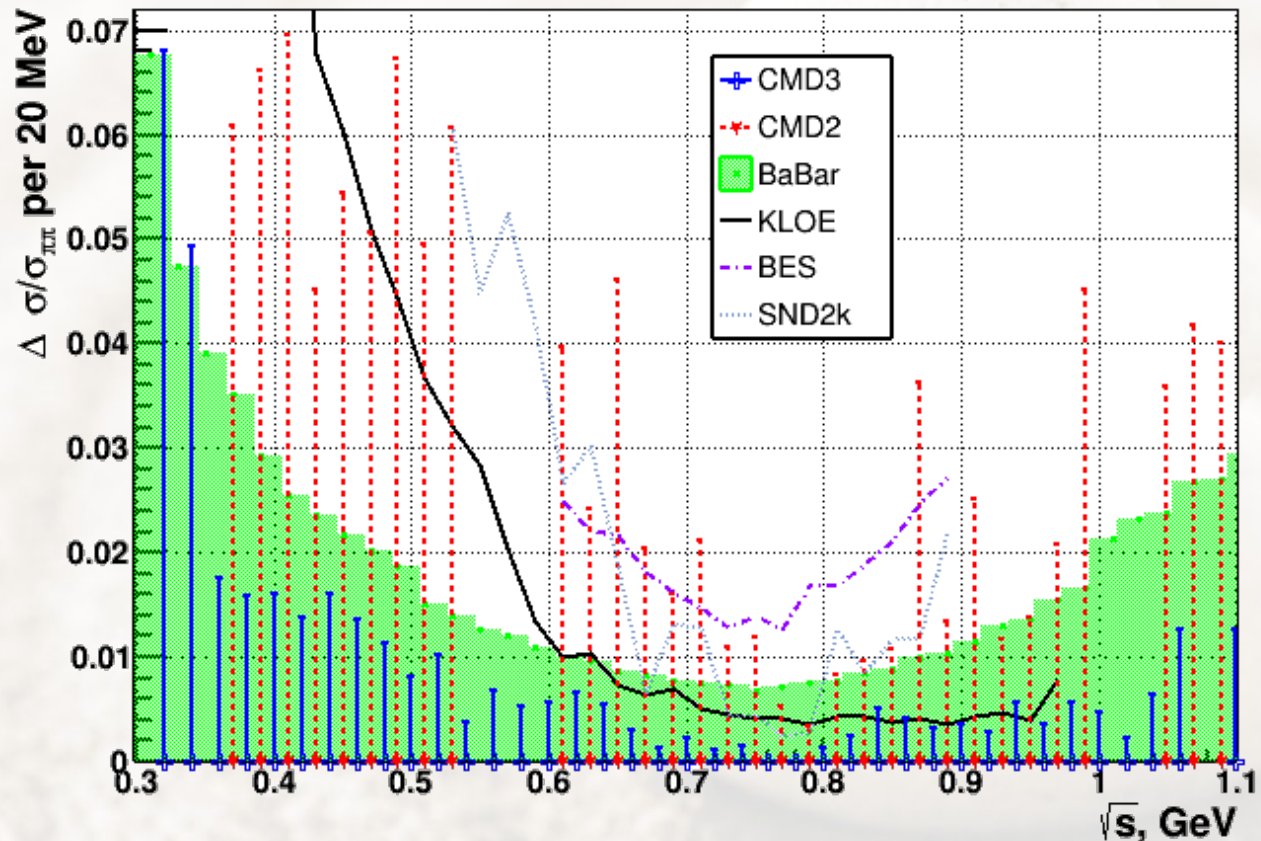
x Muon system

# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD-3

Statistical precision of *CMD-3* cross section measurement  
is a few times better than any other experiments

Full statistic is used  
collected during  $\rho$  scans

3 seasons of data taking:  
RHO2013  
RHO2018  
LOW2020



Analysis based on  $L = 61.9 \text{ pb}^{-1}$  at  $\sqrt{s} < 1 \text{ GeV}$  (+25.7  $\text{pb}^{-1}$ , 1.0-1.2  $\text{GeV}$ )

$34 \times 10^6 \pi^+\pi^-$ ,  $3.7 \times 10^6 \mu^+\mu^-$ ,  $44 \times 10^6 e^+e^-$   
events selected at  $\sqrt{s} < 1 \text{ GeV}$

# Dispersive vs Lattice

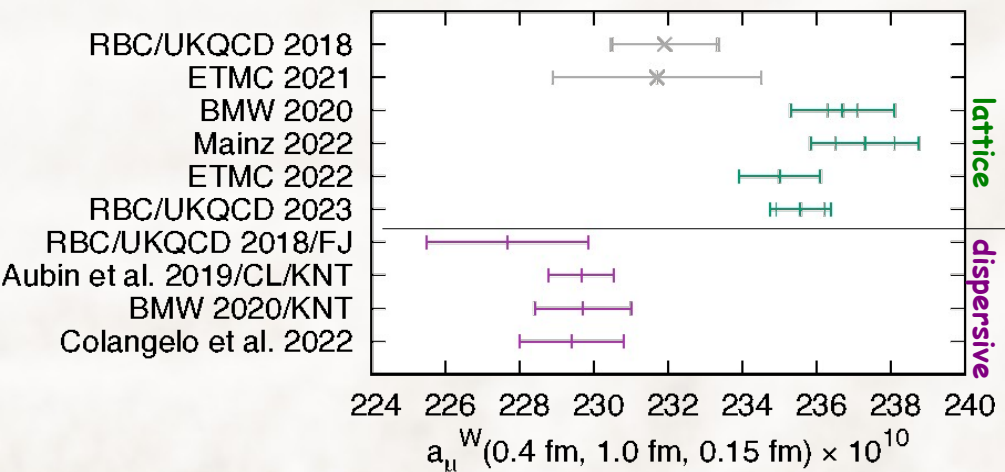


T.Blum et al, e-Print: 2301.08696 [hep-lat]

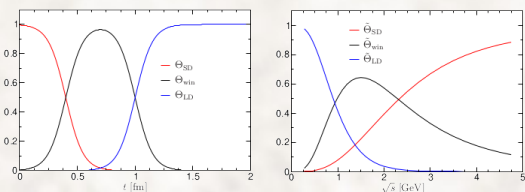
C. Alexandrou et al, e-Print: 2212.08467 [hep-lat]

$a_{\mu}^{\text{HVP}}$  contribution from intermediate window in Euclidean time

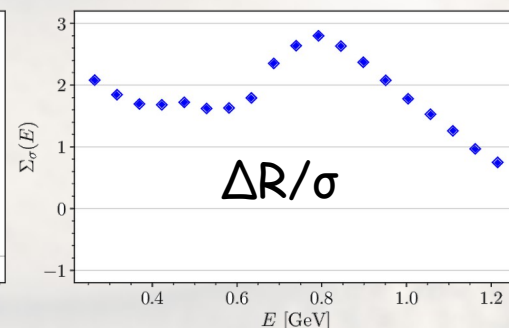
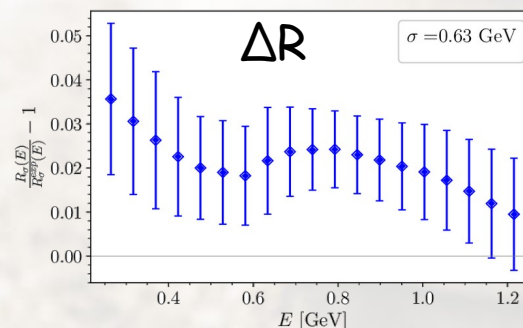
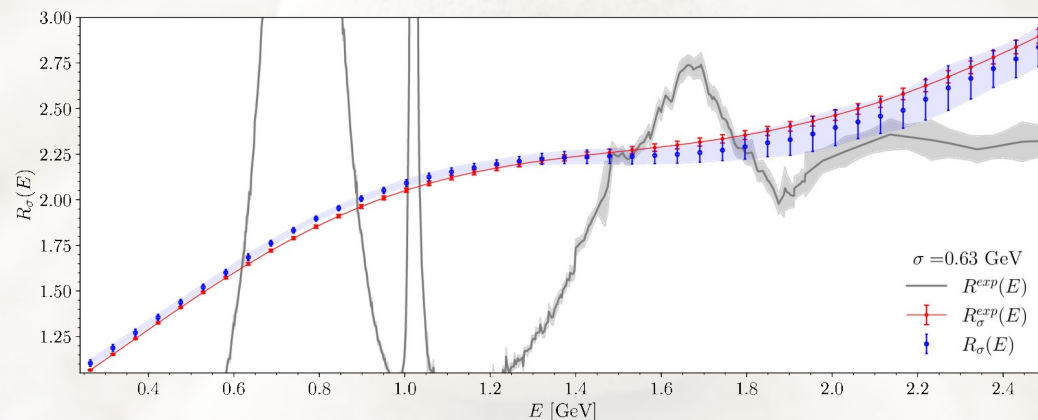
$R(s)$  is convolved with Gaussian kernel



Windows definition



$\sim 4\sigma$  tension between Lattice/Dispersive



$\sim 3\sigma$  tension at rho energies

Question of comparison:  $e+e^-$  vs  $(g-2)_{\mu}$  vs lattice

# Other experiments

