



LEVERHULME
TRUST

BMS
Beam Momentum Station

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University of Liverpool

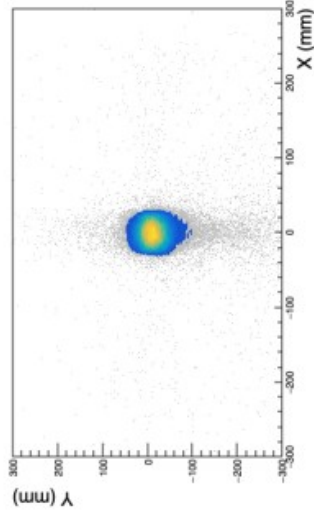
II Muon Precision Physics Workshop
9 November 2023

μ beam at the Experiment entrance

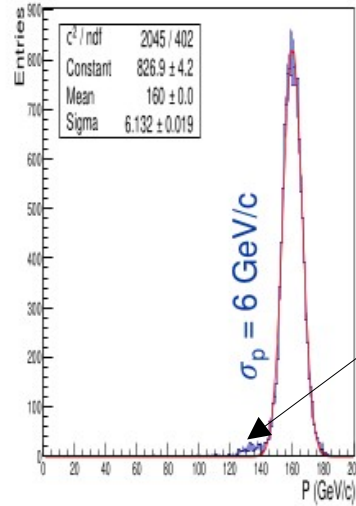
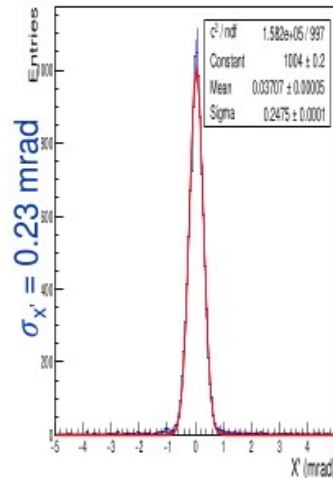
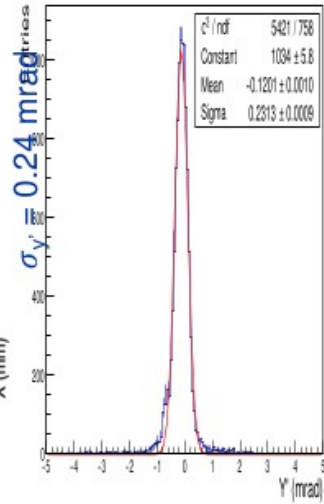
Beam Parameters

Parallel beam

Beamline BDSIM simulation
(Geant4 based)
Dipanwita Banerjee,
4th MuonE Collab. Meeting



$$\sigma_x = 13 \text{ mm}$$
$$\sigma_y = 22 \text{ mm}$$



$$E_{\mu \text{ beam}} = 160 \text{ GeV}$$

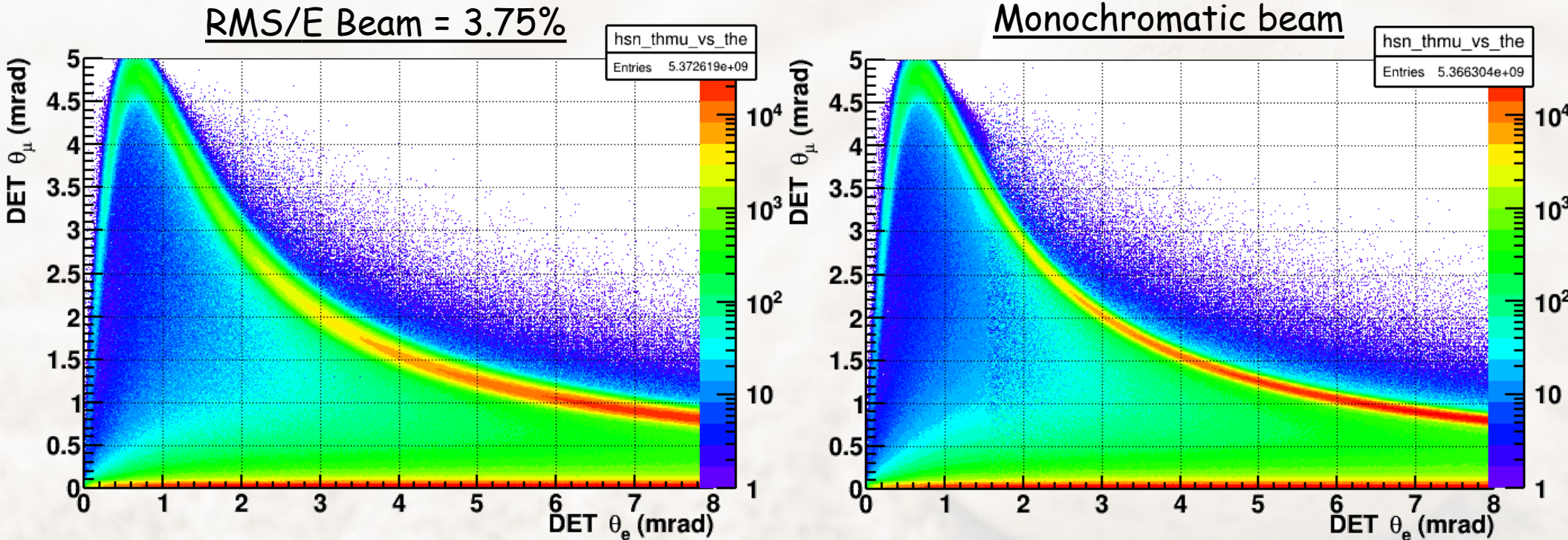
$$\text{RMS}_E / E_{\mu \text{ beam}} = 3.75\%$$

+ possible background contamination, tails

Effect of beam energy spread on scattering spectra in MUonE

MS: at $X/X_0 = .03654$ (1.5cm Be + 1.28 mm Si)
Det: $\sigma_\theta = 0.02$ mrad (10 μ m hit resolution)

Fast sim with [Mesmer](#)
Plot for $\sim 0.06\%$ of targeted $L=1.5 \times 10^7$ nb $^{-1}$



Scattering band is twice wider because of the beam energy spread
Sensitivity over background twice worse

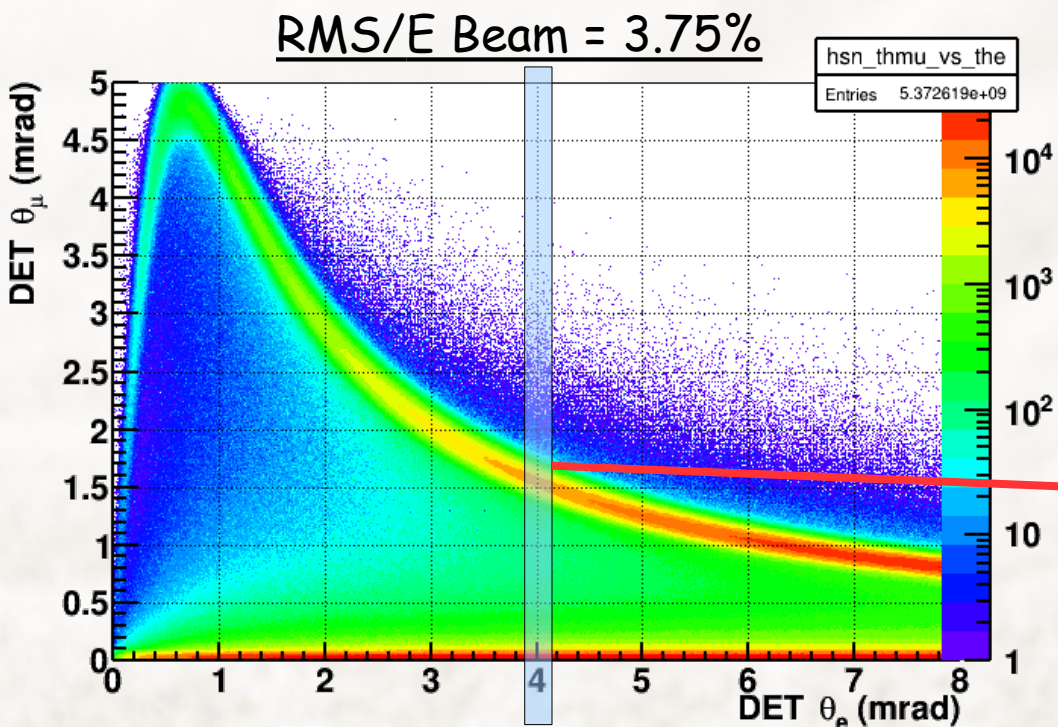
Effect of beam energy spread on scattering spectra in MUonE

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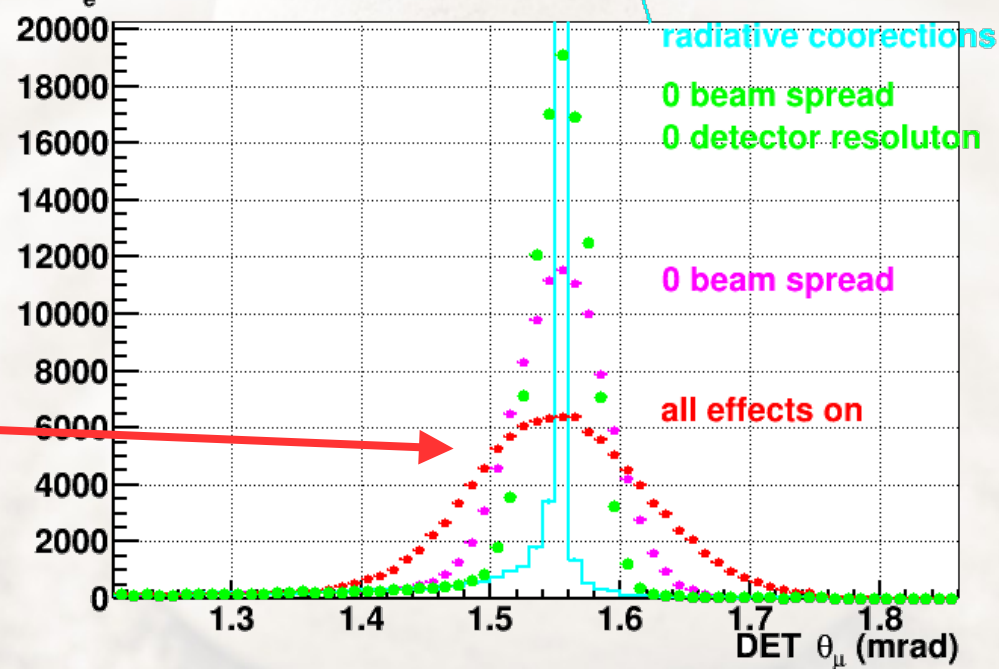
Fast sim by Mesmer

Plot for $\sim 0.06\%$ of targeted $L=1.5 \times 10^7$ nb $^{-1}$



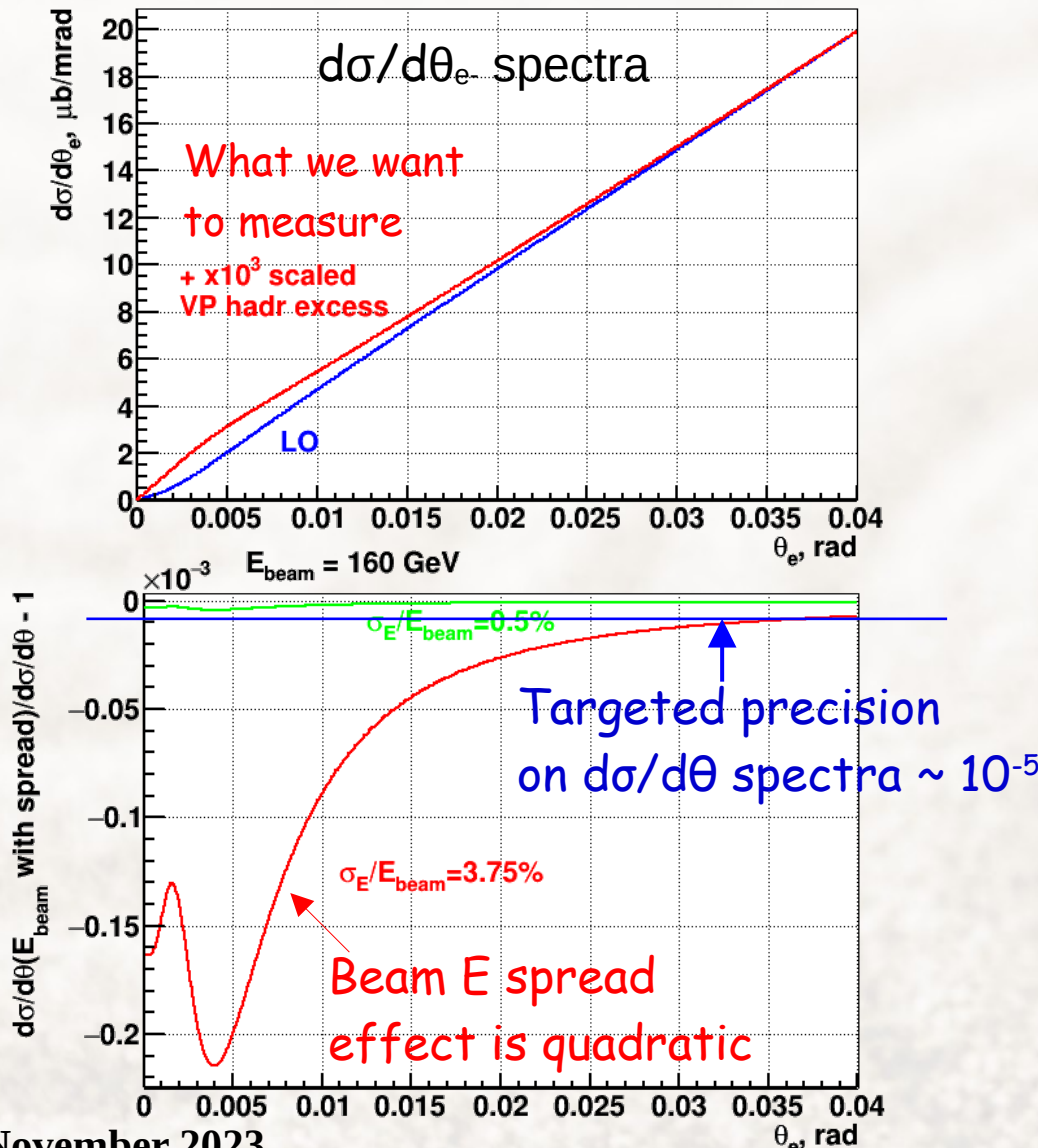
Θ_μ spectra at $\theta_e = 4$ mrad

$\theta_e = 4$ mrad



Scattering band is twice wider because of the beam energy spread
Sensitivity over background twice worse

Effect of beam energy spread on $d\sigma/d\theta_e$ spectra



Beam energy spread change measured angle spectra

gives effect
 $\times 22$ higher relative to the requirement

\rightarrow beam spread must be known
 with $\sim 1\% \times \text{RMS}$ (or $0.04\% \times E_{\text{beam}}$)

Having knowledge on event-by-event μ -momentum at $< 0.5\%$ will suppress this effect

BMS (Beam momentum station)

Bending Magnets at beamline:

$$1.067 \text{ TI} * 5 \text{ m} * 3 \\ = 16.0 \text{ TI} * \text{m}$$

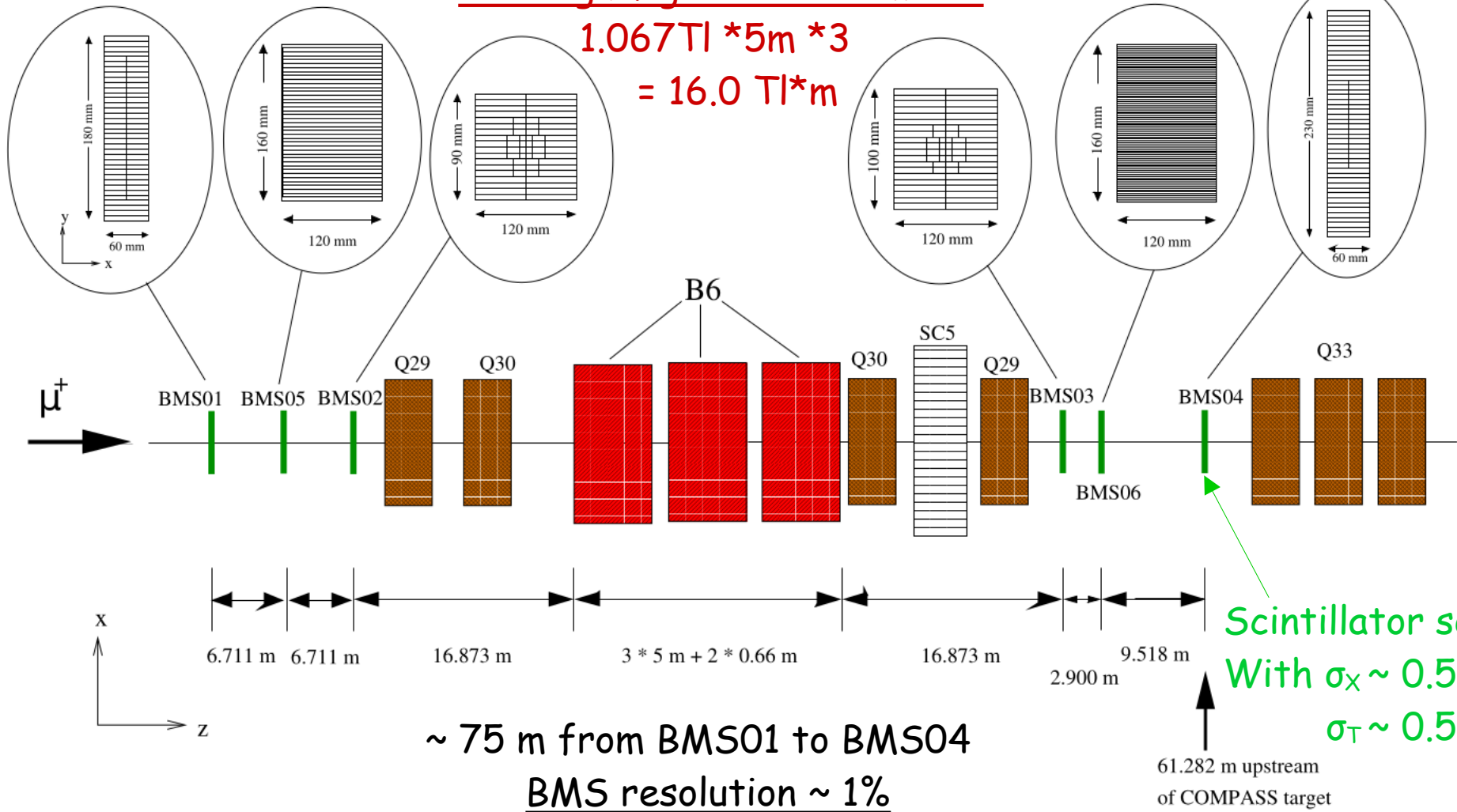
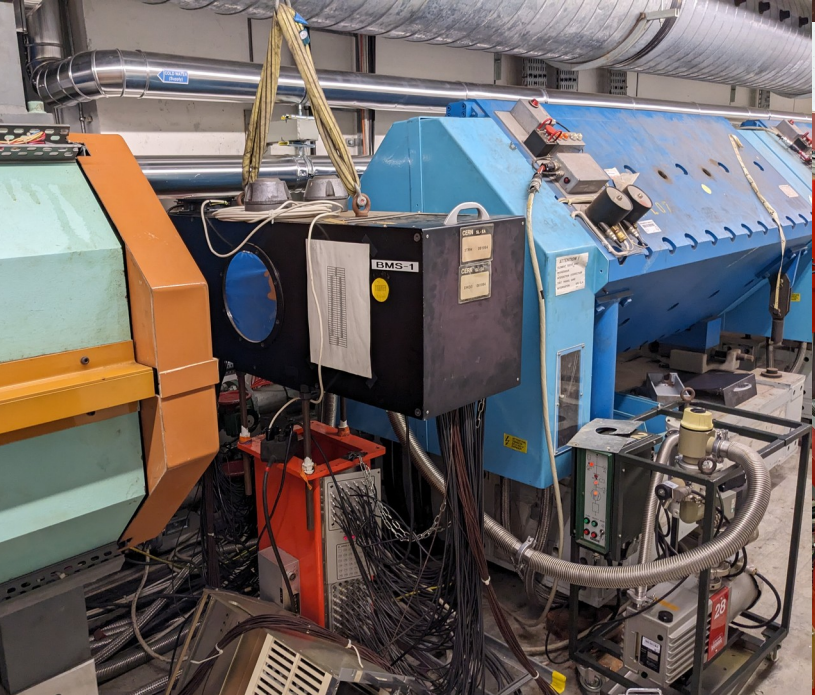


Figure 5.1: The schematic view of the Beam Momentum Station (BMS) setup. The green elements are the BMS detector planes. Their dimensions and division into channels is presented. The setup is positioned on two sides of the Bend 6 magnet group (B6). Elements marked with "Q" are the quadrupole magnets while the SC5 is a scraper. (The plot is not up to scale). Figure comes from Ref. [87].

Bending Magnets



Simulation

- x Geometry for M2 beamline: M2_BMS_To_CEDARs.gdml (update with Air in Scrapper (updated version since 21.07.23 MUonE weakly meeting, +42% Nevents after track selection)
- x Full magnetic fields in "parallel" configuration: Bends, Quadrupoles, Scarper
- x Beam profile: MuOnE_Muon_Beam_160GeV.root
- x Scintillator material of Hodoscope replaced by Air
- x 4 layers of 300 μ m Si sensors were added (in place of BMS1-4) - (for completeness, the material is not a issue)

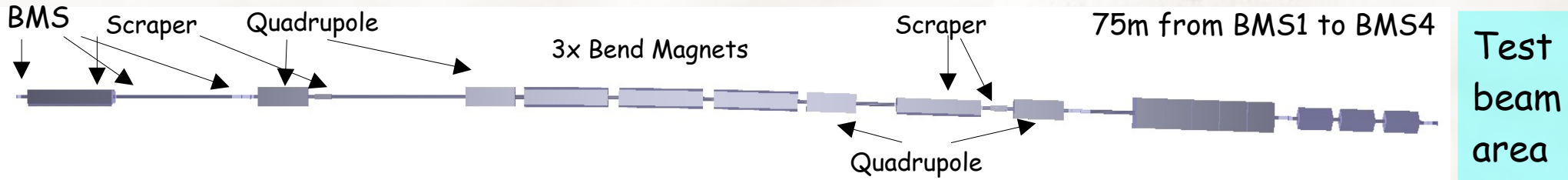
Provided by Fabian Metzger
from accelerator group

N.B. The additional geant4 tuning is required because of tracking over large volumes,
and tracking precision is crucial

Transported Muon

Thanks to Dipanwita and Fabian for providing the GDML description from BDSIM

detail GDML model



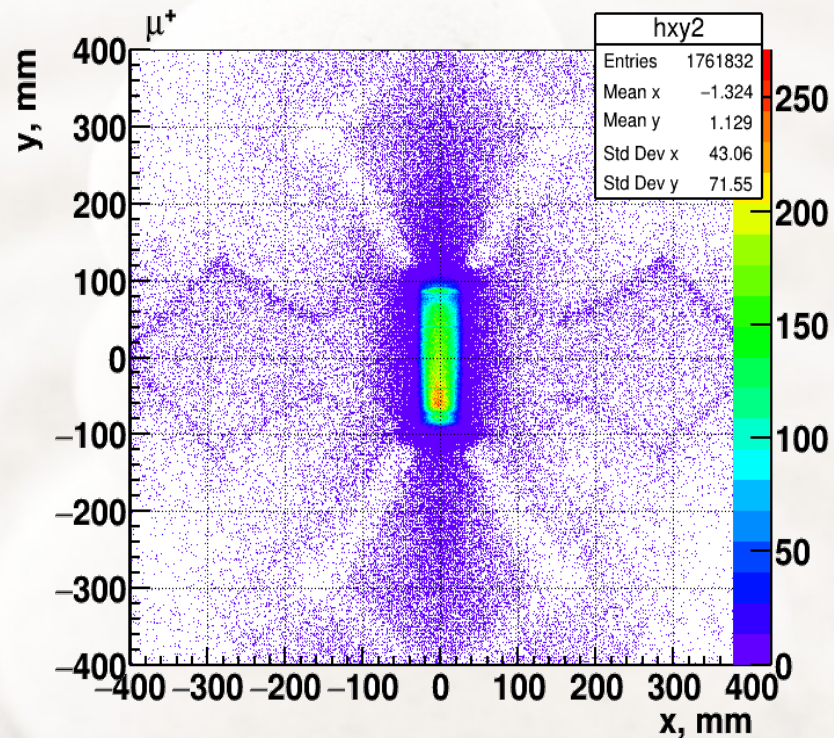
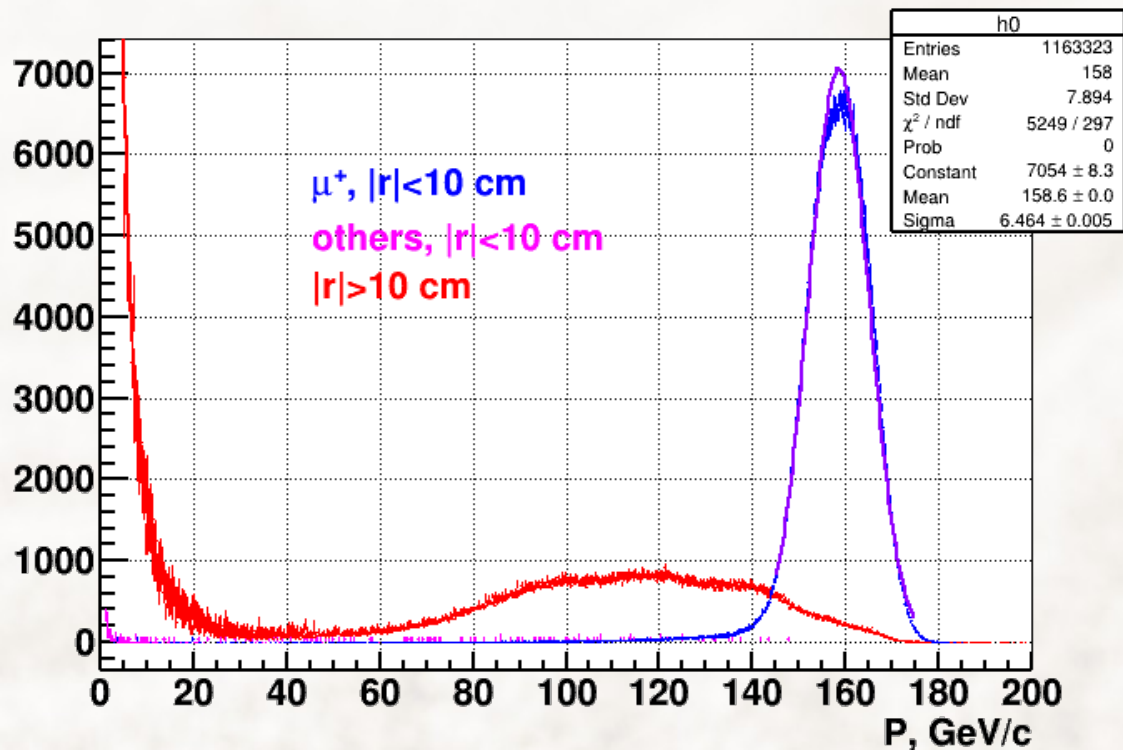
Material budget:

BMS01-06	~ 112 mm of Scintillator	= ~0.34 X0
Air gaps	14.3m	= 0.050 X0
Mylar windows	8*0.02 cm	= 0.019 X0
		$\Sigma = 0.4X0$

material of Si detector will be negligible:
 150 μ m Si = 0.0016 X0
 equivalent to 0.45m of Air

0.5 X/X0 $\rightarrow \Theta_{MS} \sim 3.5 \times 10^{-5}$ rad ,
 1 arm (13m) Hodoscope detector Θ resolution $\sim 2 \times 10^{-4}$ rad,
 $\sigma_P/P < 0.1\%$ require $\sim 3 \times 10^{-5}$ rad

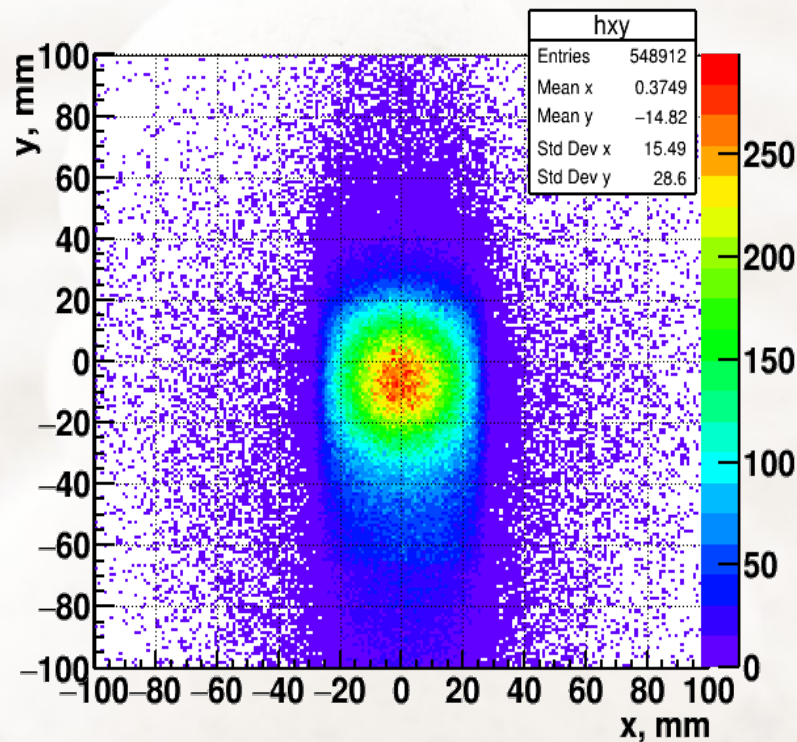
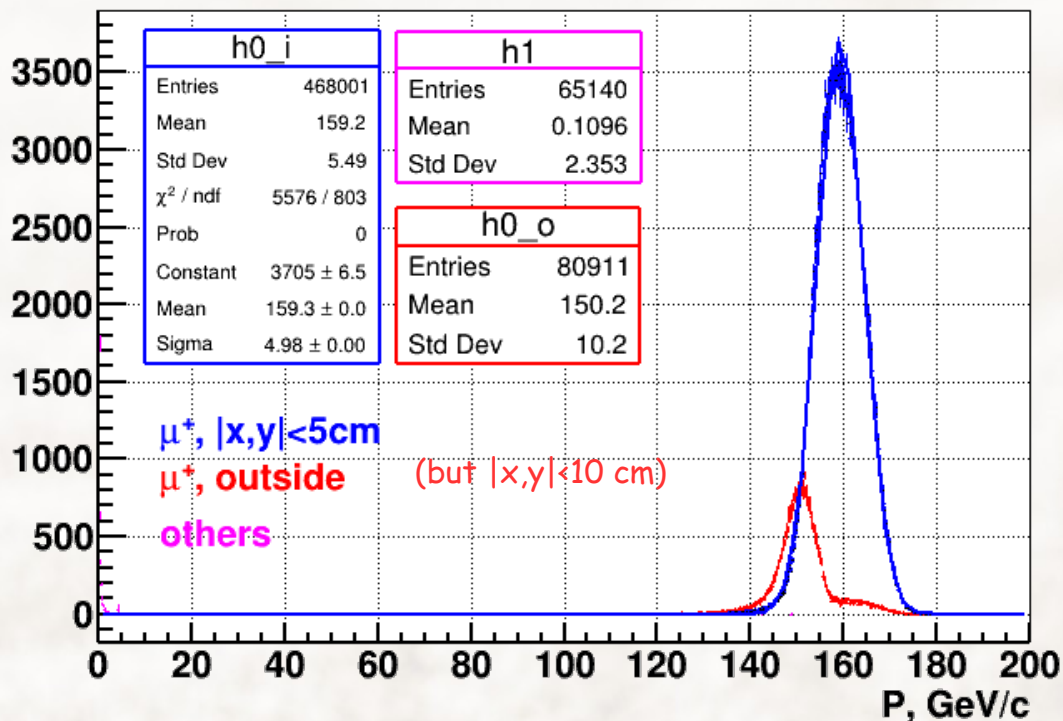
Beam at first BMS1



Beamspot $\sim 10 \times 20$ cm

Beam at entrance to CEDAR area

After passing BMS



at 20x20 cm area:

15% outside 10x10 cm area

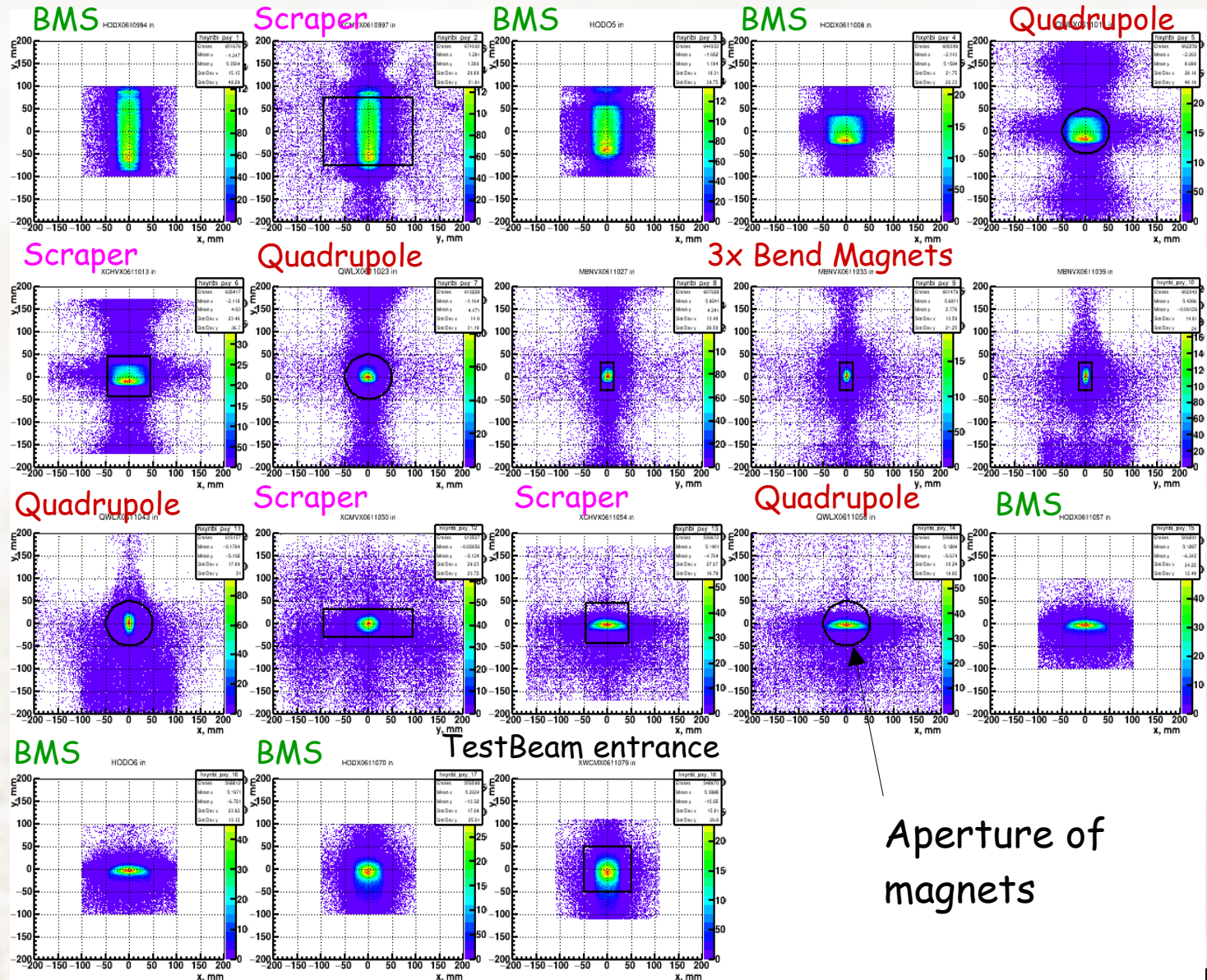
Low momentum tail:

7.6% γ , 4.1% e^- , 0.2% e^+ , 0.001% π^{+-}

$\sigma_x \sim 13.3\text{ mm}$,

$\sigma_y \sim 24.0\text{ mm}$,

Beam profile along beamline



μ^+ beam

1m sim events

0.65m μ^+ ($|r| < 10\text{cm}$)

without weights

transfer rate:

x71.8% to 10x10cm area

(x84.2% to 20x20cm area)

Aperture of magnets

Reconstruction

in/out tracks defined by two Si sensors

propagated through quadrupole magnets ($L=2.95\text{m}$ each) to the faces of Bend magnets

Momentum is taken from angle difference after passing the Bend magnets :

$$P = 160 \text{ GeV} * 0.03 \text{ rad}/(\theta^{\text{out}}_y - \theta^{\text{in}}_y)$$

Propagation is done assuming ideal quadrupole field $B=(B_0*y, B_0*x)$ (but full field in geant4)

Equation of motion (depend on sign of B_0):

$$y = c_1 * \exp(a*z) + c_2 * \exp(-a*z)$$

or
$$y = c_1 * \cos(a*z) + c_2 * \sin(a*z)$$

The exact field map can be used in the future (for trajectories at edge of acceptance)

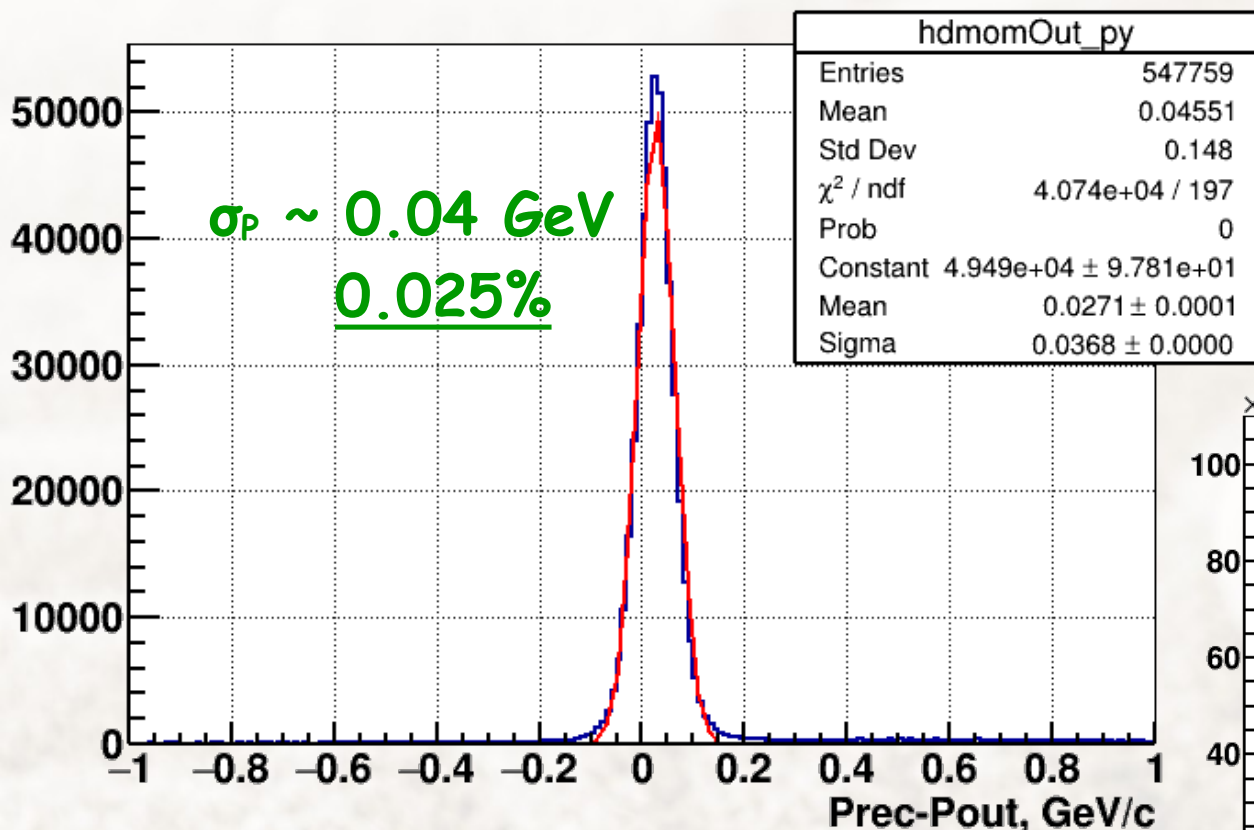
Matching between In/Out track position can be also used, resolution from MS $\sim O(\text{mm})$

will be useful to suppress background and overlaps (maybe can give also something for momentum resolution)

Momentum resolution (with 0 hit resolution)

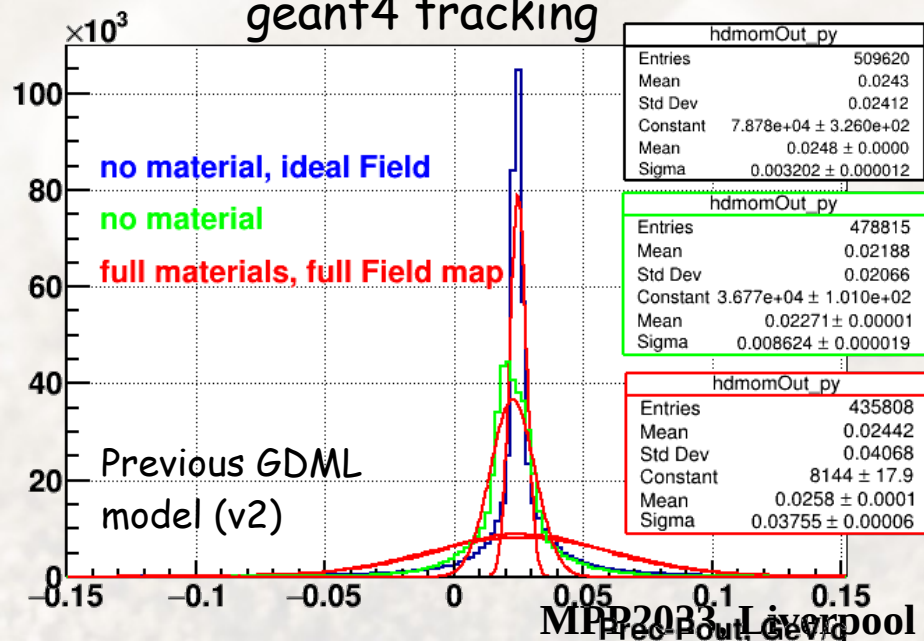
With exact position at Si planes (zero hit resolution)

Muons which cross all 4 Si planes (r=10 cm) and last volume within 20x20cm (84% from initial)



Small bias is probably from the geant4 tracking precision (non-continuous field)

Effect of material and non-homogeneous B field, geant4 tracking



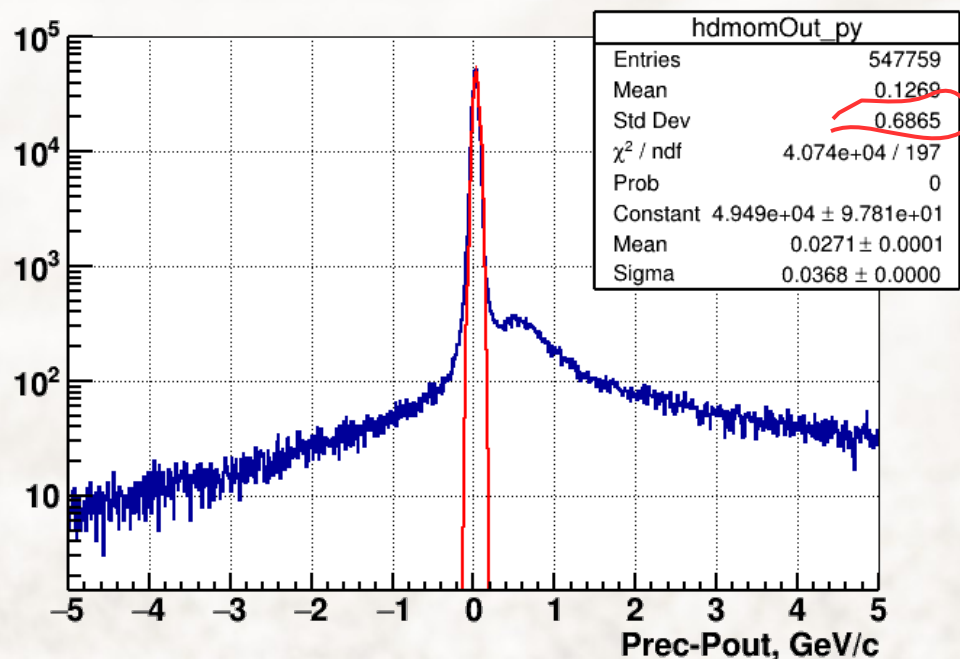
Previous GDML model (v2)

Momentum resolution tails

With exact position at Si planes (zero hit resolution)

Muons which cross all 4 Si planes ($r=10$ cm) and last volume within 20×20 cm (84% from initial)

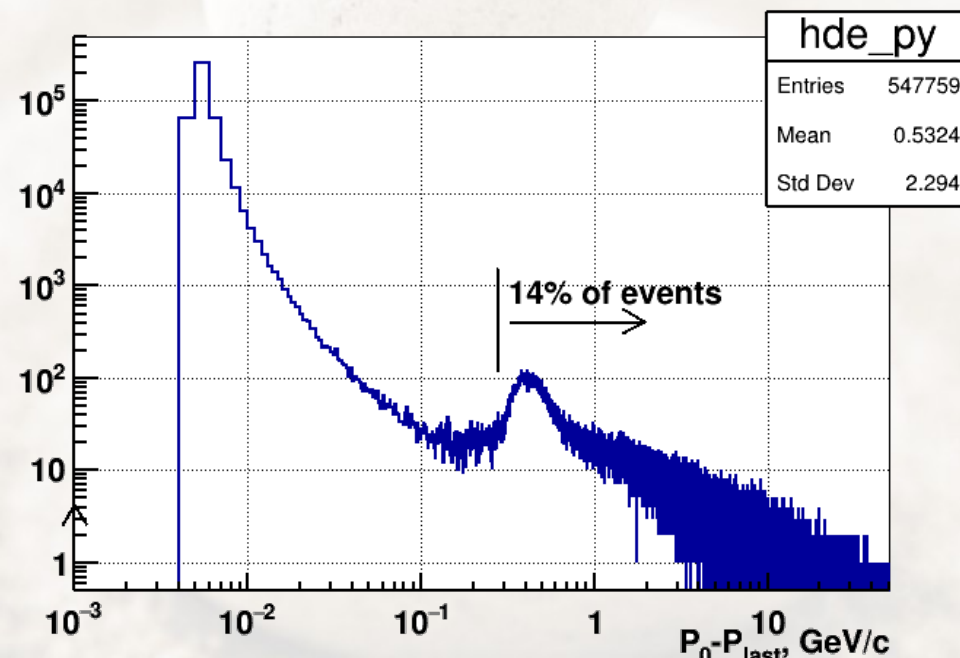
Tails in reconstructed P



$$\text{RMS}/P_0 = 0.4\%$$

$$13.7\% \text{ in } |dP| > 0.32 \text{ GeV}/c$$

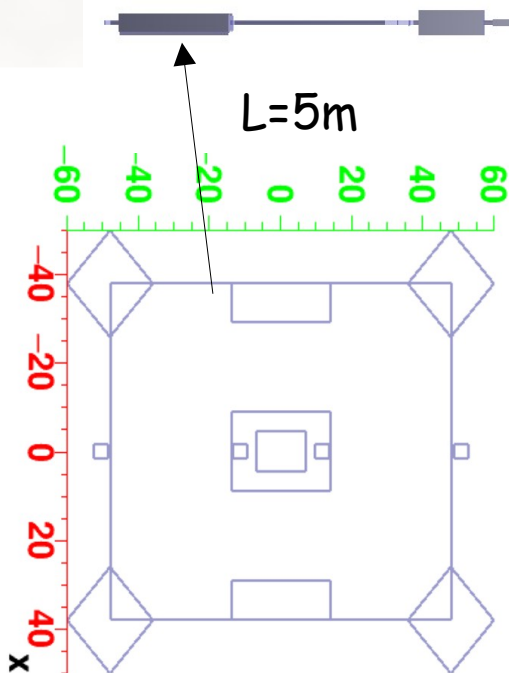
Energy loss of μ^+ over M2 beamline



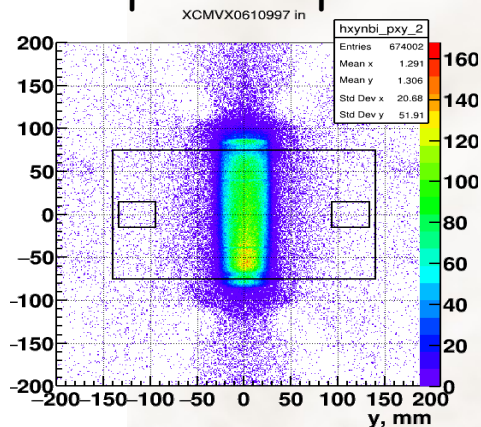
14% muons have loss > 0.3 GeV

Scraper

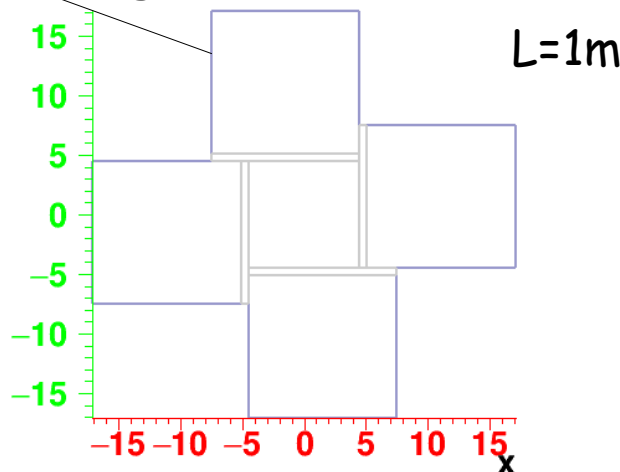
Muon beam doesn't fit to all beamline element acceptance



Scraper acceptance



Build from iron, tungsten bricks



scrapers operates in Air

Track filtration can be performed by reconstructed trajectory:

on Bend entrance/exit: $31.5 \times 2 \times 14 \times 2$ mm

Quad4 out face: $r=49\text{mm}$, Scraper1 : 75×94 Mm

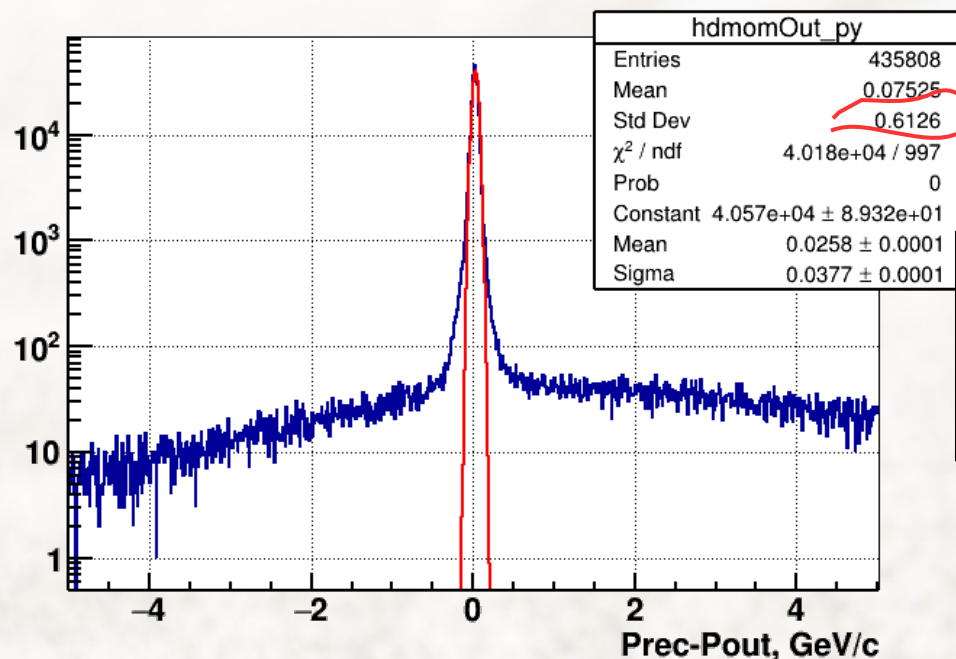
Can be performed more accurate on all elements

First GDML version was for the electron beam configuration (much narrower inner acceptance of Iron bricks)
2nd version with iron vacuum tube in 1st Scraper (now just Air)

Momentum resolution tails

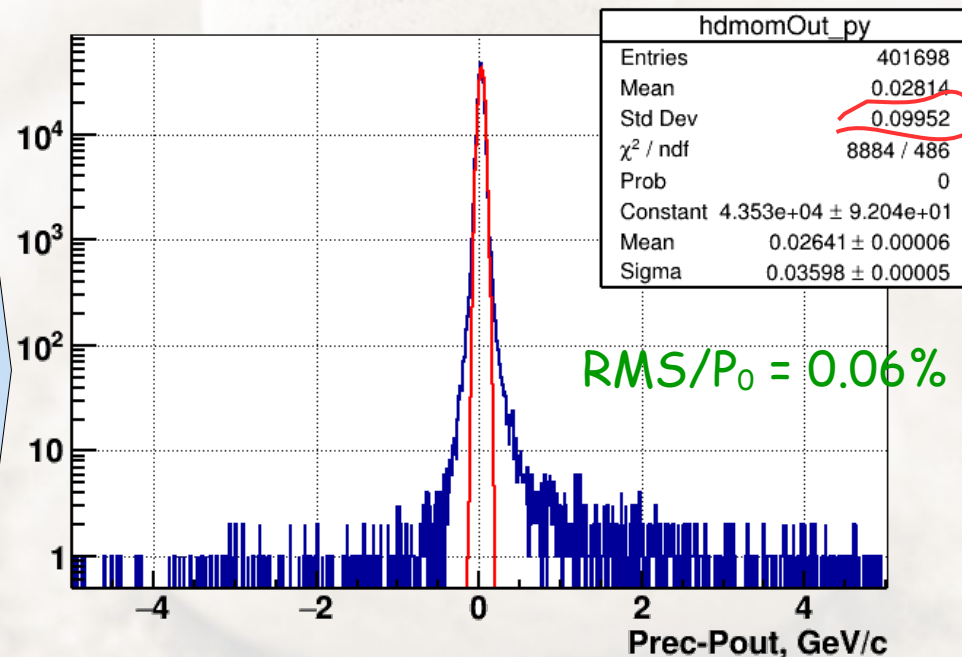
Track filtration can be performed by reconstructed trajectory:

10x10 cm vtx area at entrance to CEDAR
Crossing all 4 BMS
 $|P_{rec} - 160| < 15 \text{ GeV}$



6.3% in $|dP| > 0.32 \text{ GeV}/c$

Additional cut with help of reconstructed trajectory by not crossing beamline elements (some of them)

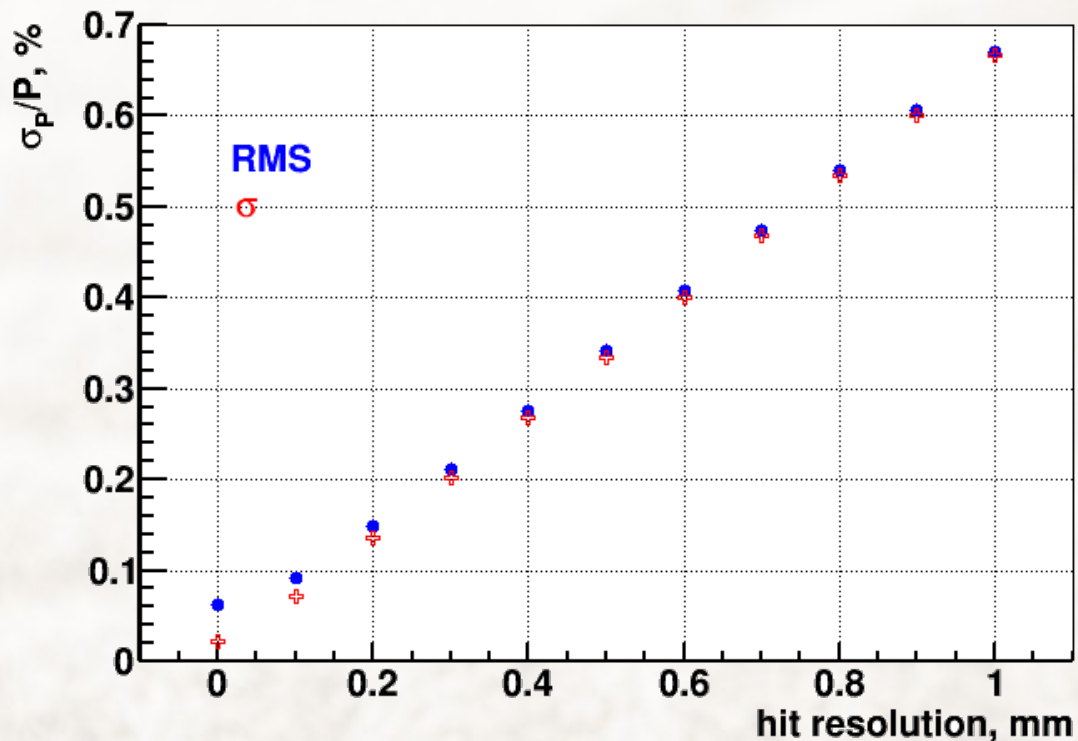


Selection efficiency

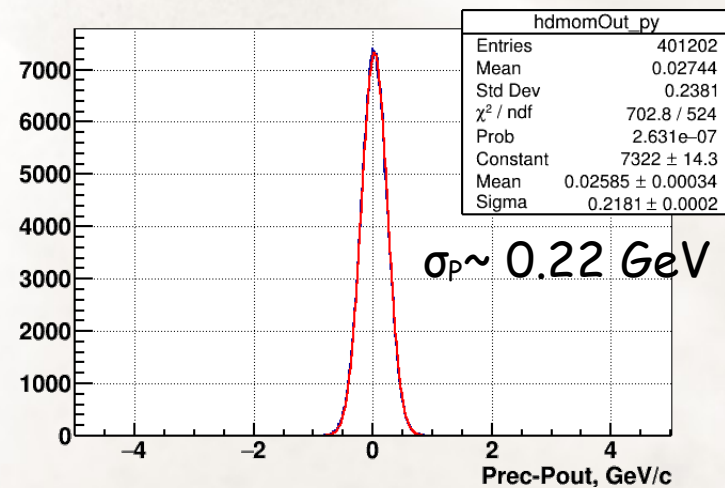
85.8% relative to left plot

still 0.3% in $|dP| > 0.32 \text{ GeV}/c$

Momentum resolution vs Hit resolution



Hit resolution 200 μm



Conclusion

- x BMS potentially can provide momentum resolution $\sim 0.1\%$
- x BMS with event-by-event matching with MuonE scattering:
 - x can increase MUonE sensitive by factor 2 (at cost of 1 additional station over 40)
 - x works as active filter to clean-up contaminations and tails in used beam

Sensor requirements:

Few of them must be 20x10cm , most 10x10 cm

X-Y planes to reconstruct trajectory over not crossing beam elements

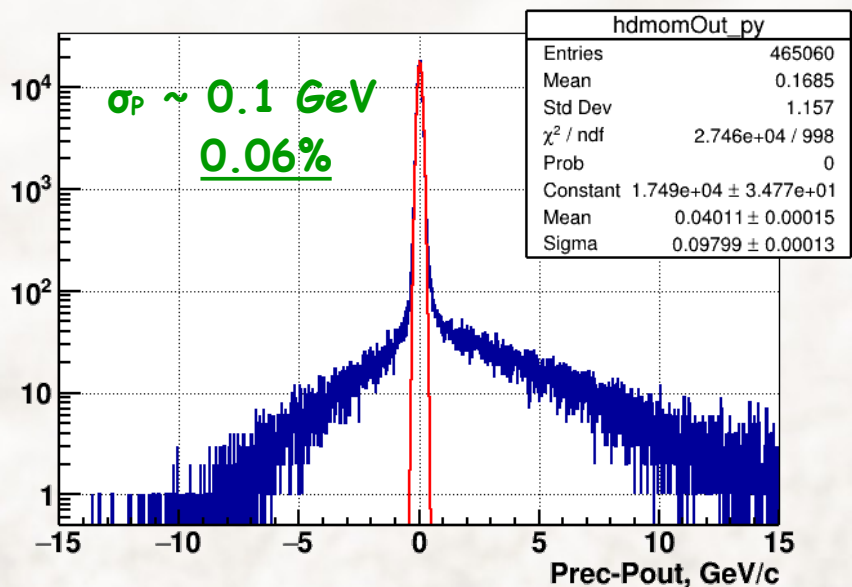
Timing to ease matching with main MUonE tracker

Redundancy (at least 2x3x2 layers) to have high efficiency

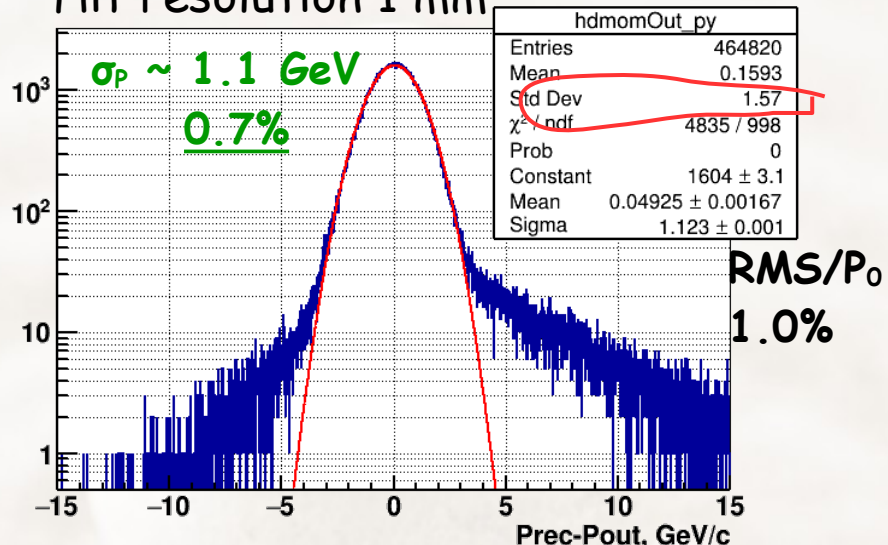
Momentum resolution with original Hodoscope

μ selected by passing 10x10 cm vtx area at entrance to CEDAR & $|P_{rec} - 160| < 15 \text{ GeV}$

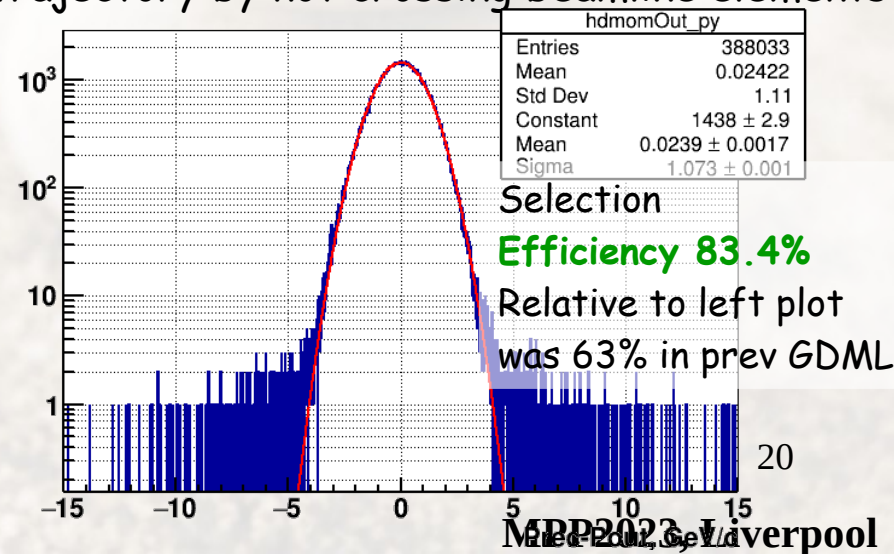
Effect of Scintillator material,
hit resolution = 0



Hit resolution 1 mm



Additional cut with help of reconstructed trajectory by not crossing beamline elements



Momentum resolution

Requirement for $\sigma_P/P \sim 0.1\%$:

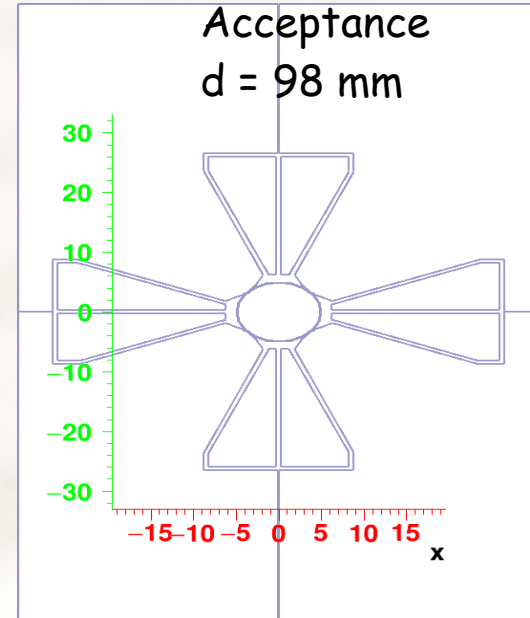
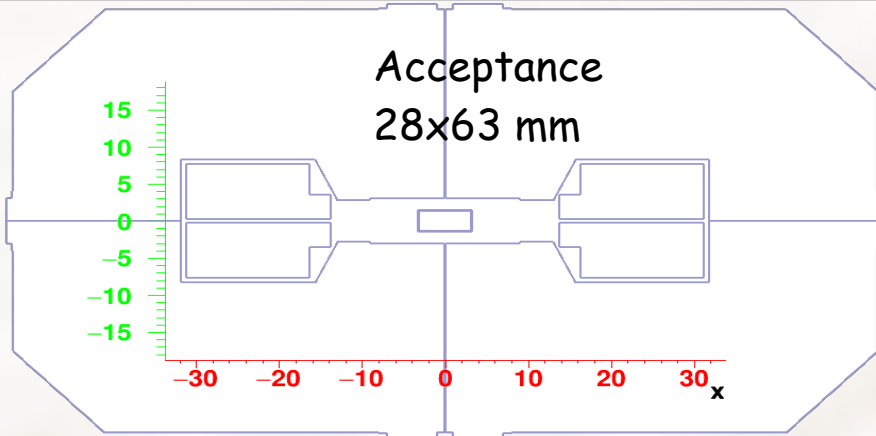
- x Bend magnet knowledge $\sim 0.1\%$
- x Quadrupole magnet knowledge $\sim 1\%$
- x Angle resolution of in/out arm: 0.02mrad
→ hit resolution (on 10 m arm) : $150\ \mu\text{m}$
- x Impact point on Quadrupole magnet: $\sim 200\ \mu\text{m}$
- x Alignment: $< 150\ \mu\text{m}$

Questions:

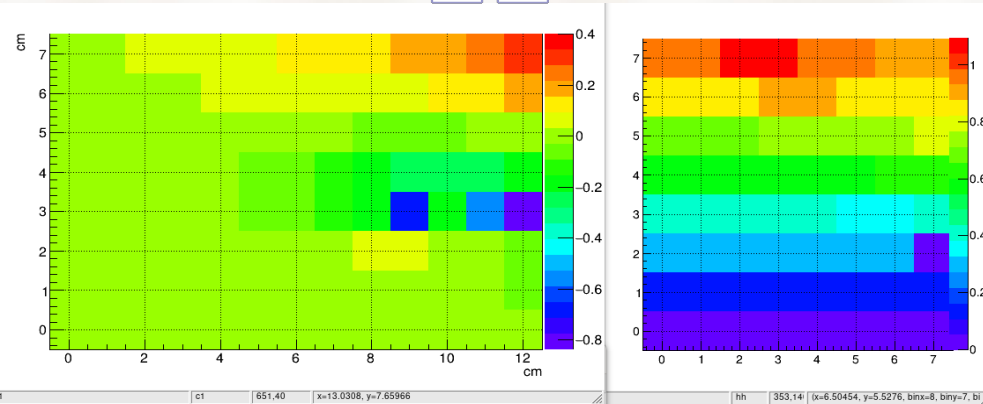
- x B field knowledge and stability
- x Alignment
- x Background events (when tracks crossed vacuum tube)
- x Geometry optimization
- x Timing layers

Field Maps

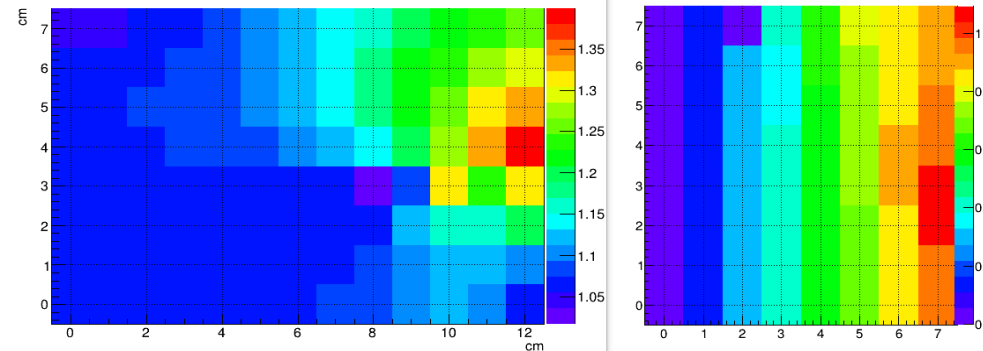
+rotated
90deg



B_x



B_y

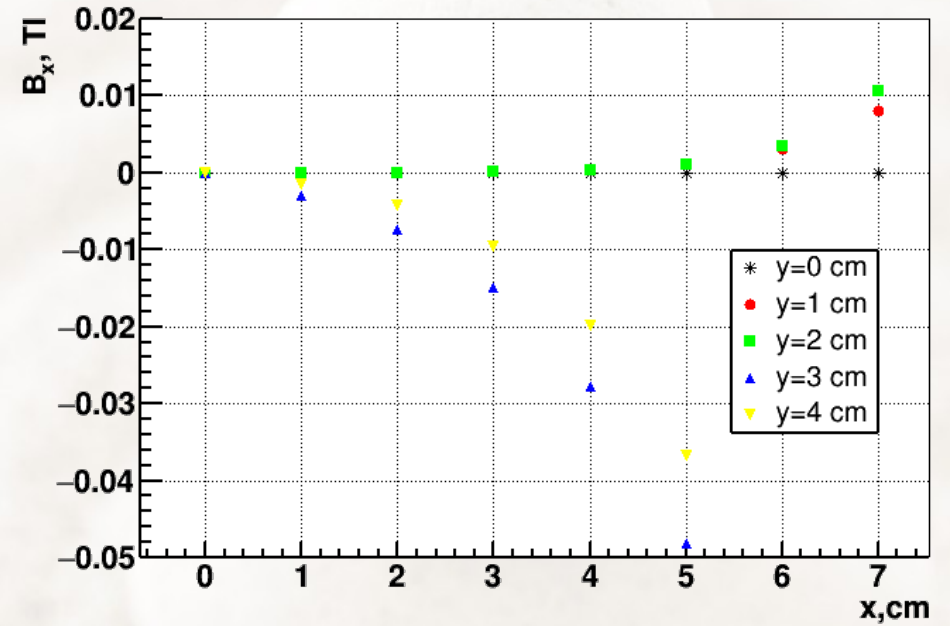
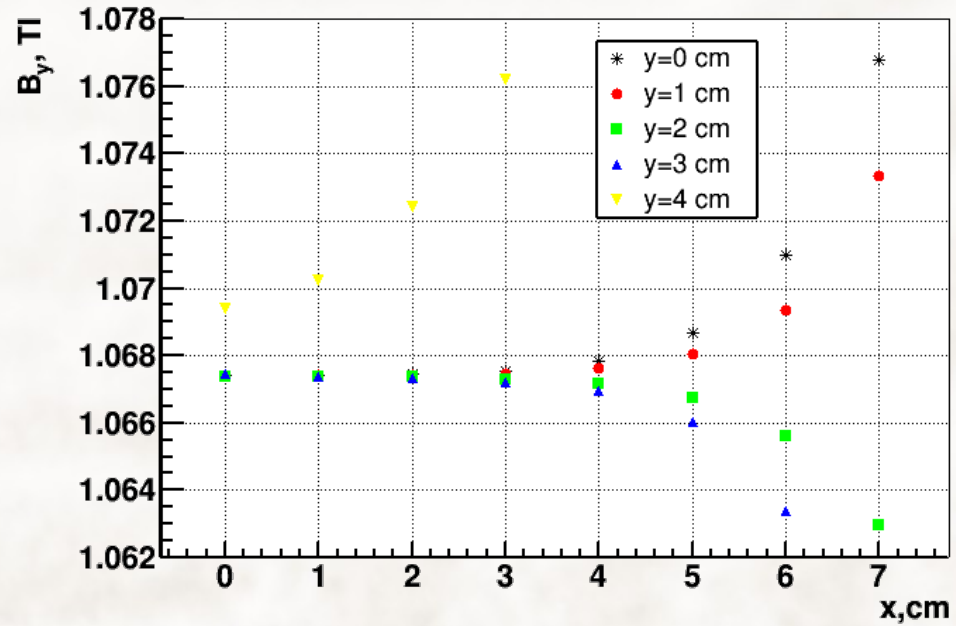


2D Field map is provided with 1x1 cm step

Symmetrical over origin

B_y is constant at $\sim 0.02\%$ Inside of 60x60mm

Bx By field



BMS hodoscope

The COMPASS experiment at CERN, 2007
<https://inspirehep.net/literature/747655>

Station	# of dets.	Planes per det.	# of ch. per det.	Active area $X \times Y$ (cm ²)	Resolution
Beam detectors					
BM01-04	4	Y	64	6 – 12 × 9 – 23	$\sigma_s = 1.3 - 2.5$ mm, $\sigma_t = 0.3$ ns
BM05	2	Y	64	12 × 16	$\sigma_s = 0.7$ mm, $\sigma_t = 0.5$ ns
BM06	2	Y	128	12 × 16	$\sigma_s = 0.4$ mm, $\sigma_t = 0.5$ ns

Bending Magnet:

$$1.067 \text{ Tl} * 5 \text{ m} * 3 = 16.0 \text{ Tl} * \text{m}$$

Or deflection power $\Delta\phi = (B*L)*0.29979/P \rightarrow 0.03$ rad for $P=160$ GeV

4 Quadrupole magnets (L=2.95m): $B=(B_0*y, B_0*x)$,

“Parallel” optic: $B_0 = 0.1397, -0.1128, -0.2067, 0.1462$ Tl/cm

“short” optic: $B_0 = 0.1397, -0.1128, -0.2127, 0.1761$ Tl/cm

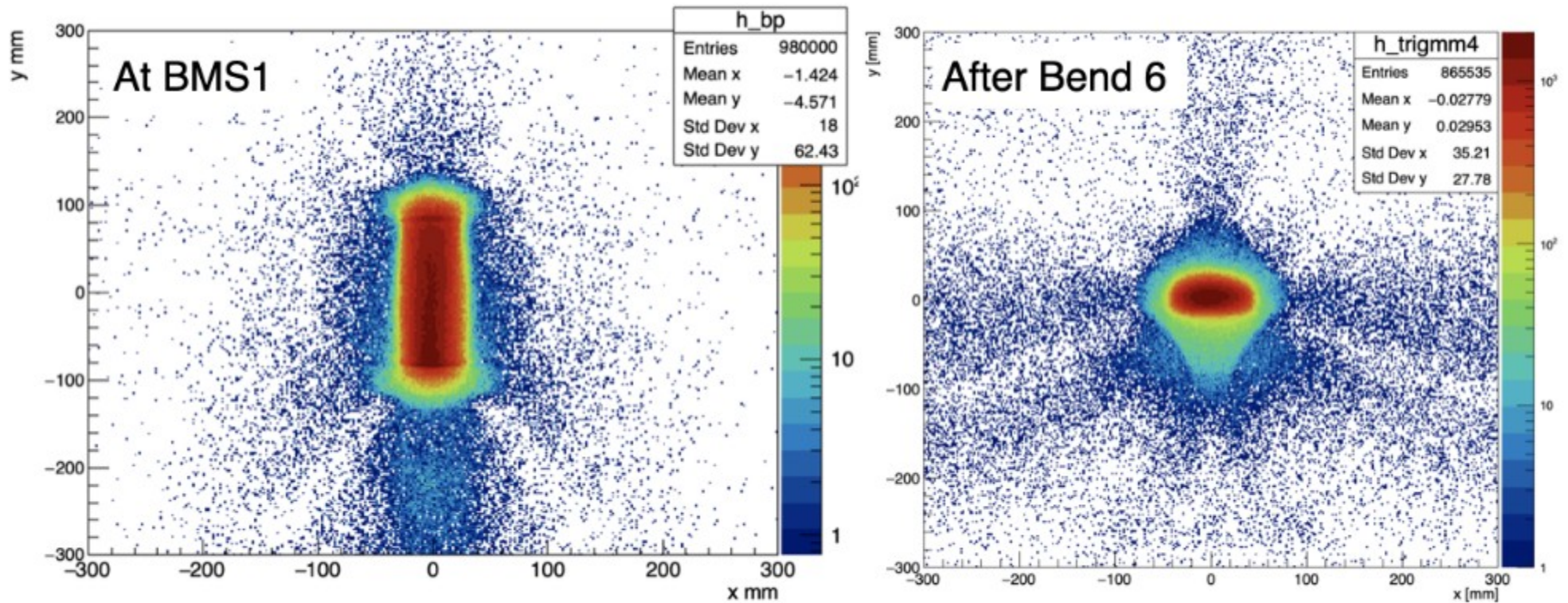
$$\Delta\phi/r \sim 1 \times 10^{-4} \text{ rad/mm}$$

$$0.5 X/X_0 \rightarrow \Theta_{MS} \sim 3.5 \times 10^{-5} \text{ rad},$$

1 arm (13m) Hodoscope detector Θ resolution $\sim 2 \times 10^{-4}$ rad

$$\sigma_p/P = \sqrt{2} * 2 \times 10^{-4} \text{ rad} / 0.03 \text{ rad} \sim 1\%$$

Beam profile at BMS



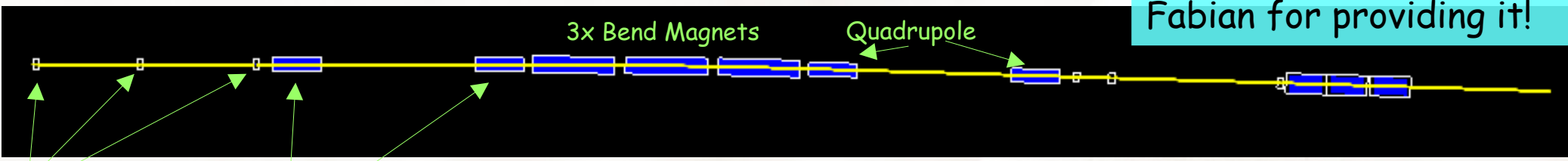
NA64 Status Report 2022

<https://cds.cern.ch/record/2811174/files/SPSC-SR-316.pdf>

Transported Muon

First simplified geometry with muon track

Thanks to Dipanwita and Fabian for providing it!



Material budget:

BMS01-04 ~ 20 mm of Scintillator → ~0.06 X_0 per station (x4)

BMS05-06 ~ 16 mm → ~0.05 per station (x2)

4 Air gaps $0.46 + 1.44 + 1.45 + 0.84 = 4.3\text{m} = 0.014 X_0$

2x Scrapper (with QP Field) in Air : 10. m = 0.036 X_0

Mylar window $8 \times 0.02\text{ cm} = 0.019 X_0$

$$\Sigma = 0.4X_0$$

X/X_0 of Si detector will be negligible:

Can be compared as $150\mu\text{m Si} \rightarrow 0.0016 X_0$ or 0.45m of Air

Half of total $X/X_0 \rightarrow \Theta_{MS} \sim 3.5 \times 10^{-5} \text{ rad}$,

1 arm (13m) Hodoscope detector Θ resolution $\sim 2 \times 10^{-4} \text{ rad}$,

9 November 2023 $\sigma_P/P < 0.1\%$ require $\sim 3 \times 10^{-5} \text{ rad}$

Simulation

- x Geometry for M2 beamline: M2_BMS_To_CEDARs.gdml (update with Air in Scrapper)
- x Full magnetic fields in "parallel" configuration: Bends, Quadrupoles, Scarper
- x Beam profile: MuOnE_Muon_Beam_160GeV.root
- x Scintillator material of Hodoscope replaced by Air
- x 4 layers of 300 μ m Si sensors were added (in place of BMS1-4) - (just for completeness, it is not a issue)

Provided by Fabian Metzger
from accelerator group

N.B. When tracking precision is crucial and large volumes are used, the default geant4 configuration of the track propagator in field should be tuned. The tracking can be checked by doing trajectory reconstruction with switched off materials, etc effects in simulation.

Runge Kutta propagator doesn't like a non-continuous field behaviour \rightarrow some small residual bias effect will be seen on the momentum resolution plots.