
Status of charged lepton flavour violation searches and lepton universality tests

Alberto Lusiani
Scuola Normale Superiore and INFN, sezione di Pisa



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Introduction

Lepton flavour violation (LFV)

- ▶ Standard Model accidental symmetry conserves L_e, L_μ, L_τ
- ▶ ν SM (including neutrino mixing) predicts extremely suppressed charged Lepton Flavour Violation, ($\propto m_{\nu_i}^2/m_W^2$),
e.g., $\mathcal{B}(\mu \rightarrow e\gamma) \sim 10^{-54}$
⇒ can do clean searches for New Physics
- ▶ LFV processes
 - ▶ muon LFV decays
 - ▶ tau LFV decays
 - ▶ hadrons, $W/Z, H$ decays to leptons

Lepton flavour universality (LFU)

- ▶ Standard Model predicts universal couplings for leptons with only exception of Higgs Yukawa couplings
- ▶ most tested:
charged-weak-current couplings universality
- ▶ precise SM predictions of coupling ratios
⇒ can search for small NP deviations
⇒ can obtain constraints on NP models
- ▶ lepton universality tests related to
 - ▶ B anomalies ($R_D, R_{D^*}, R_K, R_K^*, \dots$)
 - ▶ Cabibbo angle anomaly

Lepton Flavour Violation

Experimental searches for LFV processes

Process	Current bound on BR	Future Sensitivity
$\mu \rightarrow e\gamma$	$< 4.2 \times 10^{-13}$ MEG	10^{-14} MEGII
$\mu \rightarrow \bar{e}ee$	$< 1.0 \times 10^{-12}$ SINDRUM	10^{-16} Mu3e
$\mu A \rightarrow eA$	$< 7 \times 10^{-13}$ SINDRUMII	$10^{-16} \rightarrow 10^{-18}$ COMET, Mu2e
$\tau \rightarrow l\gamma$	$< 3.3 \times 10^{-8}$	$3 \times 10^{-9}(e), 10^{-9}(\mu)$
$\tau \rightarrow e\bar{e}e$	$< 2.7 \times 10^{-8}$	5×10^{-9}
$\tau \rightarrow \mu\bar{\mu}\mu$	$< 2.1 \times 10^{-8}$	4×10^{-9}
$\tau \rightarrow \mu\bar{e}e, e\bar{\mu}\mu$	$< 1.8, 2.7 \times 10^{-8}$ Belle	$3, 5 \times 10^{-9}$ BelleII
...
$\tau \rightarrow l\pi^0$	$< 8.0 \times 10^{-8}$	4×10^{-9}
$\tau \rightarrow l\eta$	$< 6.5 \times 10^{-8}$	7×10^{-9}
$\tau \rightarrow l\rho$	$< 1.2 \times 10^{-8}$ Belle	10^{-9} BelleII
$K^0 \rightarrow \mu^\pm e^\mp$	$< 4.7 \times 10^{-12}$	
$B_d^0 \rightarrow \tau^\pm \mu^\mp$	$< 1.2 \times 10^{-5}$ LHCb	$\sim 10^{-6}$?
...
$h \rightarrow e^\pm \mu^\mp$	$< 6.1 \times 10^{-5}$ Atlas	2.1×10^{-5}
$h \rightarrow e^\pm \tau^\mp$	$< 2.2 \times 10^{-3}$ CMS	2.4×10^{-4}
$h \rightarrow \tau^\pm \mu^\mp$	$< 1.5 \times 10^{-3}$ CMS	2.3×10^{-4} ILC
$Z \rightarrow e^\pm \mu^\mp$	$< 7.5 \times 10^{-7}$ Atlas	
$Z \rightarrow l^\pm \tau^\mp$	$< 10^{-7}$ Atlas	

[M.Ardu, CLFV 2023]

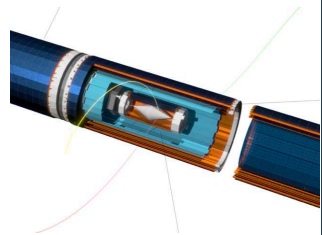
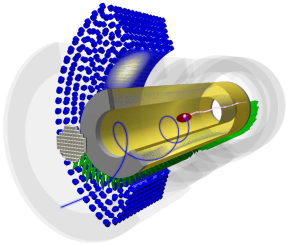
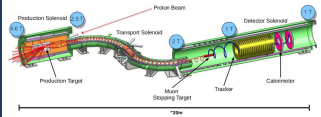
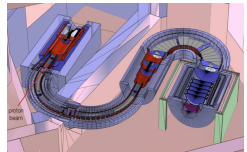
- ▶ muon searches most sensitive
- ▶ tau searches probe many operators
can distinguish models
- ▶ W, Z, H , hadrons decays complementary

Muon CLFV experiments

$$\mu^- N \rightarrow e^- N$$

$$\mu^+ \rightarrow e^+ \gamma$$

$$\mu^+ \rightarrow e^+ e^- e^+$$



[T.Mori, ICHEP 2022]

Muon CLFV experiments

$$\mu^- N \rightarrow e^- N$$

- ▶ signal: monochromatic $\sim 104\text{MeV}$ electron
- ▶ BG: beam-related prompt
- ▶ pulsed muon beam
- ▶ "extinction" of $\sim 10^{-10}$
- ▶ low mass tracker

$$\mu^+ \rightarrow e^+ \gamma$$

- ▶ signal: 2-body kinematics
- ▶ BG: accidental
- ▶ DC muon beam
- ▶ low mass tracker
- ▶ excellent gamma-ray measurement

$$\mu^+ \rightarrow e^+ e^- e^+$$

- ▶ signal: 3-body kinematics
- ▶ BG: accidental
- ▶ DC muon beam
- ▶ low mass tracker

[T.Mori, ICHEP 2022]

Muon CLFV experiments

$$\mu^- N \rightarrow e^- N$$

COMET & Mu2e

π capture and π, μ transport
by solenoids

prompt

- ▶ pulsed muon beam
- ▶ "extinction" of π
- ▶ low mass tracker

$$\mu^+ \rightarrow e^+ \gamma$$

MEG II

gradient field spectrometer
& LXe photon detector

▶ DC muon beam

- ▶ excellent gamma-ray
measurement

$$\mu^+ \rightarrow e^+ e^- e^+$$

Mu3e

low mass pixel tracker
based on HV-MAPS

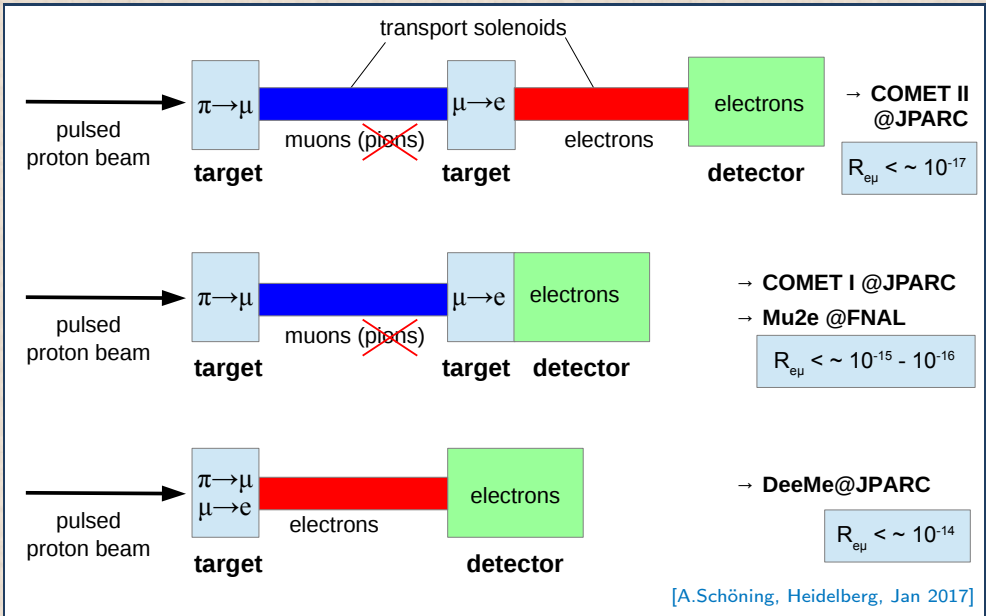
BG: accidental

▶ DC muon beam
▶ low mass tracker

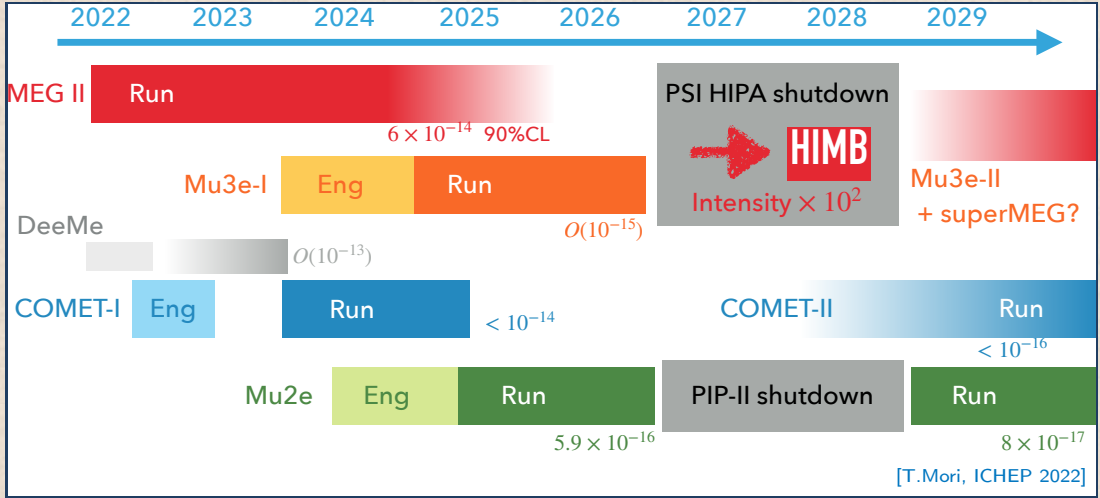
**INNOVATIVE EXPERIMENTAL TECHNIQUES
ARE DRIVING FORCE**

[T.Mori, ICHEP 2022]

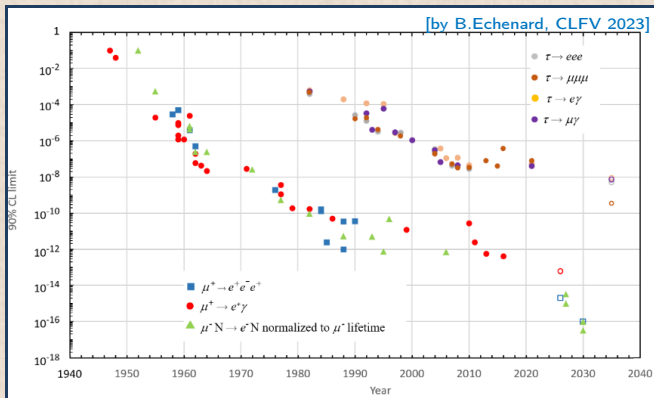
Searches for muon conversion in nuclei, techniques



Timeline of muon CLFV experiments



Muon LFV searches status and prospects



1st MEG-II search published

- ▶ MEG-II Run 1 (2021) search
Euro.Phys.J.C 84 (2024) 3, 216
 $\mathcal{B}(\mu^+ \rightarrow e^+ \gamma) < 7.5 \cdot 10^{-13}$ (90% CL)
- ▶ combined MEG 2016 + MEG-II 2024:
 $\mathcal{B}(\mu^+ \rightarrow e^+ \gamma) < 3.1 \cdot 10^{-13}$ (90% CL)
- ▶ MEG 2016 final limit was:
 $[\mathcal{B}(\mu^+ \rightarrow e^+ \gamma) < 4.2 \cdot 10^{-13}$ (90% CL)]

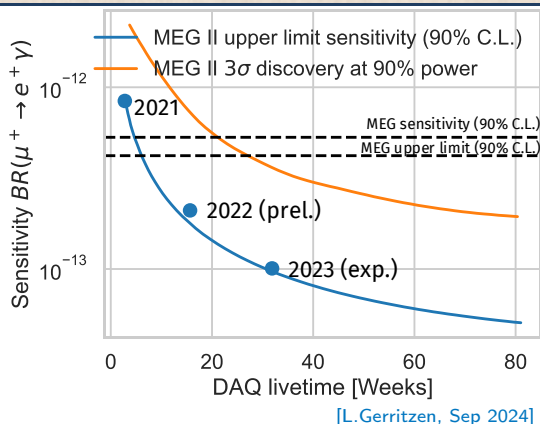
MEG-II vs. MEG detector performances

	Δp_{e^+}	$\Delta \theta_{e^+}$	ΔE_γ	$\Delta \vec{x}$	$\Delta t_{e\gamma}$	ε_{e^+}	ε_γ
MEG	380 keV	9.4 mrad	2.4%/1.7%	5 mm	122 ps	30%	63%
MEG II (21)	89 keV	7.2 mrad	2.0%/1.8%	2.5mm	78 ps	67%	62%
MEG II (22)	79 keV	6.2 mrad	TBD	2.5 mm	TBD	67%	62%

[L.Gerritzen, Sep 2024]

Future MEG + MEG-II sensitivity

- 2021 analysis published in January (no discovery)
- 2022 will follow soon
- 2023 dataset bigger than 2021+2022 combined
- 2024: likely short run
- 2025-2026: Ready to take data



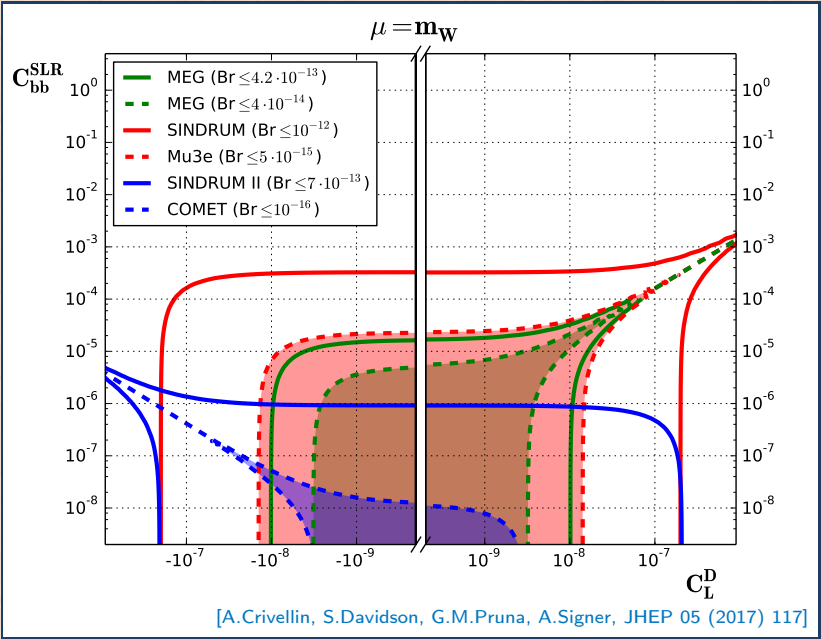
Comparison and complementarity of muon LFV searches

- ▶ model-independent parametrization of New Physics with SMEFT

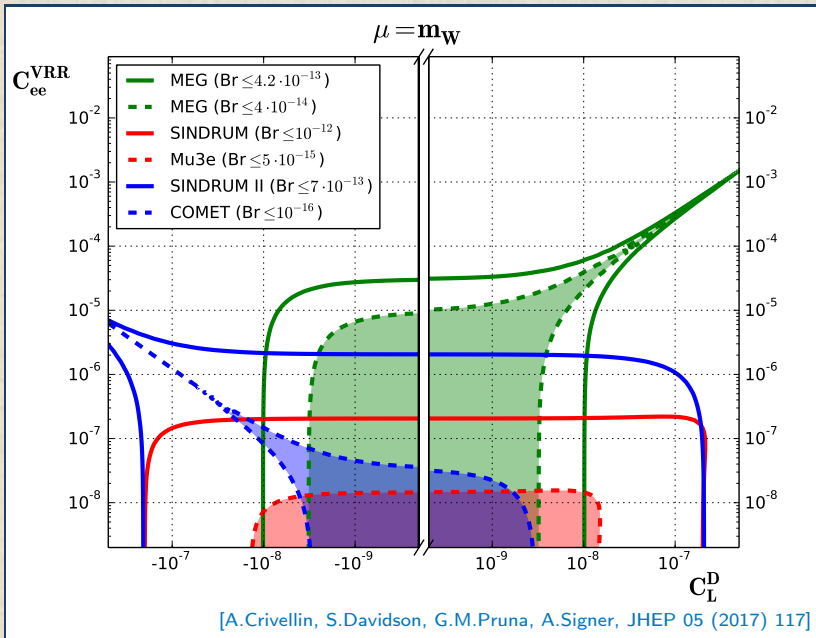
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \sum_k C_k^{(5)} Q_k^{(5)} + \frac{1}{\Lambda^2} \sum_k C_k^{(6)} Q_k^{(6)} + \dots$$

- ▶ scale-dependent Wilson coefficients (renormalization)
- ▶ use **EW scale as reference** to compare Wilson coefficients constraints from experimental measurements at different energy scales

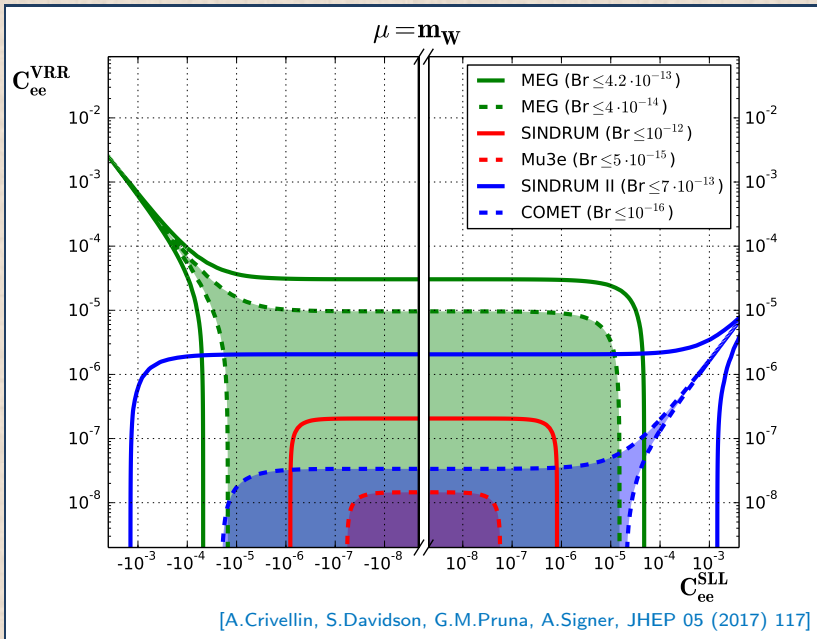
Comparison and complementarity of muon LFV searches



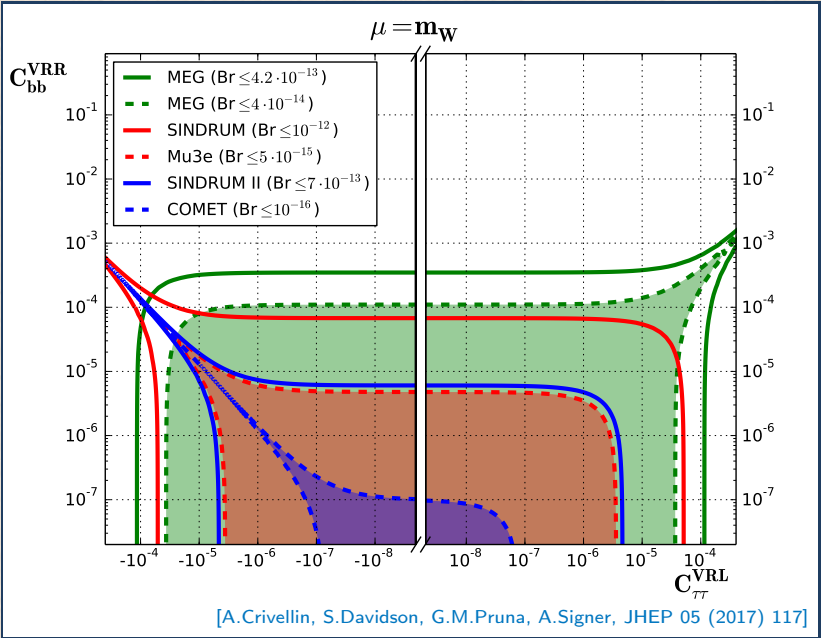
Comparison and complementarity of muon LFV searches



Comparison and complementarity of muon LFV searches



Comparison and complementarity of muon LFV searches



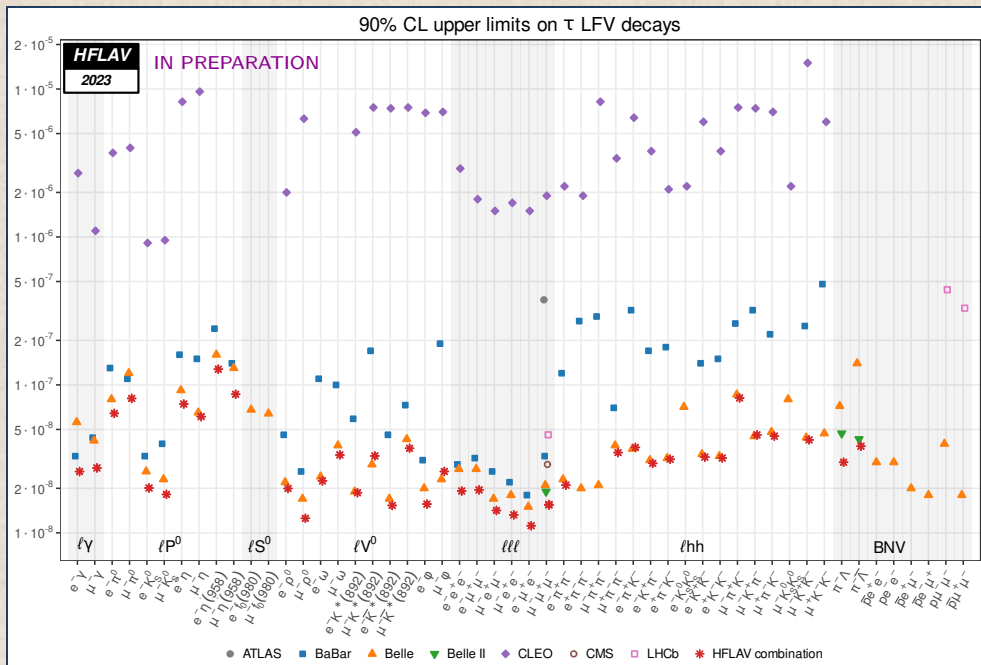
Searches for LFV in tau decays

- ▶ present upper limits mainly from CLEO, *BABAR*, Belle
- ▶ LHCb, CMS and ATLAS performed searches on $\tau^- \rightarrow \mu^- \mu^+ \mu^-$, $\tau^- \rightarrow \bar{\nu} \mu^+ \mu^-$
- ▶ Belle II will significantly improve *B*-factories limits
- ▶ possible future players FCC-ee(Z), CEPC, STCF

new Belle II limit on $\tau^- \rightarrow \mu^- \mu^+ \mu^-$

- ▶ $\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 1.9 \cdot 10^{-8}$ [JHEP 09 \(2024\) 062](#), 424 fb^{-1}
- ▶ previous $\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 2.1 \cdot 10^{-8}$ 90% CL, [Phys.Lett.B687 \(2010\) 139-143](#), 782 fb^{-1}

Tau LFV decay upper limits



Facilities for tau lepton measurements

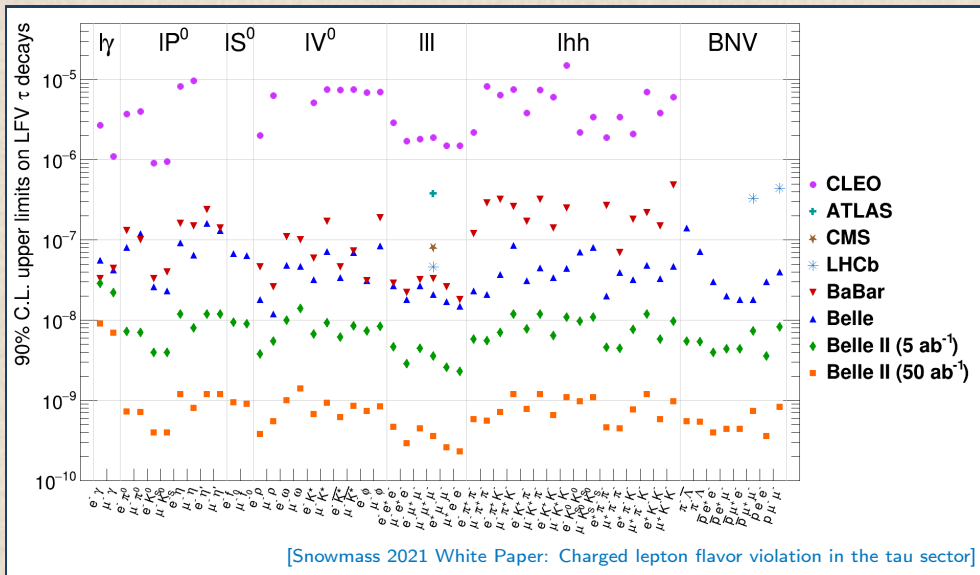
tau pairs yields at past, present and future e^+e^- colliders

facility	Z [million]	$\tau^+\tau^-$ [million]	$\tau^+\tau^-$ relative sample size	
LEP	25	0.84		
<i>BABAR</i>	-	$0.5 \cdot 10^3$		
Belle	-	$1.0 \cdot 10^3$		
Belle II	-	$45 \cdot 10^3$		
STCF at 4.26 GeV, 10 years	-	$35 \cdot 10^3$		
CEPC	$4 \cdot 10^6$	$135 \cdot 10^3$	$1.6 \cdot 10^5 \times \text{LEP}$	$3.0 \times \text{Belle II}$
FCC-ee	$6 \cdot 10^6$	$200 \cdot 10^3$	$2.4 \cdot 10^5 \times \text{LEP}$	$4.5 \times \text{Belle II}$

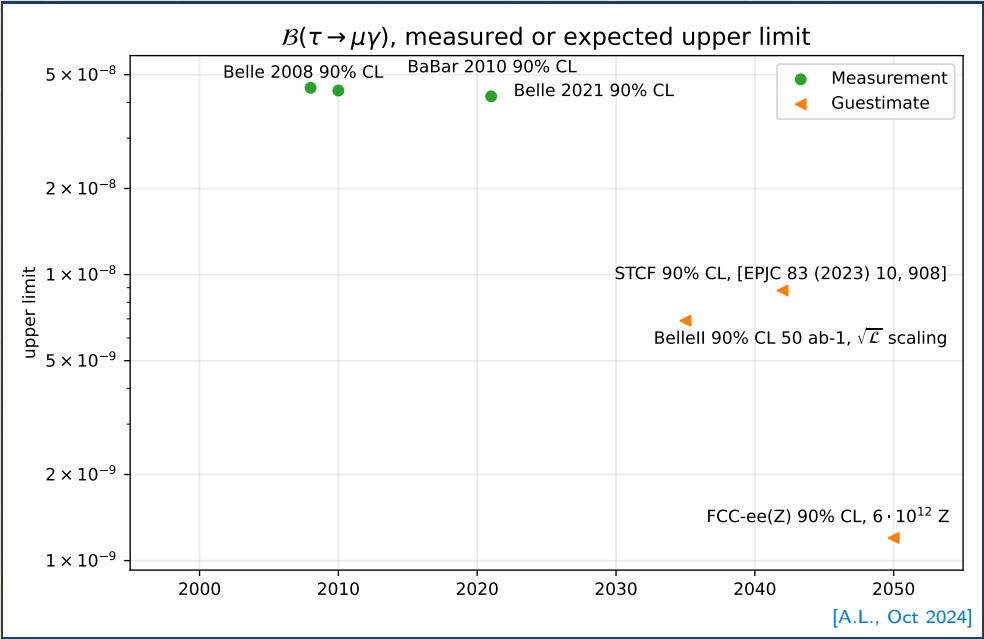
experimental conditions of tau pairs much better at Z peak compared to lower energies

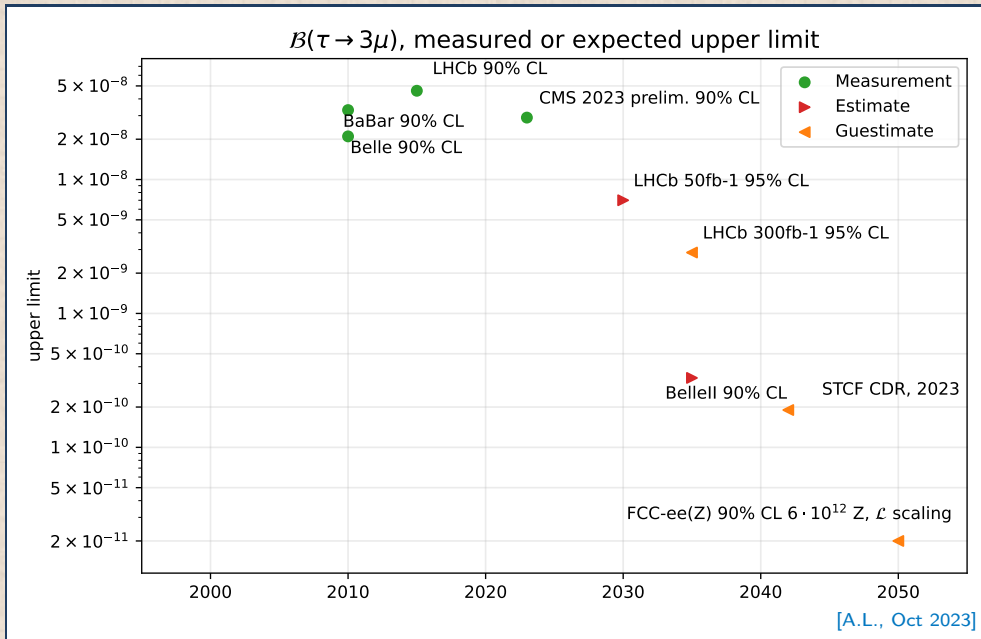
- ▶ better momentum resolution and vertexing because less multiple scattering with higher track momenta
- ▶ better higher momentum muon id (much lower pion-to-muon misidentification)
- ▶ much better $\tau^+\tau^-$ separation from $q\bar{q}$ background because of higher $q\bar{q}$ multiplicity at Z peak
- ▶ LHC produces more tau leptons, but with much less favourable experimental conditions

Tau LFV decay upper limits, Belle II expected



LFV search for $\tau \rightarrow \mu\gamma$



LFV search for $\tau \rightarrow 3\mu$ 

Experimental LFV searches with tau in final state

$B^0 \rightarrow \mu^\pm e^\mp$	1.0×10^{-9}	90%	LHCb
$B_s^0 \rightarrow \mu^\pm e^\mp$	5.4×10^{-9}	90%	LHCb
$B^0 \rightarrow K^{*0} \mu^+ e^-$	5.7×10^{-9}	90%	LHCb
$B^0 \rightarrow K^{*0} \mu^- e^+$	6.8×10^{-9}	90%	LHCb
$B_s^0 \rightarrow \phi \mu^\pm e^\mp$	1.6×10^{-8}	90%	LHCb
$B^+ \rightarrow K^+ \mu^+ e^-$	6.4×10^{-9}	90%	LHCb
$B^+ \rightarrow K^+ \mu^- e^+$	7.0×10^{-9}	90%	LHCb
$B^0 \rightarrow \tau^\pm \mu^\mp$	1.5×10^{-5}	90%	LHCb
$B_s^0 \rightarrow \tau^\pm \mu^\mp$	4.2×10^{-5}	90%	LHCb
$B^0 \rightarrow \tau^\pm e^\mp$	1.6×10^{-5}	90%	Belle
$B^0 \rightarrow K^{*0} \tau^+ \mu^-$	1.0×10^{-5}	90%	LHCb
$B^0 \rightarrow K^{*0} \tau^- \mu^+$	8.2×10^{-6}	90%	LHCb
$D^0 \rightarrow \mu^\pm e^\mp$	1.3×10^{-8}	90%	LHCb
$D^+ \rightarrow \pi^+ \mu^+ e^-$	2.2×10^{-7}	90%	LHCb
$D^+ \rightarrow \pi^+ \mu^- e^+$	2.1×10^{-7}	90%	LHCb
$D^+ \rightarrow K^+ \mu^+ e^-$	1.0×10^{-7}	90%	LHCb
$D^+ \rightarrow K^+ \mu^- e^+$	7.5×10^{-8}	90%	LHCb

$K_L^0 \rightarrow \mu^\pm e^\mp$	4.7×10^{-12}	90%	BNL
$K_L^0 \rightarrow e^\pm e^\pm \mu^\mp \mu^\mp$	4.12×10^{-11}	90%	KTeV
$K_L^0 \rightarrow \pi^0 \mu^\pm e^\mp$	7.56×10^{-11}	90%	KTeV
$K_L^0 \rightarrow \pi^0 \pi^0 \mu^\pm e^\mp$	1.64×10^{-10}	90%	KTeV
$K^+ \rightarrow \mu^- \nu e^+ e^+$	8.1×10^{-11}	90%	NA62
$Z \rightarrow e^\pm \mu^\mp$	7.5×10^{-7}	95%	ATLAS
$Z \rightarrow e^\pm \tau^\mp$	5.0×10^{-6}	95%	ATLAS
$Z \rightarrow \mu^\pm \tau^\mp$	6.5×10^{-6}	95%	ATLAS
$H \rightarrow e^\pm \mu^\mp$	6.2×10^{-5}	95%	ATLAS
$H \rightarrow e^\pm \tau^\mp$	2.0×10^{-3}	95%	ATLAS
$H \rightarrow \mu^\pm \tau^\mp$	1.5×10^{-3}	95%	CMS

Lepton flavour universality

Experimental tests of lepton flavour universality

2013 [A.Pich, Precision Tau Physics (2014)]

$ g_\mu/g_e $	$\Gamma_{\tau \rightarrow \mu}/\Gamma_{\tau \rightarrow e}$ 1.0018(14)	$\Gamma_{\pi \rightarrow \mu}/\Gamma_{\pi \rightarrow e}$ 1.0021(16)	$\Gamma_{K \rightarrow \mu}/\Gamma_{K \rightarrow e}$ 0.9978(20)	$\Gamma_{K \rightarrow \pi\mu}/\Gamma_{K\tau \rightarrow \pi e}$ 1.0010(25)	$\Gamma_{W \rightarrow \mu}/\Gamma_{W \rightarrow e}$ 0.996(10)
$ g_\tau/g_\mu $	$\Gamma_{\tau \rightarrow e}/\Gamma_{\mu \rightarrow e}$ 1.0011(15)	$\Gamma_{\tau \rightarrow \pi}/\Gamma_{\pi \rightarrow \mu}$ 0.9962(27)	$\Gamma_{\tau \rightarrow K}/\Gamma_{K \rightarrow \mu}$ 0.9858(70)	$\Gamma_{W \rightarrow \tau}/\Gamma_{W \rightarrow \mu}$ 1.034(13)	
$ g_\tau/g_e $	$\Gamma_{\tau \rightarrow \mu}/\Gamma_{\mu \rightarrow e}$ 1.0030(15)				$\Gamma_{W \rightarrow \tau}/\Gamma_{W \rightarrow e}$ 1.031(13)

2024 [V.Cirigliano *et al.*, 2022] [HFLAV report 2023, in preparation] [PDG 2024]

$ g_\mu/g_e $	$\Gamma_{\tau \rightarrow \mu}/\Gamma_{\tau \rightarrow e}$ 1.002(11)	$\Gamma_{\pi \rightarrow \mu}/\Gamma_{\pi \rightarrow e}$ 1.0010(9)	$\Gamma_{K \rightarrow \mu}/\Gamma_{K \rightarrow e}$ 0.9978(18)	$\Gamma_{K \rightarrow \pi\mu}/\Gamma_{K\tau \rightarrow \pi e}$ 1.0009(18)	$\Gamma_{W \rightarrow \mu}/\Gamma_{W \rightarrow e}$ 1.001(3)
$ g_\tau/g_\mu $	$\Gamma_{\tau \rightarrow e}/\Gamma_{\mu \rightarrow e}$ 1.0016(14)	$\Gamma_{\tau \rightarrow \pi}/\Gamma_{\pi \rightarrow \mu}$ 0.9958(38)	$\Gamma_{\tau \rightarrow K}/\Gamma_{K \rightarrow \mu}$ 0.9856(75)	$\Gamma_{W \rightarrow \tau}/\Gamma_{W \rightarrow \mu}$ 1.007(10)	
$ g_\tau/g_e $	$\Gamma_{\tau \rightarrow \mu}/\Gamma_{\mu \rightarrow e}$ 1.0018(14)				$\Gamma_{W \rightarrow \tau}/\Gamma_{W \rightarrow e}$ 1.008(10)

Lepton universality tests

today status [HFLAV 2023 report, preliminary]

$$\left(\frac{g_\tau}{g_\mu}\right) = \sqrt{\frac{\mathcal{B}_{\tau e} \tau_\mu m_\mu^5 f_{\mu e} R_\gamma^\mu R_W^{\mu e}}{\mathcal{B}_{\mu e} \tau_\tau m_\tau^5 f_{\tau e} R_\gamma^\tau R_W^{\tau e}}} = 1.0016 \pm 0.0014 = \sqrt{\frac{\mathcal{B}_{\tau e}}{\mathcal{B}_{\tau e}^{\text{SM}}}}$$

$$\left(\frac{g_\tau}{g_e}\right) = \sqrt{\frac{\mathcal{B}_{\tau\mu} \tau_\mu m_\mu^5 f_{\mu e} R_\gamma^\mu R_W^{\mu e}}{\mathcal{B}_{\mu e} \tau_\tau m_\tau^5 f_{\tau\mu} R_\gamma^\tau R_W^{\tau\mu}}} = 1.0018 \pm 0.0014 = \sqrt{\frac{\mathcal{B}_{\tau\mu}}{\mathcal{B}_{\tau\mu}^{\text{SM}}}}$$

$$\left(\frac{g_\mu}{g_e}\right) = \sqrt{\frac{\mathcal{B}_{\tau\mu} f_{\tau e}}{\mathcal{B}_{\tau e} f_{\tau\mu}}} = 1.0002 \pm 0.0011$$

using Standard Model predictions for leptons \mathcal{L} , $\ell = e, \mu, \tau$ (Marciano, 1988):

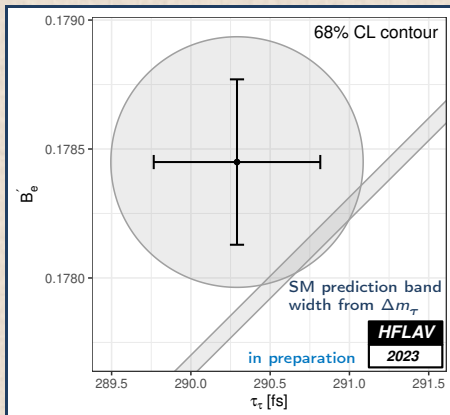
$$\Gamma[\mathcal{L} \rightarrow \nu_{\mathcal{L}} \ell \bar{\nu}_\ell(\gamma)] = \Gamma_{\mathcal{L}\ell} = \Gamma_{\mathcal{L}} \mathcal{B}_{\mathcal{L}\ell} = \frac{\mathcal{B}_{\mathcal{L}\ell}}{\tau_{\mathcal{L}}} = \frac{G_{\mathcal{L}} G_\ell m_{\mathcal{L}}^5}{192\pi^3} f(m_\ell^2/m_{\mathcal{L}}^2) R_W^{\mathcal{L}} R_\gamma^{\mathcal{L}}$$

$$G_{\mathcal{L}} = \frac{g_{\mathcal{L}}^2}{4\sqrt{2}M_W^2}; \quad f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln x; \quad f_{\mathcal{L}\ell} = f(m_\ell^2/m_{\mathcal{L}}^2)$$

$$R_W^{\mathcal{L}\ell} = 1 + \frac{3}{5} \frac{m_{\mathcal{L}}^2}{M_W^2} + \frac{9}{5} \frac{m_\ell^2}{M_W^2}; \quad R_\gamma^{\mathcal{L}} = 1 + \frac{\alpha(m_{\mathcal{L}})}{2\pi} \left(\frac{25}{4} - \pi^2\right); \quad \text{all statistical correlations included}$$

- ▶ less precise tests possible with hadronic tau decays
- ▶ tau BF, mass, lifetime from HFLAV tau averages in preparation

Canonical tau lepton universality test plot



[HFLAV 2023 prelim.]

$$(g_\tau/g_{e\mu}) = 1.0017 \pm 0.0013$$

$$[g_{e\mu} = g_e = g_\mu \text{ assuming } g_e = g_\mu]$$

$\Delta(g_\tau/g_{e\mu})$ contributions

input	Δ input	$\Delta(g_\tau/g_{e\mu})$
$\mathcal{B}'_{\tau \rightarrow e}$	0.180%	0.090%
τ_τ	0.181%	0.090%
m_τ	0.005%	0.012%
total		0.128%

best measurements

$\mathcal{B}'_{\tau \rightarrow e}$	ALEPH
τ_τ	Belle
m_τ	Belle II

- ▶ $\mathcal{B}'(\tau \rightarrow e\bar{\nu}\nu) = \text{average of } \begin{cases} \mathcal{B}(\tau \rightarrow e\bar{\nu}\nu) \\ \mathcal{B}(\tau \rightarrow \mu\bar{\nu}\nu) \cdot \frac{f_{\tau e} R_W^{\tau e}}{f_{\tau \mu} R_W^{\tau \mu}} \end{cases}$
- ▶ $\frac{\mathcal{B}'(\tau \rightarrow e\bar{\nu}\nu)\tau_\mu}{\mathcal{B}(\mu \rightarrow e\bar{\nu}\nu)\tau_\tau} = \frac{g_\tau^2}{g_{e\mu}^2} \frac{m_\tau^5 f_{\tau e} R_\gamma^{\tau e} R_W^{\tau e}}{m_\mu^5 f_{\mu e} R_\gamma^{\mu e} R_W^{\mu e}}$
- ▶ $\left(\frac{g_\tau}{g_{e\mu}}\right)^2 = \frac{\mathcal{B}'(\tau \rightarrow e\bar{\nu}\nu)}{\mathcal{B}(\mu \rightarrow e\bar{\nu}\nu)} \frac{\tau_\mu}{\tau_\tau} \frac{m_\mu^5}{m_\tau^5} \frac{f_{\mu e} R_\gamma^{\mu e} R_W^{\mu e}}{f_{\tau e} R_\gamma^{\tau e} R_W^{\tau e}}$

Tau - muon universality using tau hadronic branching fractions

$$\left(\frac{g_\tau}{g_\mu}\right)_h^2 = \frac{\mathcal{B}(\tau \rightarrow h\nu_\tau)}{\mathcal{B}(h \rightarrow \mu\bar{\nu}_\mu)} \frac{2m_h m_\mu^2 \tau_h}{(1 + \delta R_{\tau/h}) m_\tau^3 \tau_\tau} \left(\frac{1 - m_\mu^2/m_h^2}{1 - m_h^2/m_\tau^2}\right)^2,$$

- ▶ $h = \pi$ or K
- ▶ $\delta R_{\tau/\pi} = (0.18 \pm 0.57)\%$ [PhysRevD.104.L091502 (2021)]
- ▶ $\delta R_{\tau/K} = (0.97 \pm 0.58)\%$ [PhysRevD.104.L091502 (2021)]
- ▶ tau BF from HFLAV tau averages in preparation

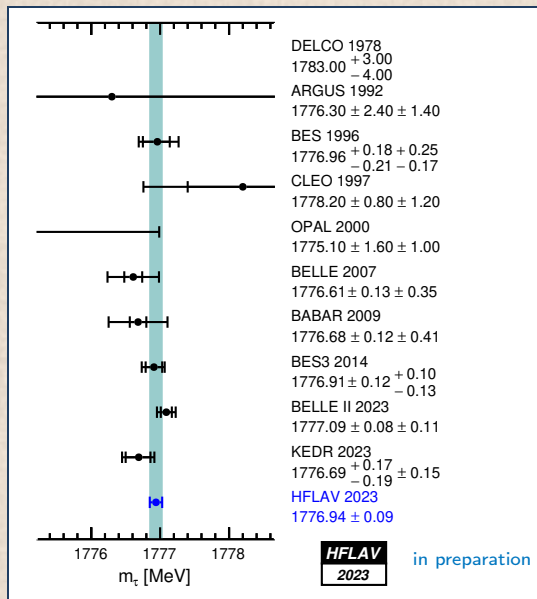
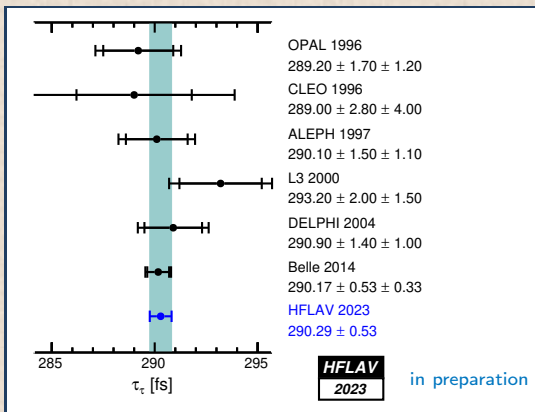
$$\left(\frac{g_\tau}{g_\mu}\right)_\pi = 0.996 \pm 0.004, \quad \left(\frac{g_\tau}{g_\mu}\right)_K = 0.986 \pm 0.008.$$

- ▶ $\mathcal{B}(\pi \rightarrow \mu\bar{\nu}_\mu), \mathcal{B}(K \rightarrow \mu\bar{\nu}_\mu)$ PDG 2023

$$\left(\frac{g_\tau}{g_\mu}\right)_{\tau+\pi+K} = 1.0011 \pm 0.0014, \tag{1}$$

- ▶ average of three tau vs. mu universality tests
- ▶ assuming uncorrelated $\delta R_{\tau/\pi}$ and $\delta R_{\tau/K}$

Tau mass and lifetime measurements



Tau branching fractions measurements

$$\mathcal{B}_3 = \mathcal{B}(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)$$

0.17360 ± 0.00037	average
$0.17319 \pm 0.00070 \pm 0.00032$	ALEPH
$0.17325 \pm 0.00095 \pm 0.00077$	DELPHI
$0.17342 \pm 0.00110 \pm 0.00067$	L3
$0.17340 \pm 0.00090 \pm 0.00060$	OPAL

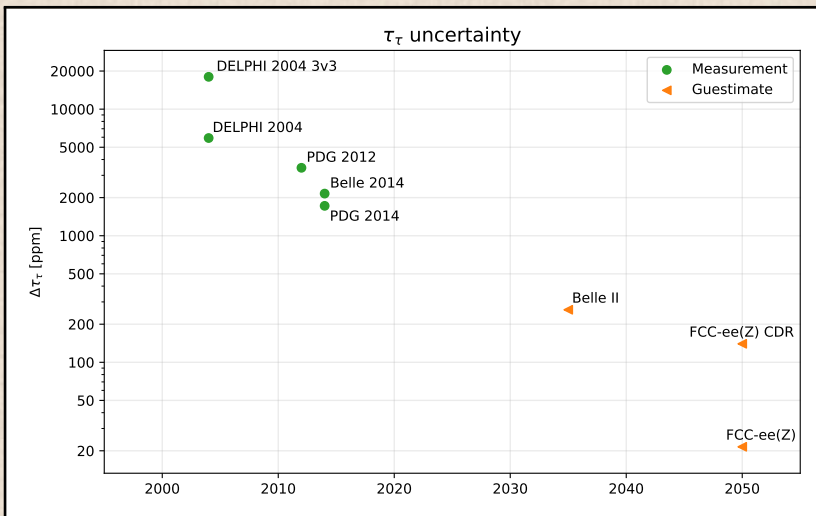
$$\mathcal{B}_5 = \mathcal{B}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)$$

0.1784 ± 0.0004	average
$0.1784 \pm 0.0007 \pm 0.0004$	ALEPH
$0.1776 \pm 0.0006 \pm 0.0017$	CLEO
$0.1788 \pm 0.0011 \pm 0.0011$	DELPHI
$0.1781 \pm 0.0010 \pm 0.0008$	L3
$0.1781 \pm 0.0009 \pm 0.0006$	OPAL

$$\mathcal{B}_{3/5} = \frac{\mathcal{B}(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{\mathcal{B}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$$

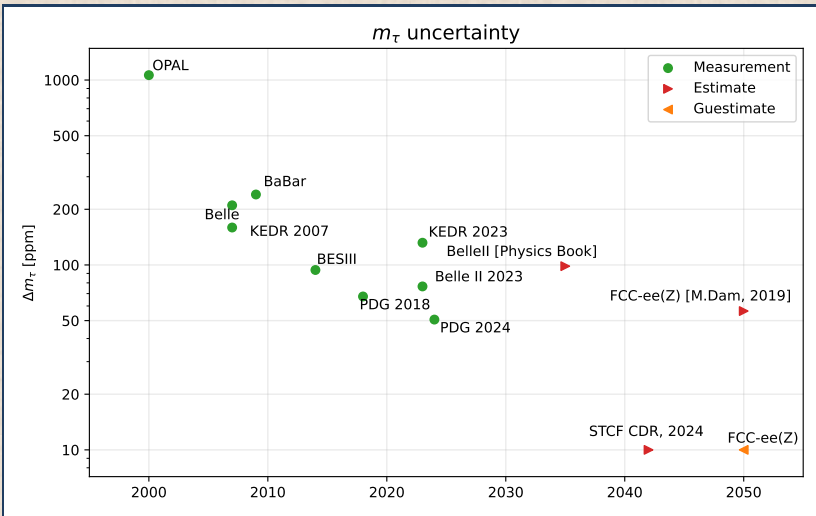
0.9730 ± 0.0022	average
$0.9970 \pm 0.0350 \pm 0.0400$	ARGUS
$0.9796 \pm 0.0016 \pm 0.0036$	BABAR
$0.9675 \pm 0.0007 \pm 0.0036$	Belle II
$0.9777 \pm 0.0063 \pm 0.0087$	CLEO

Tau Lifetime measurement prospects



FCC-ee(Z) with $6 \cdot 10^{12}$ Z

Tau mass measurement prospects



FCC-ee(Z) with $6 \cdot 10^{12}$ Z

Tau leptonic branching fractions measurement prospects

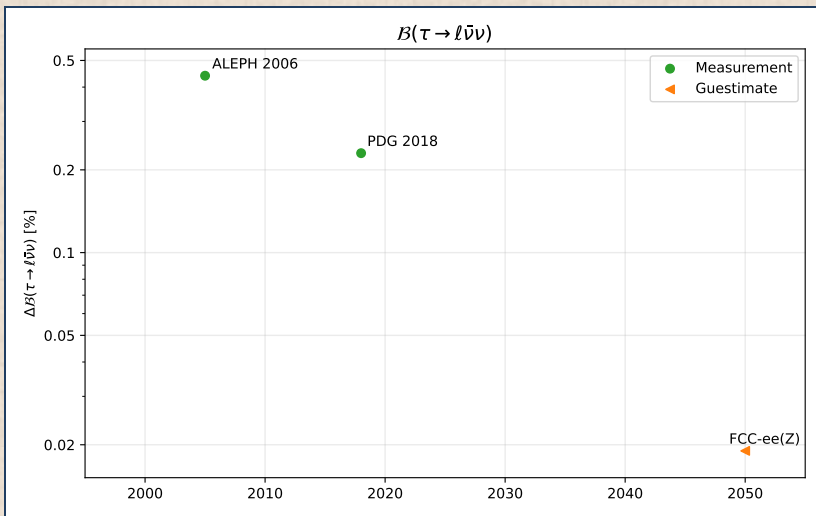
- ▶ ALEPH 2006 measurement precision: $4400 \text{ ppm} = [4000(\text{stat.}) \oplus 1900(\text{syst.})] \text{ ppm}$
(average of the two similar electron and muon decays branching fractions)
 - ▶ complex simultaneous measurement of 12 tau branching fractions
 - ▶ many systematic uncertainties, no reliable extrapolations to FCC-ee statistics
 - ▶ several systematics related to photon and $\pi^0 \rightarrow \gamma\gamma$ reconstruction

- ▶ $\Delta_{\text{stat}}^{\text{FCC}} \mathcal{B}(\tau \rightarrow \ell \bar{\nu} \nu) = 4000 \text{ ppm} \cdot \sqrt{\frac{6.2 \cdot 10^6 \text{ (ALEPH Z bosons)}}{6 \cdot 10^{12}}} = 4.1 \text{ ppm (FCC Z bosons)}$

- ▶ $\Delta_{\text{syst}}^{\text{FCC}} \mathcal{B}(\tau \rightarrow \ell \bar{\nu} \nu) = \frac{1}{10} \cdot 1900 \text{ ppm} = 190 \text{ ppm}$
[assume also 100% correlated between $\mathcal{B}(\tau \rightarrow e \bar{\nu} \nu)$ and $\mathcal{B}(\tau \rightarrow \mu \bar{\nu} \nu)$]

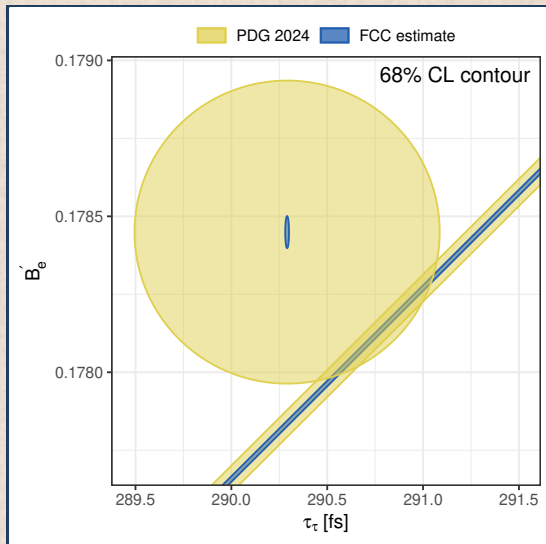
- ▶ $\Delta^{\text{FCC}} \mathcal{B}(\tau \rightarrow \ell \bar{\nu} \nu) \simeq 190 \text{ ppm}$

Tau leptonic Branching fractions prospects at FCC-ee and other facilities



- ▶ FCC-ee(Z) with $6 \cdot 10^{12}$ Z
- ▶ Belle II is working on these measurements

Canonical tau lepton universality plot extrapolation at FCC-ee



FCC-ee(Z) with $6 \cdot 10^{12}$ Z

μ/e universality from $\mathcal{B}(\pi \rightarrow e\nu(\gamma))/\mathcal{B}(\pi \rightarrow \mu\nu(\gamma))$

- ▶ $R_{e/\mu}^\pi, \text{SM} = 1.23524(15) \cdot 10^{-4}$
- ▶ $R_{e/\mu}^\pi, \text{PIENU}(2015) = 1.2344(23)\text{stat}(19)\text{syst} \cdot 10^{-4}$ PRL 115 (2015) 071801
- ▶ $R_{e/\mu}^\pi, \text{EXP} = 1.2327(23) \cdot 10^{-4}$ PDG 2024
- ▶ on-going PEN experiment at PSI also aims to measure $R_{e/\mu}^\pi$
- ▶ future: PIONEER (PSI) uncertainty goal equal to SM prediction precision

Summary

- ▶ status and prospects of lepton flavour violation searches
- ▶ status and prospects of lepton flavour universality tests

End

Backup slides

Searches for muon conversion in nuclei, $\mu N \rightarrow e N$

- ▶ DeeMe, C target, 1 year (JPARC, Japan), $SES \sim 1 \cdot 10^{-13}$
- ▶ DeeMe, SiC target, 4 years (JPARC, Japan), $SES \sim 5 \cdot 10^{-15}$
- ▶ Mu2e (FNAL, USA), $SES \sim 3 \cdot 10^{-17}$
- ▶ COMET-1 (JPARC, Japan), $SES \sim 3 \cdot 10^{-15}$
- ▶ COMET-2 (JPARC, Japan), $SES \sim 3 \cdot 10^{-17}$
- ▶ PRISM/PRIME (JPARC, Japan), $SES \sim 1 \cdot 10^{-18}$