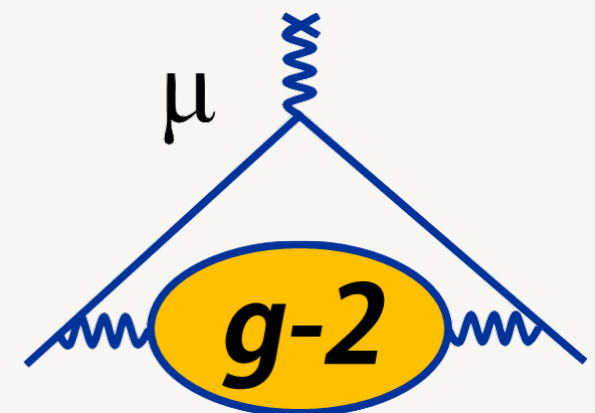


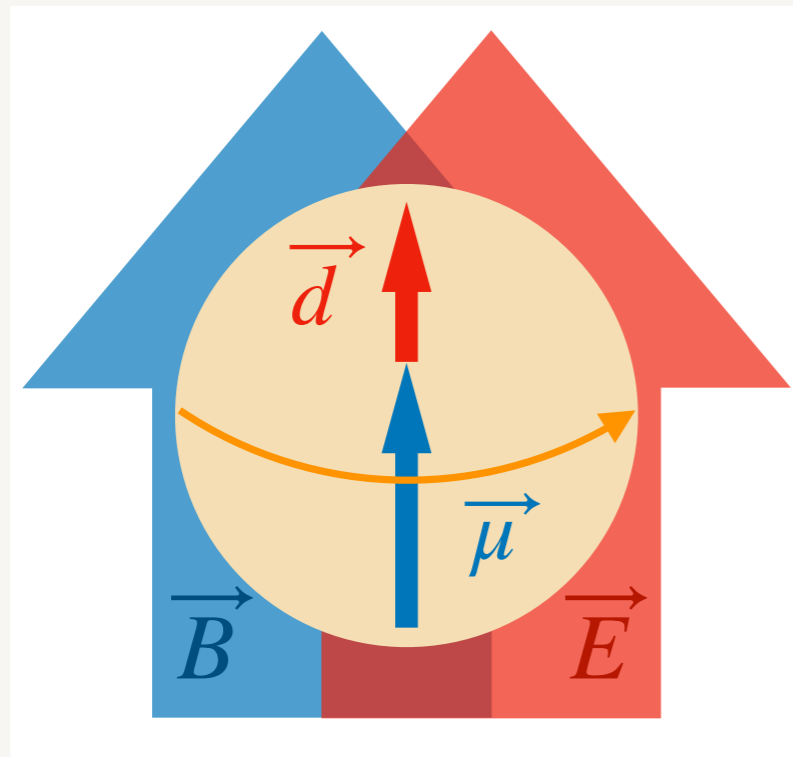
Status of muon EDM measurement at the Muon $g-2$ experiment in Fermilab

Mikio Sakurai

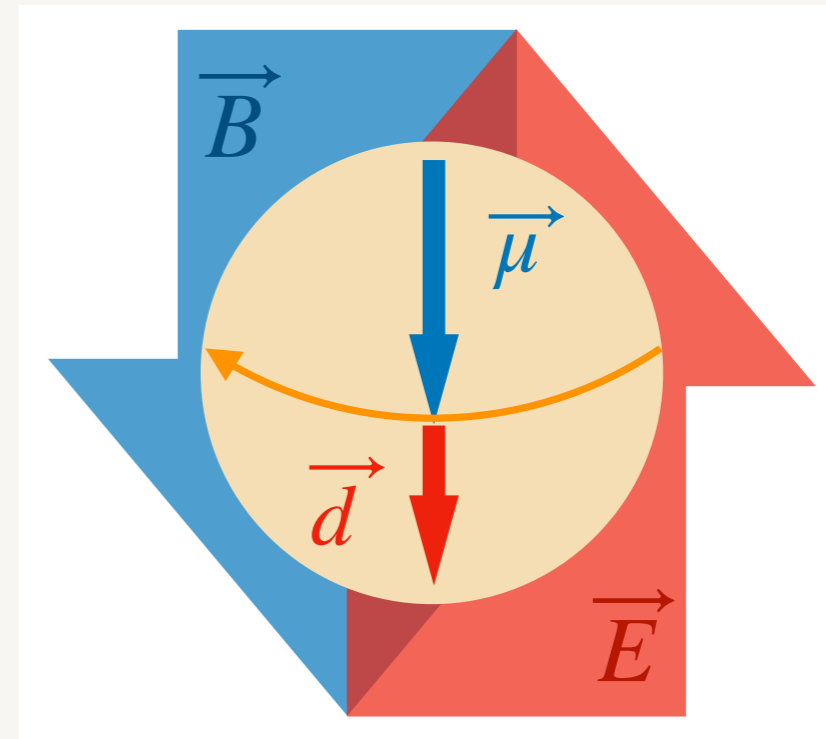
on behalf of the EDM group
Muon $g-2$ collaboration

m.sakurai@ucl.ac.uk





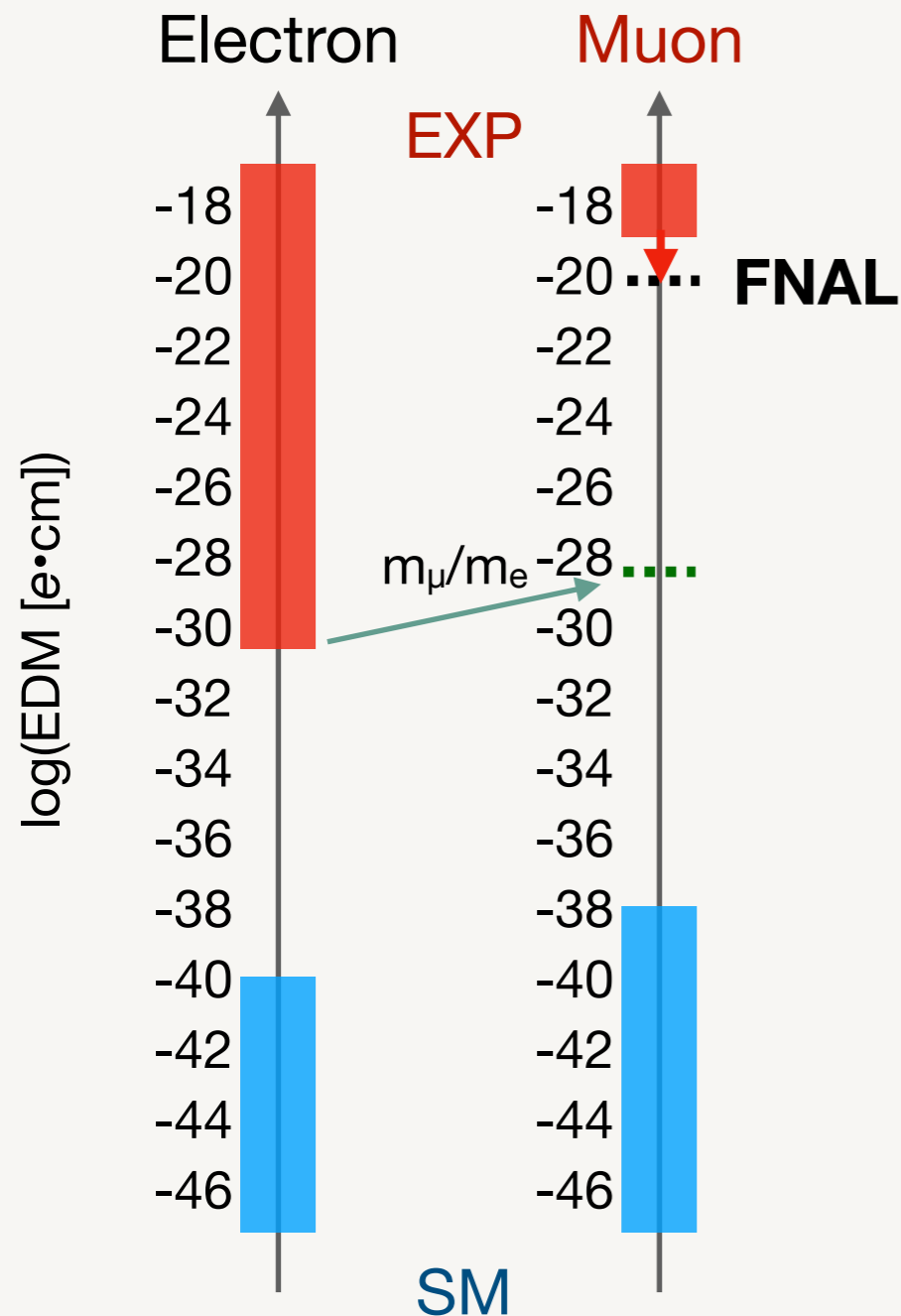
$T \rightarrow$



$$\mathcal{H} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

$$\mathcal{H}^T = -\vec{\mu} \cdot \vec{B} + \vec{d} \cdot \vec{E}$$

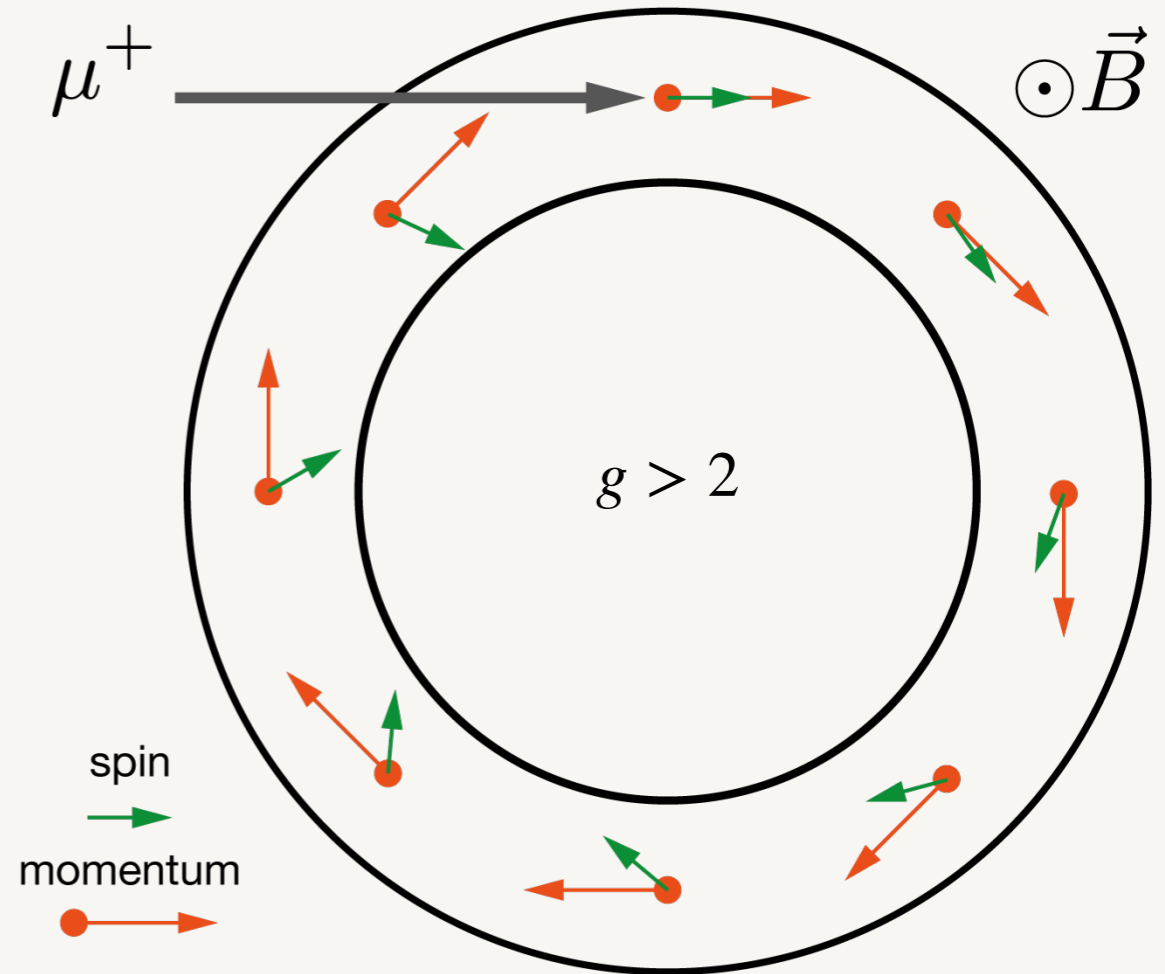
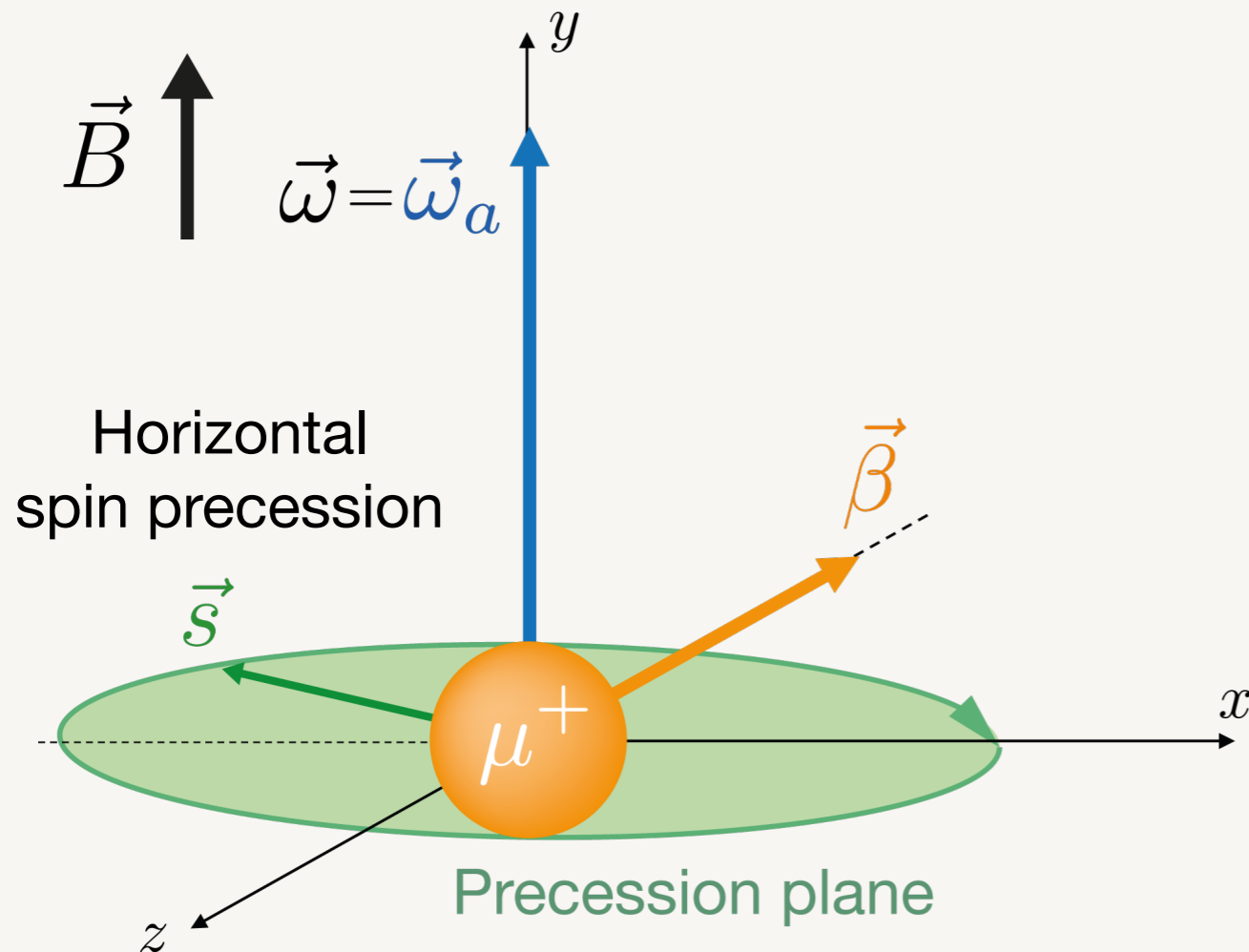
- If $\vec{d} = 0$, $H = H^T$
- If $\vec{d} \neq 0$, $H \neq H^T \rightarrow T$ violation \Rightarrow CP violation assuming CPT invariance



- Muon EDM has been measured in conjunction with muon g-2 over the past decades
- The current best direct limit was set at BNL:
 $d_\mu < 1.8 \times 10^{-19} e \cdot \text{cm}$ (95% C. L.)
G. W. Bennett et al., PRD 80, 052008 (2009)
- Indirect limits
 - Electron (m_μ/m_e): $d_\mu < 8.5 \times 10^{-28} e \cdot \text{cm}$
electron EDM: T. S. Roussy et al., Science 381,46-50 (2023)
 - ^{199}Hg : $d_\mu < 6 \times 10^{-20} e \cdot \text{cm}$
Y. Ema et al., PRL 128, 131803 (2023)
- Key opportunity to further push EDM searches together with other experimental efforts (e, p, n...)
- Probing the role of lepton flavour universality

SM: M. Pospelov et al., PRD 89, 056006 (2014)
 Y. Yamaguchi et al., PRL 125, 241802 (2020)

Muon spin precession in a storage ring

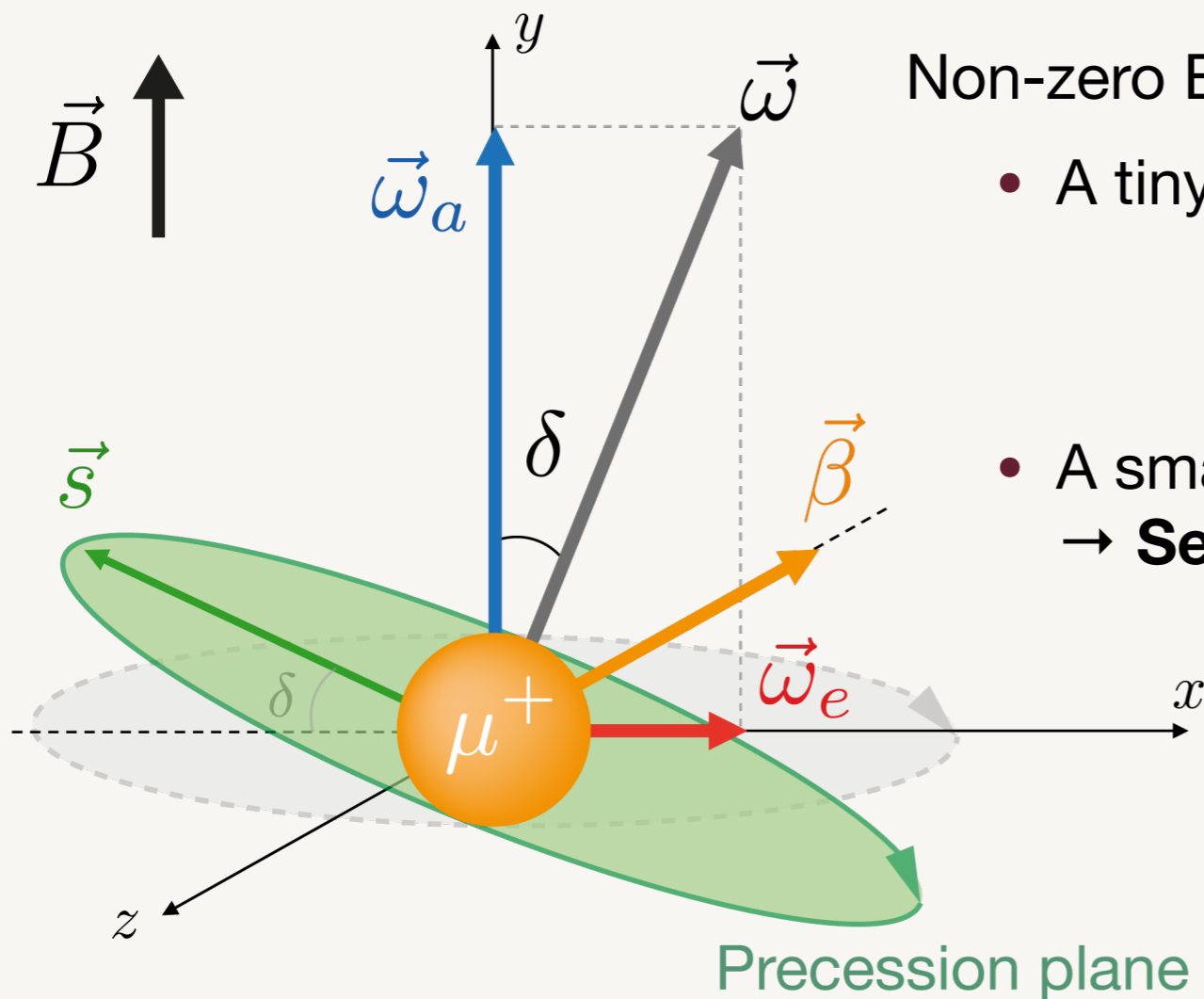


0 for $\gamma = 29.3$ ($p = 3.09$ GeV/c)

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] - \frac{e}{m} \left[\frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

$\vec{\omega}_a$: horizontal precession

Addition of a non-zero EDM



Non-zero EDM introduces

- A tiny increase in the precession frequency

$$\omega = \sqrt{\omega_a^2 + \omega_e^2}$$

- A small tilt to the spin precession plane
→ **Search for an EDM by looking for this tilt**

0 for $\gamma = 29.3$ ($p = 3.09$ GeV/c)

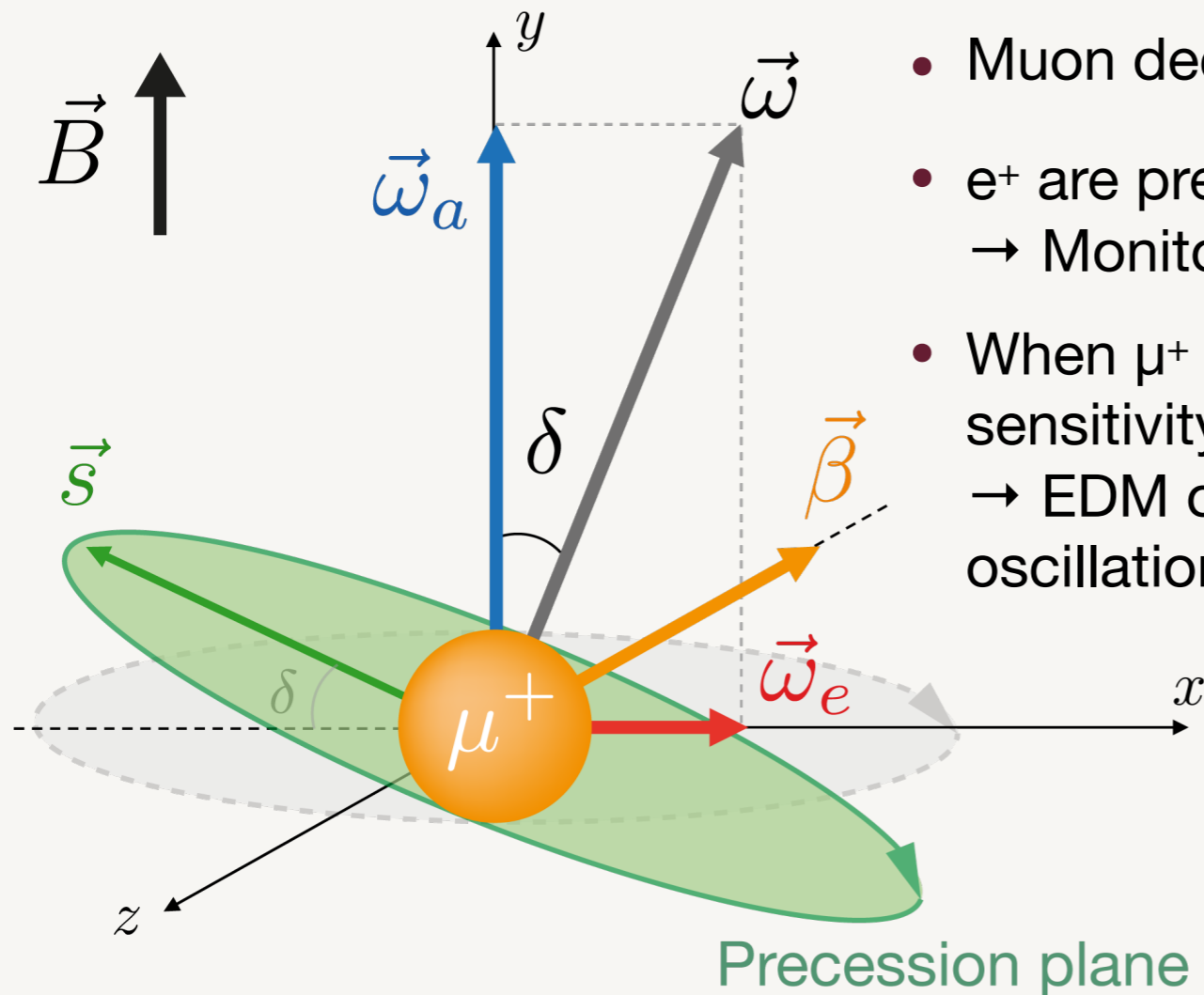
$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] - \frac{e}{m} \left[\frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

$$d_\mu = \eta \frac{e\hbar}{4mc} \neq 0$$

$\vec{\omega}_a$: horizontal precession

$\vec{\omega}_e$: vertical precession

Measuring the muon EDM



- Muon decay: $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$
- e^+ are preferentially emitted in μ^+ spin direction
→ Monitor μ^+ spin precession by detecting e^+
- When μ^+ spin aligns with its momentum vector, no sensitivity to EDM and maximal sensitivity to EDM at $\pi/2$
→ EDM oscillation is $\pi/2$ out of phase with the $g-2$ oscillation

0 for $\gamma = 29.3$ ($p = 3.09$ GeV/c)

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] - \frac{e}{m} \left[\frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

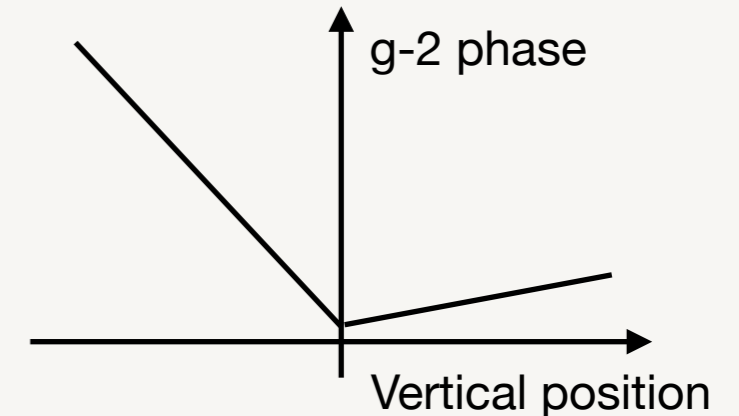
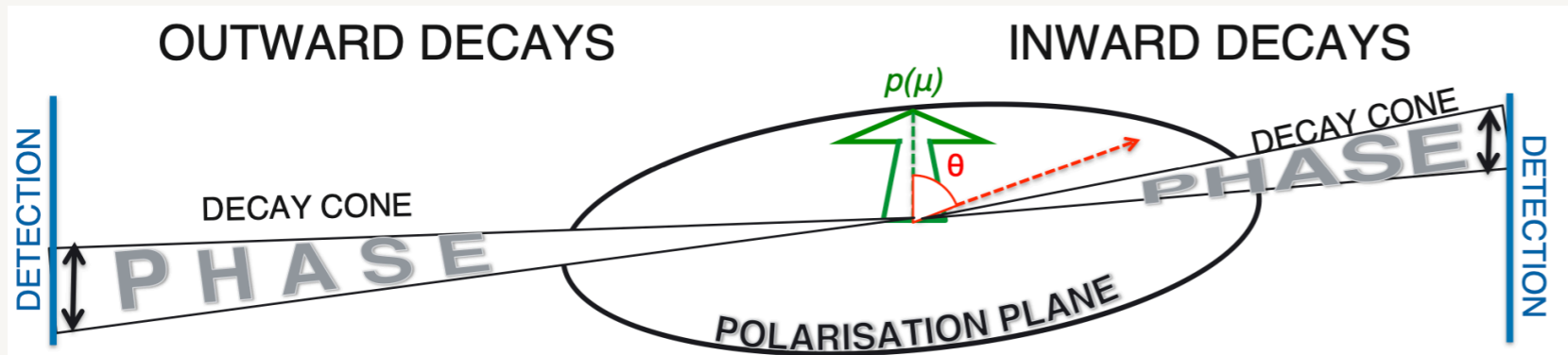
$\vec{\omega}_a$: horizontal precession

$\vec{\omega}_e$: vertical precession

$$d_\mu = \eta \frac{e\hbar}{4mc} \neq 0$$

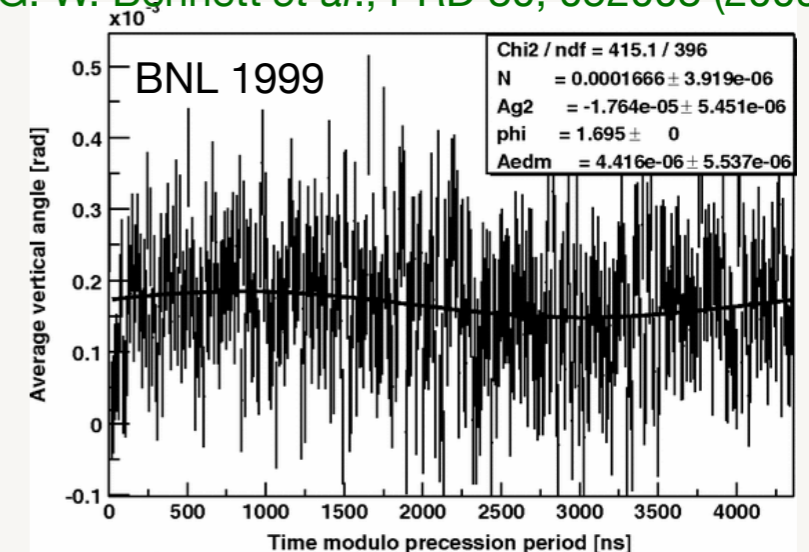
Measuring the muon EDM at FNAL

- Phase asymmetry

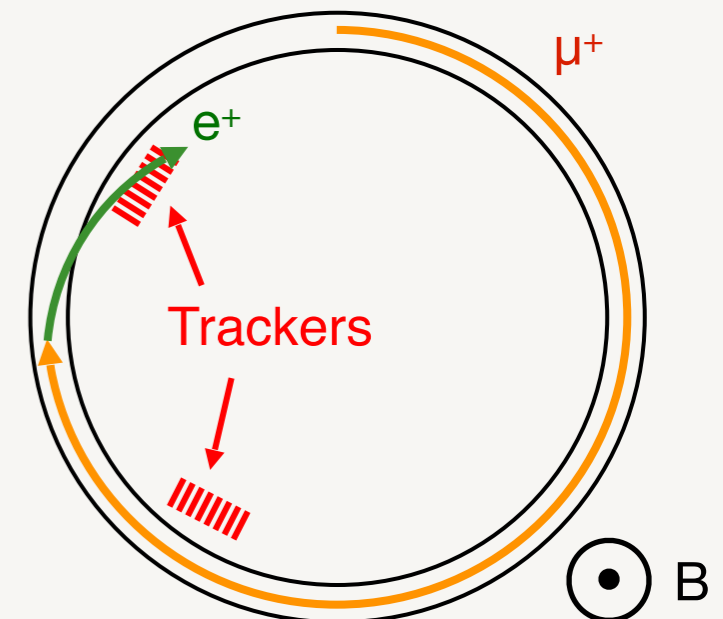
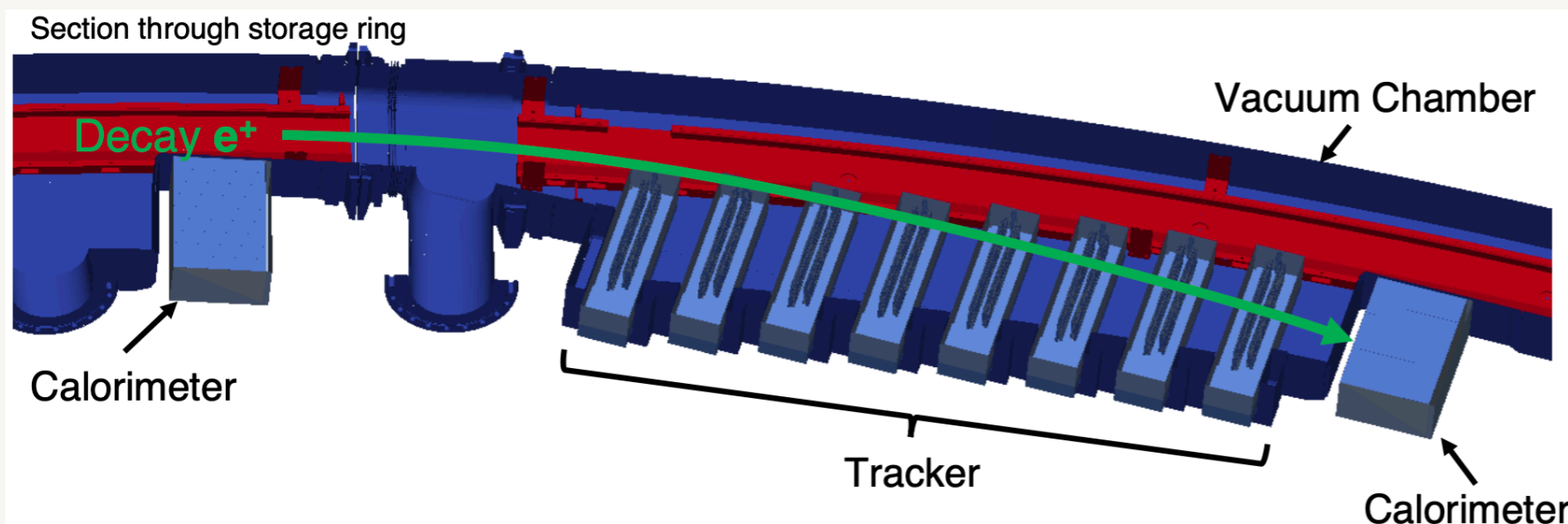


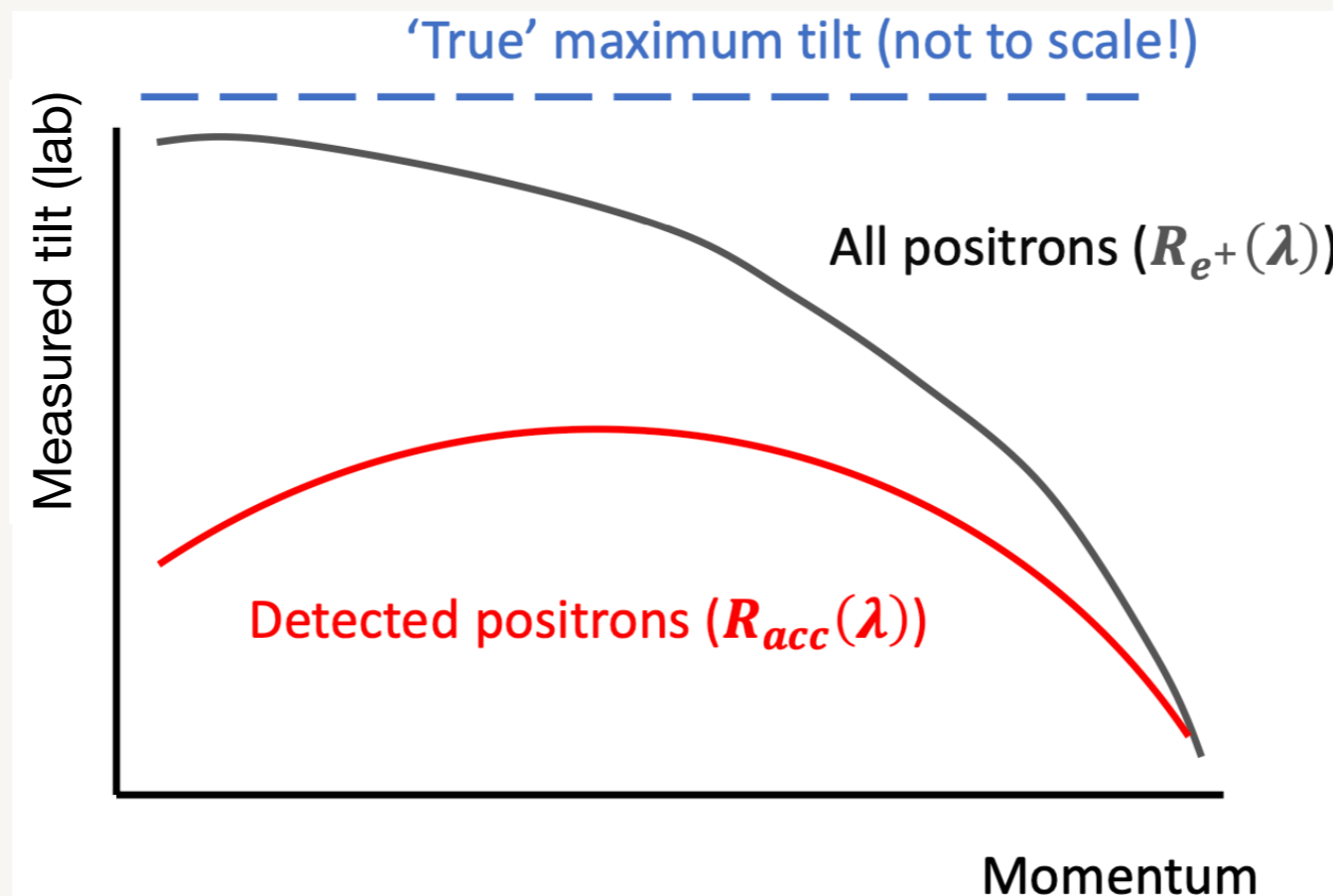
- Look for a phase asymmetry in vertical position caused by inward/outward decay positrons
- Calorimeter-based approach used at BNL → systematically limited
- Vertical decay angle
 - Direct measurement of positron decay angle by tracker
 - Statistically limited at BNL
- @FNAL: stats improved but calorimeter-based approach is still systematically limited
- FNAL muon EDM search focuses on the **tracker-based approach, measuring vertical decay angle**

G. W. Bennett *et al.*, PRD 80, 052008 (2009)



- 2 straw tracker stations (12 and 18) around the ring
 - 8 Argon-Ethane straw module per station with hit resolution $\sim 100 \mu\text{m}$
 - Operation inside the vacuum chamber
- Hits are fitted into tracks, which are then extrapolated backwards to the decay vertex
 - Used for the EDM analysis to measure the vertical decay angle



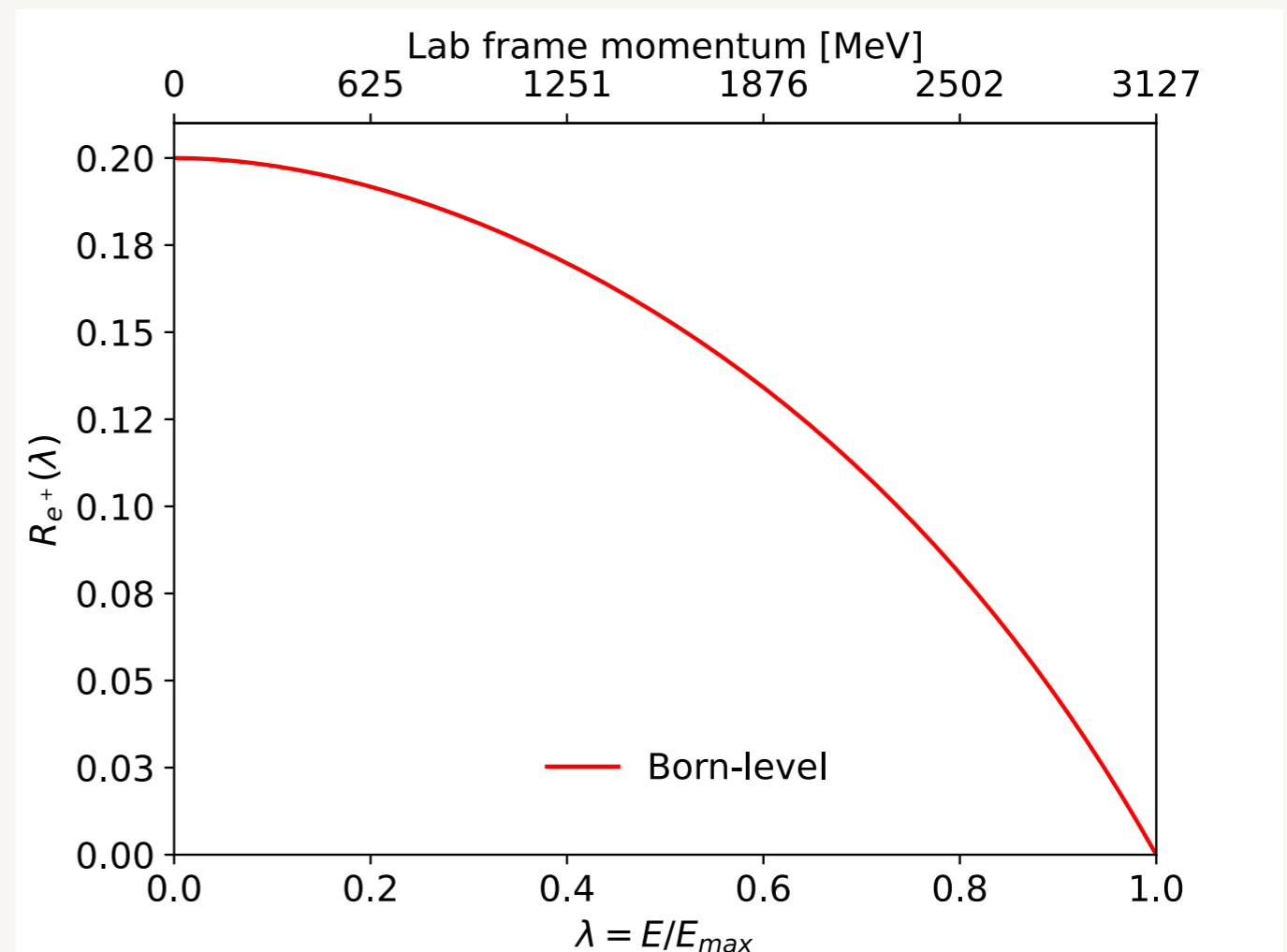
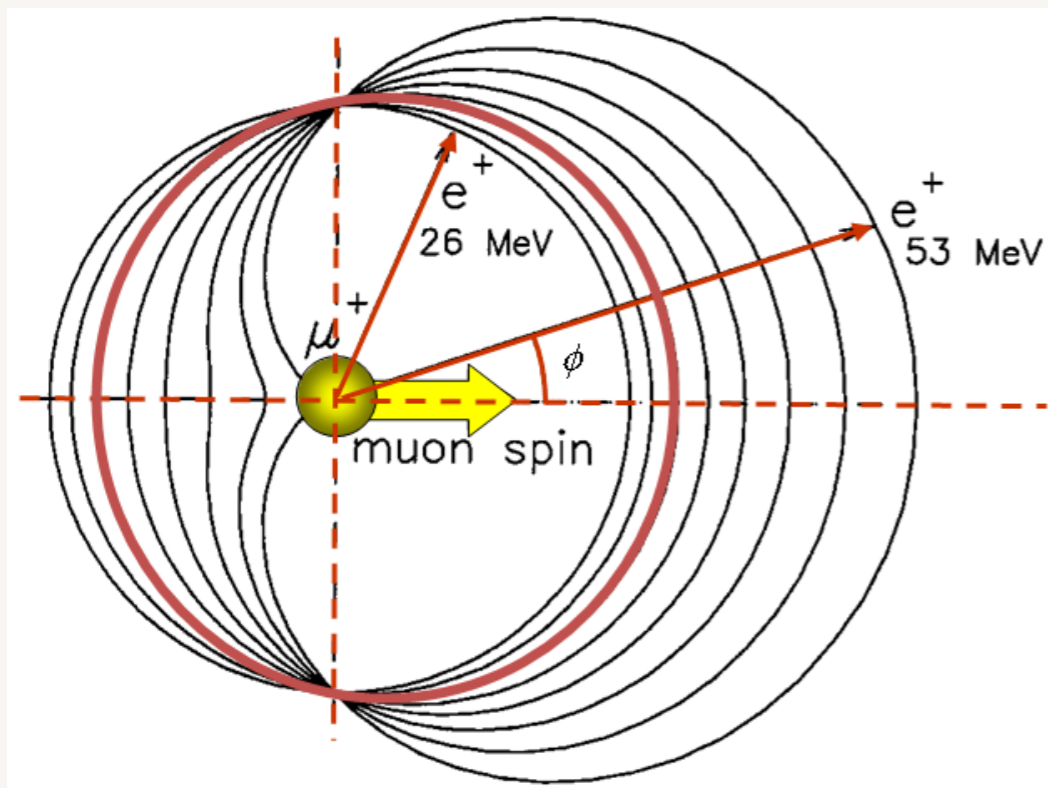


- Measured tilt in trackers is reduced from the rest frame tilt via

$$\text{Measured tilt (lab)} = R_\gamma R_P R_{e^+}(\lambda) R_{acc}(\lambda) \text{ True tilt (rest)}$$
 - R_γ : Lorentz boost $1/\gamma \sim 1/29$
 - R_P : average beam polarisation ~ 0.96
 - $R_{e^+}(\lambda)$: momentum-dependent asymmetry in muon decay property
 - $R_{acc}(\lambda)$: momentum-dependent tracker acceptance

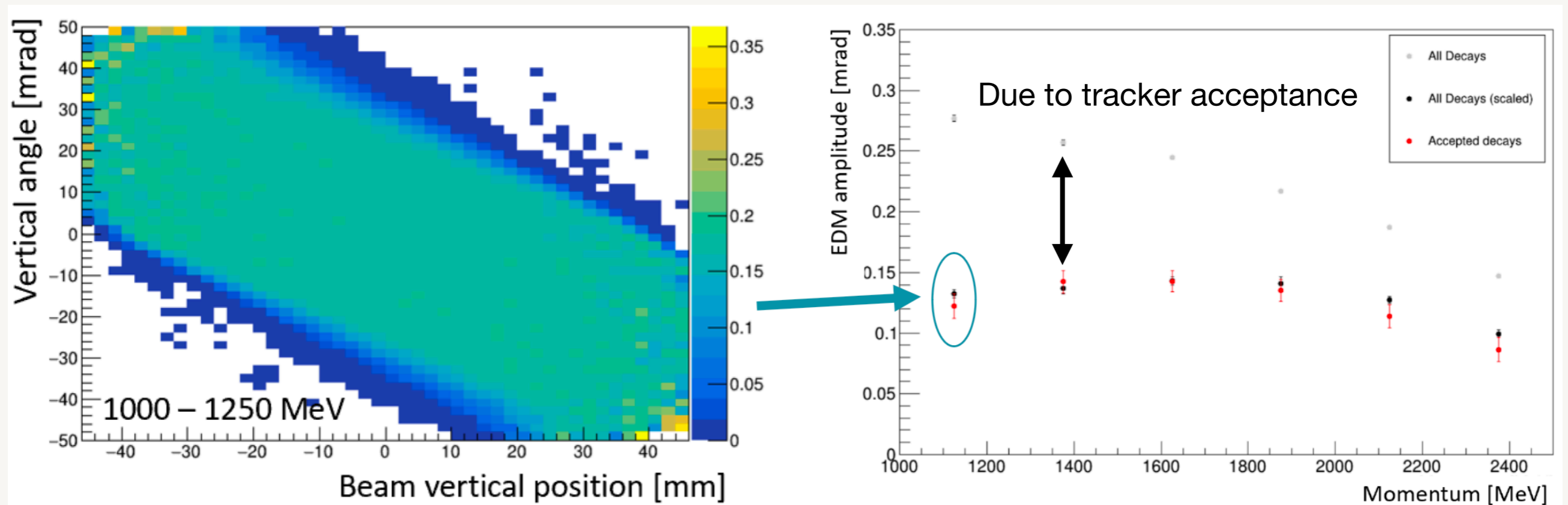
Momentum dependent $R_{e^+}(\lambda)$ factor

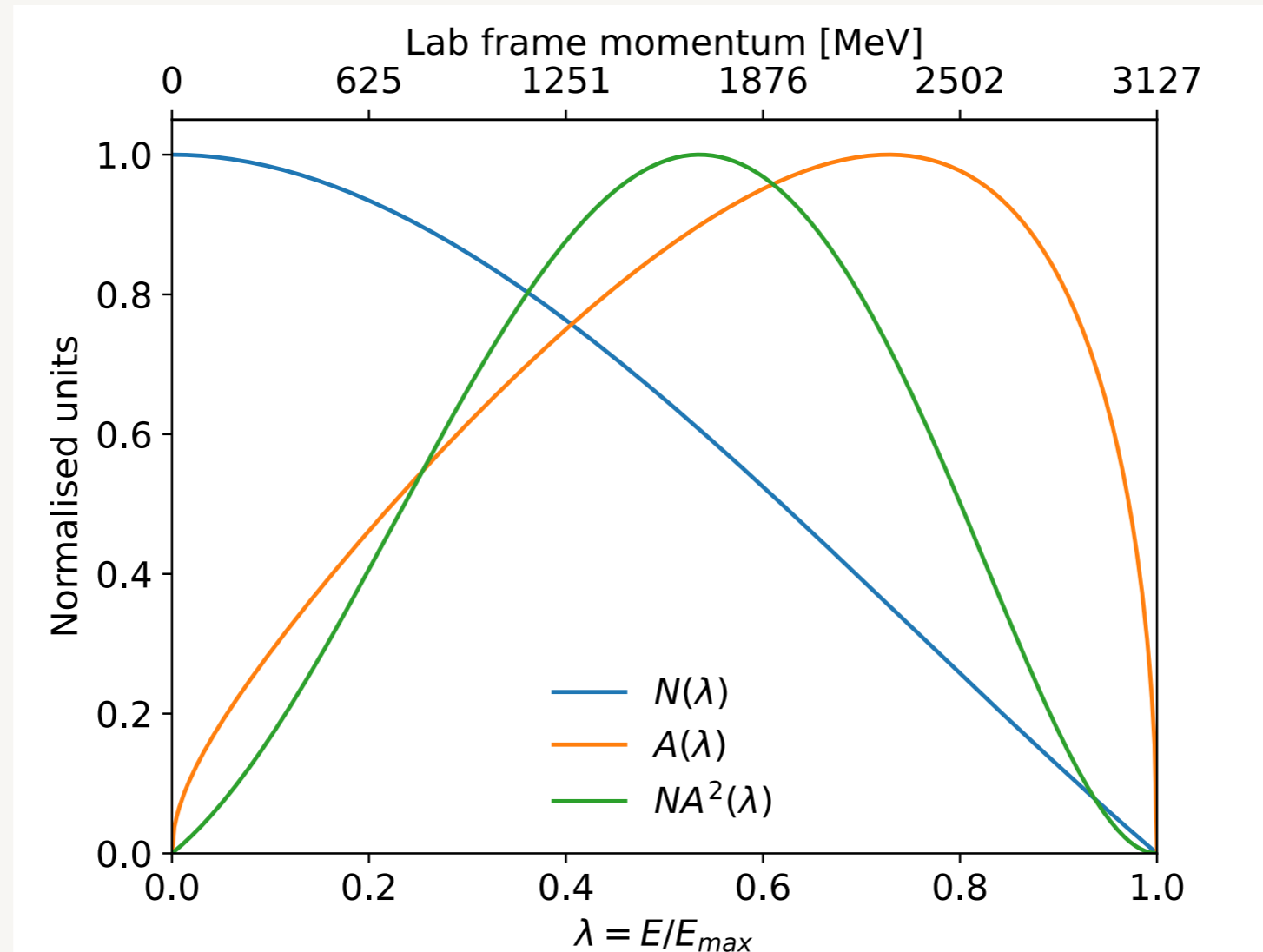
- Positrons are preferentially emitted along muon spin direction
→ ‘Boosted’ Michel spectrum
- Can be described analytically but misses radiative corrections leading to a small reduction in the tilt seen
→ Determine $R_{e^+}(\lambda)$ factor using MC to take account for the higher-order effects



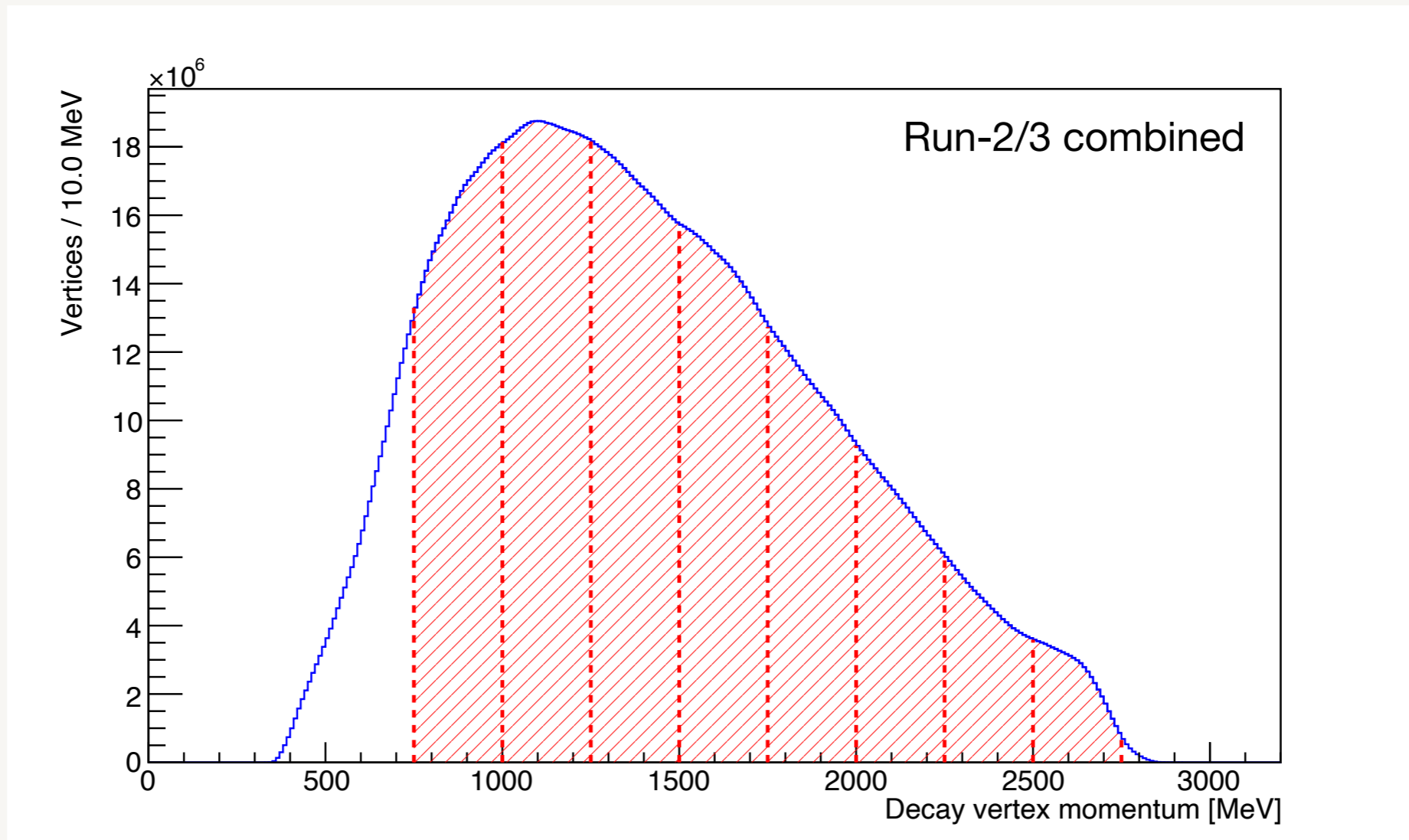
Momentum dependent acceptance $R_{\text{acc}}(\lambda)$ factor

- Due to the finite size of the detector, a fraction of decay positrons can be detected
- The ratio of detected decays to all decays in MC gives $R_{\text{acc}}(\lambda)$ factor
→ Statistically limited due to the low numbers of detected decays
- 2D acceptance probability maps in each momentum bin to shape the ideal all decays MC without reducing its statistical power for correction evaluation



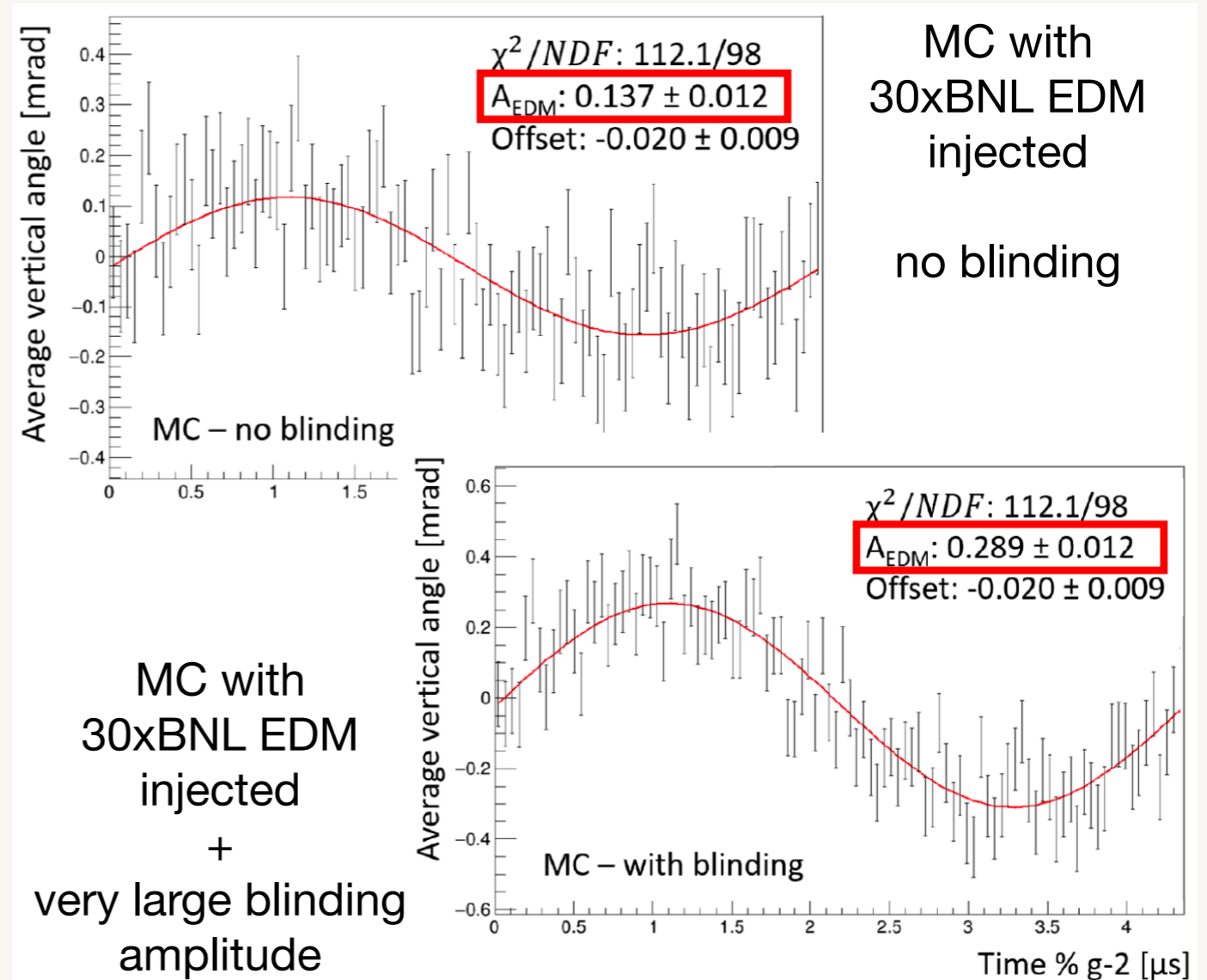


- Statistical sensitivity: $\sigma(d_\mu) \propto 1/\sqrt{NA^2}$
- Mid-momentum range muons carry more sensitivity



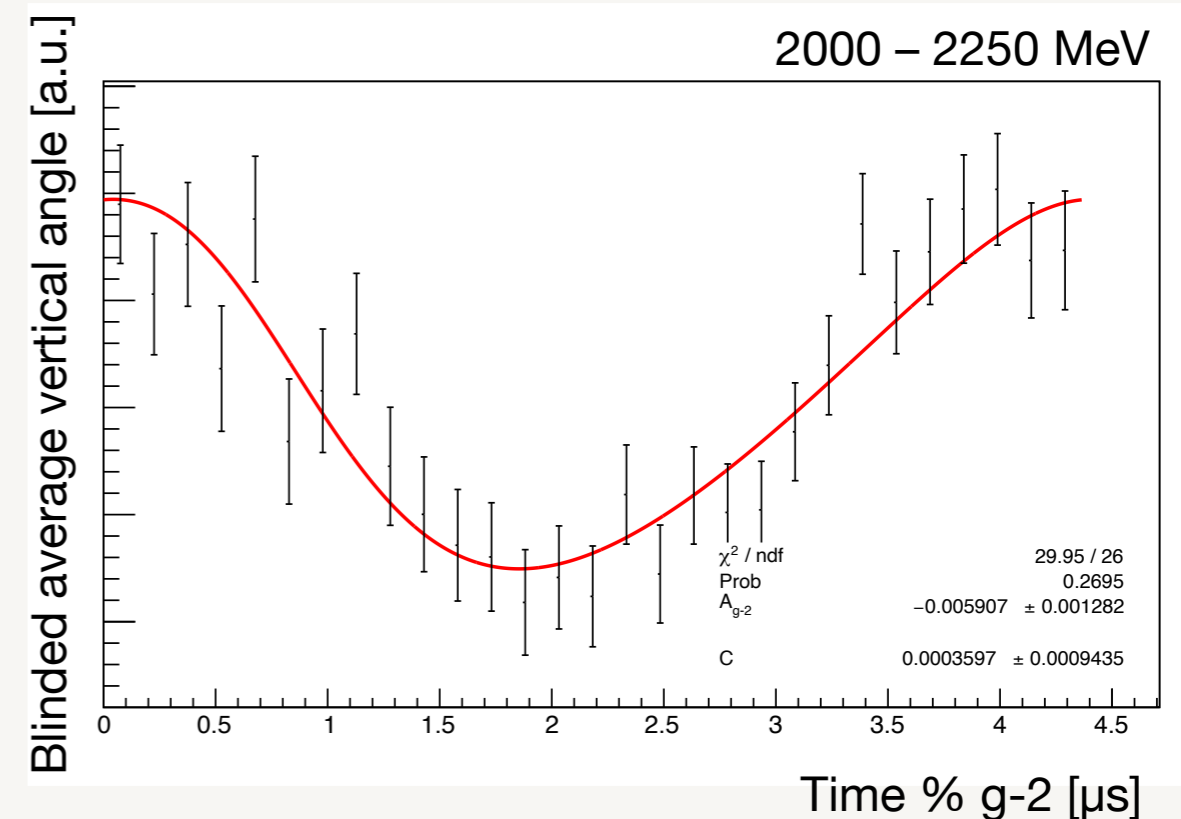
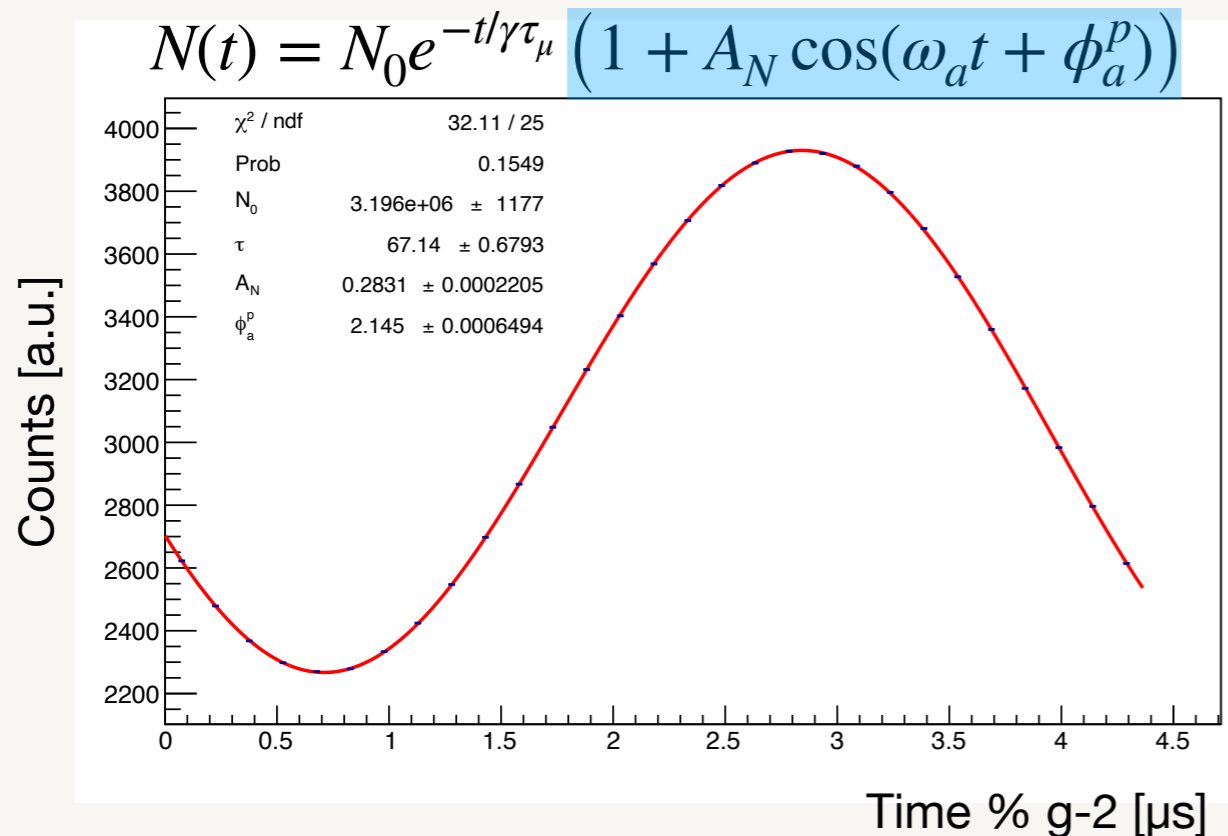
- Momentum range 750 – 2750 MeV are used for the EDM analysis
- Total 8 momentum bins, each 250 MeV wide
 - can increase overall sensitivity to the EDM by allowing more accurate application of momentum-dependent correction factors

- Need to blind the vertical angle oscillation to prevent bias in the analysis
- Inject a very large fake signal into the oscillation in phase with EDM
 - Amplitude is sampled randomly from a gaussian distribution, chosen to be \gg BNL limit
 - Applying per momentum bin
 - Only blind A_{EDM} without changing the fit quality



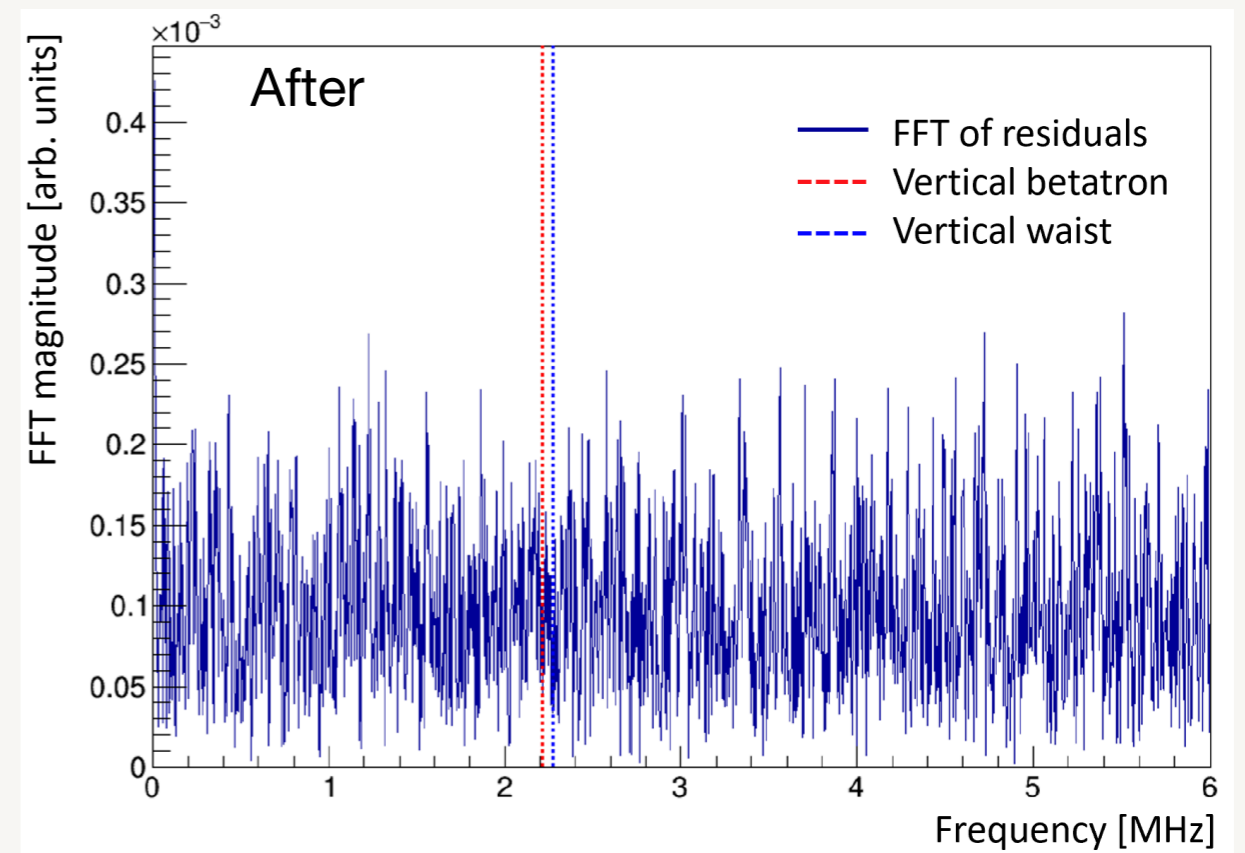
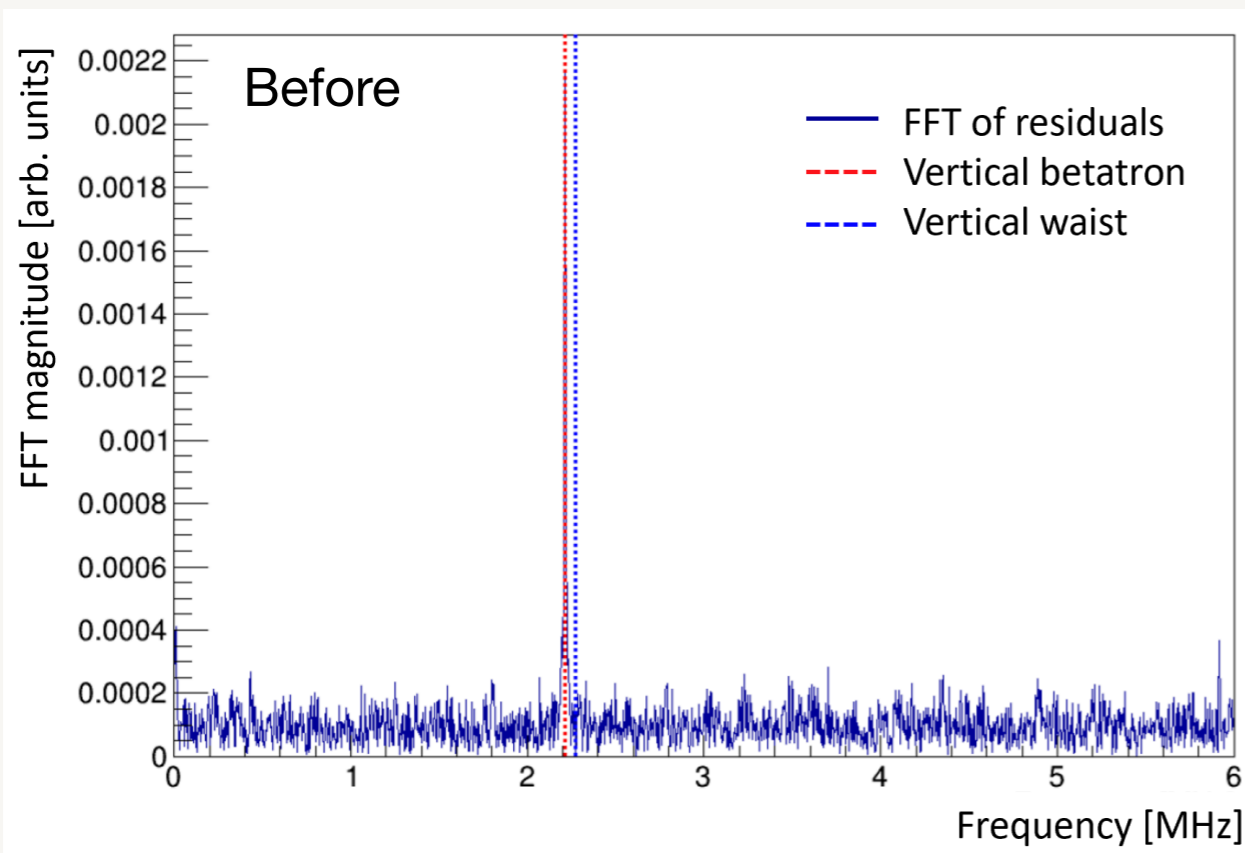
- For each momentum bin, plot average vertical angle vs. time modulo the g-2 period then fit it using

$$\langle \theta_y \rangle = \frac{A_{g-2} \cos(\omega_a t + \phi_a) + A_{\text{EDM}} \sin(\omega_a t + \phi_a)}{1 + A_N \cos(\omega_a t + \phi_a^p)} + c$$



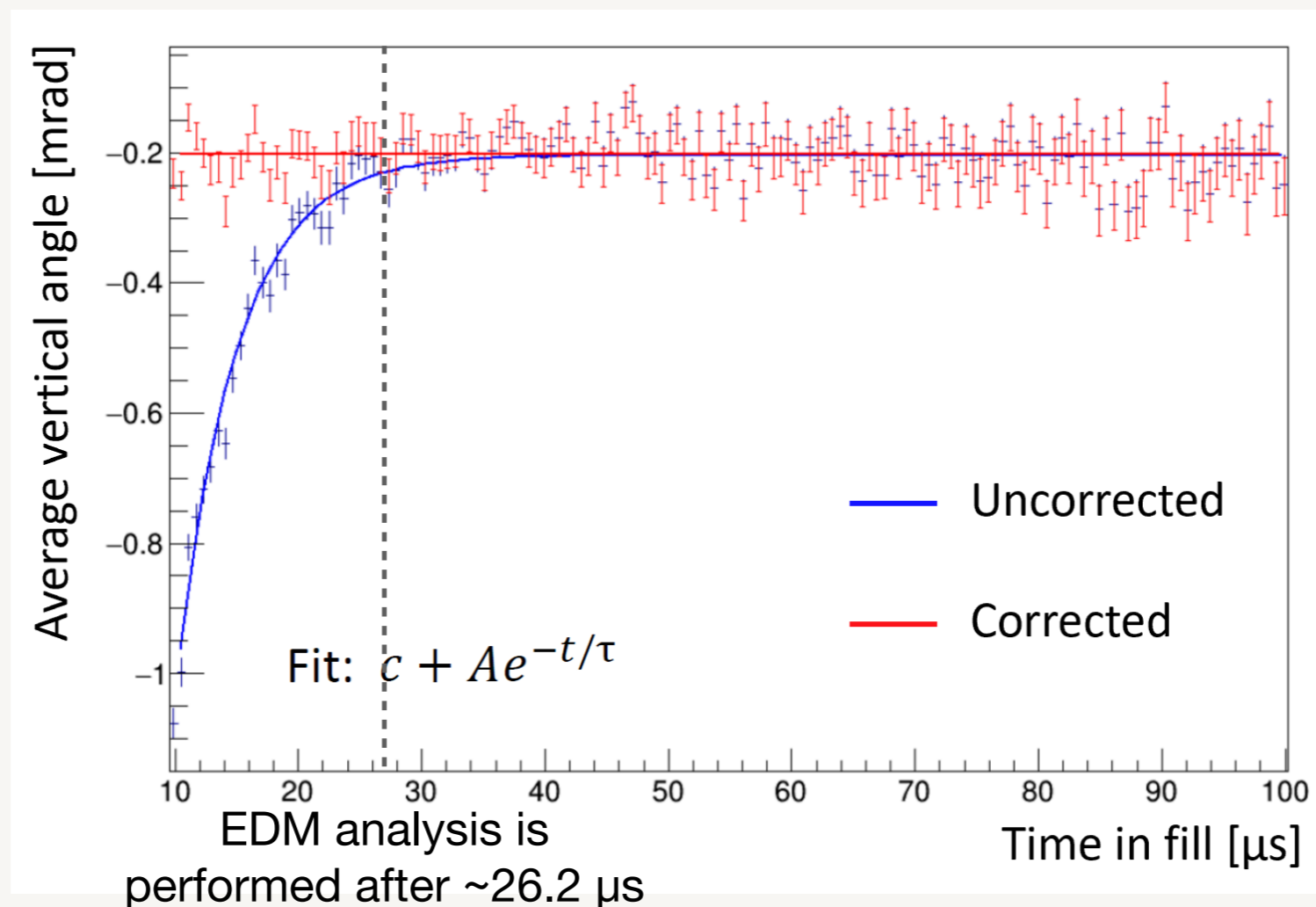
Beam dynamics corrections

- Muon beam has a vertical betatron oscillation which appears in the FFT of the fit residuals
 - Before the analysis, apply time randomisation via a uniform smearing within the oscillation period
 - Fast rotation effect, which is relevant at early times, is similarly randomised out

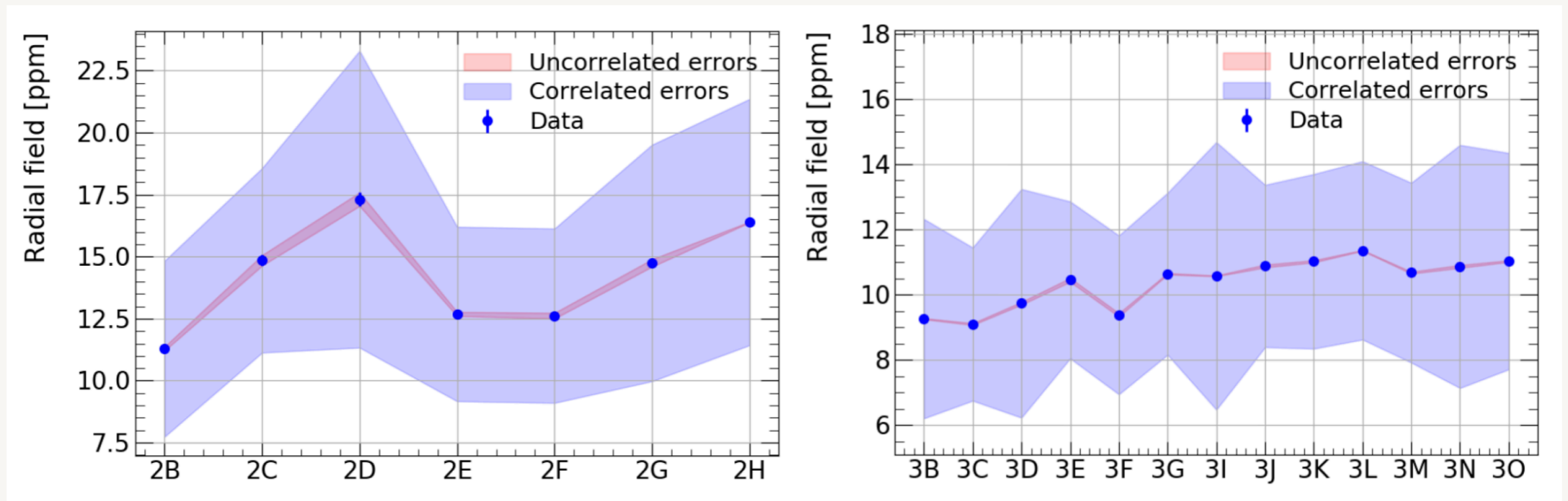


Early time beam scraping correction

- At early times, the average vertical beam position changes rapidly over time due to beam scraping
 - This consequently changes the average vertical decay angle as well
 - Remove the quick angle change by fitting the data for each momentum bin per tracker station

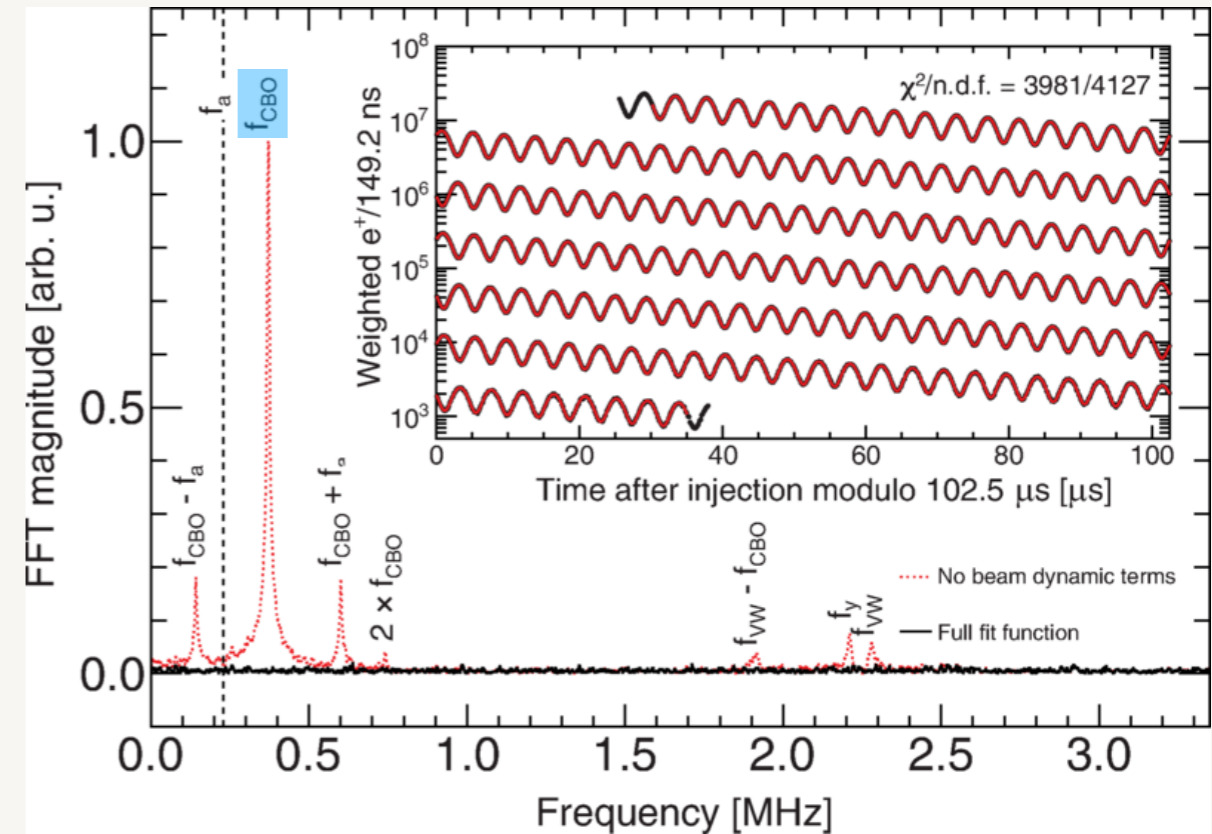


- MDM coupling to the radial magnetic field B_r mimics an EDM signal
- Dedicated ‘radial field scans’ campaign were performed in Run-4/5/6 and extrapolate the measurements to Run-2/3 using the vertical beam position
- Sufficient precision was achieved ensuring that the radial field does not limit the EDM measurement

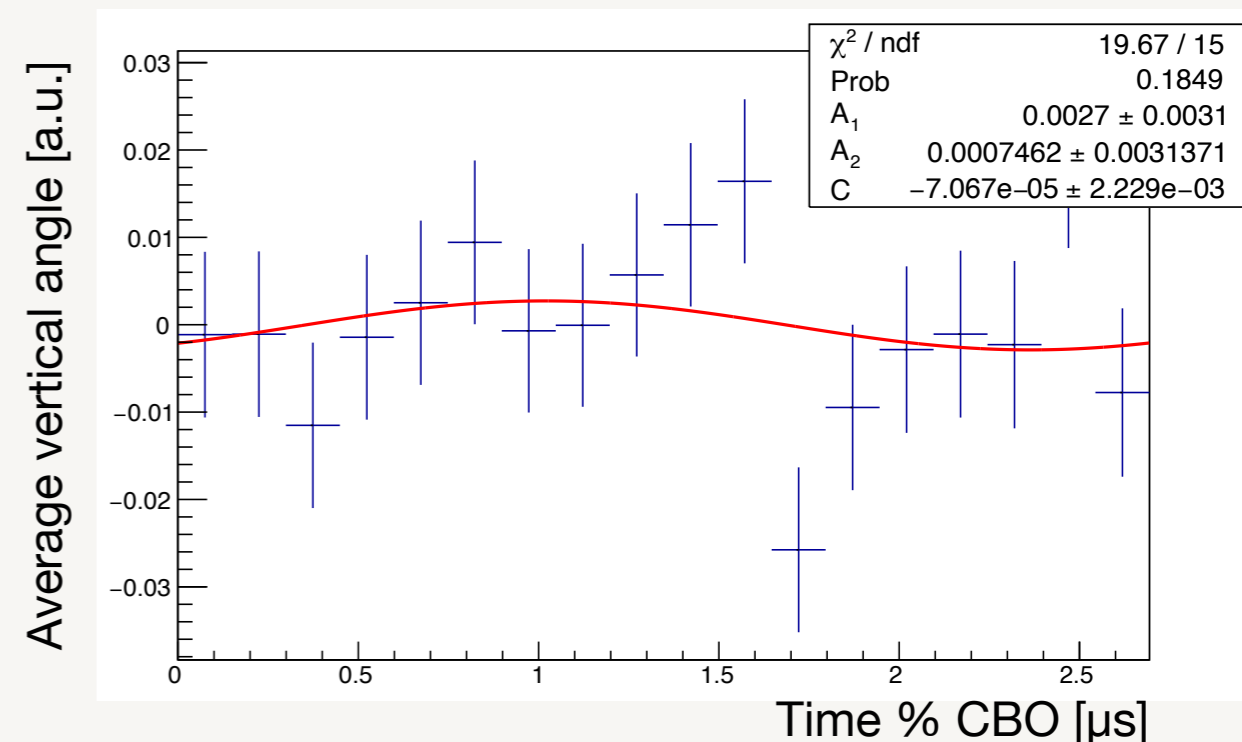


Cross-check at other oscillation frequencies

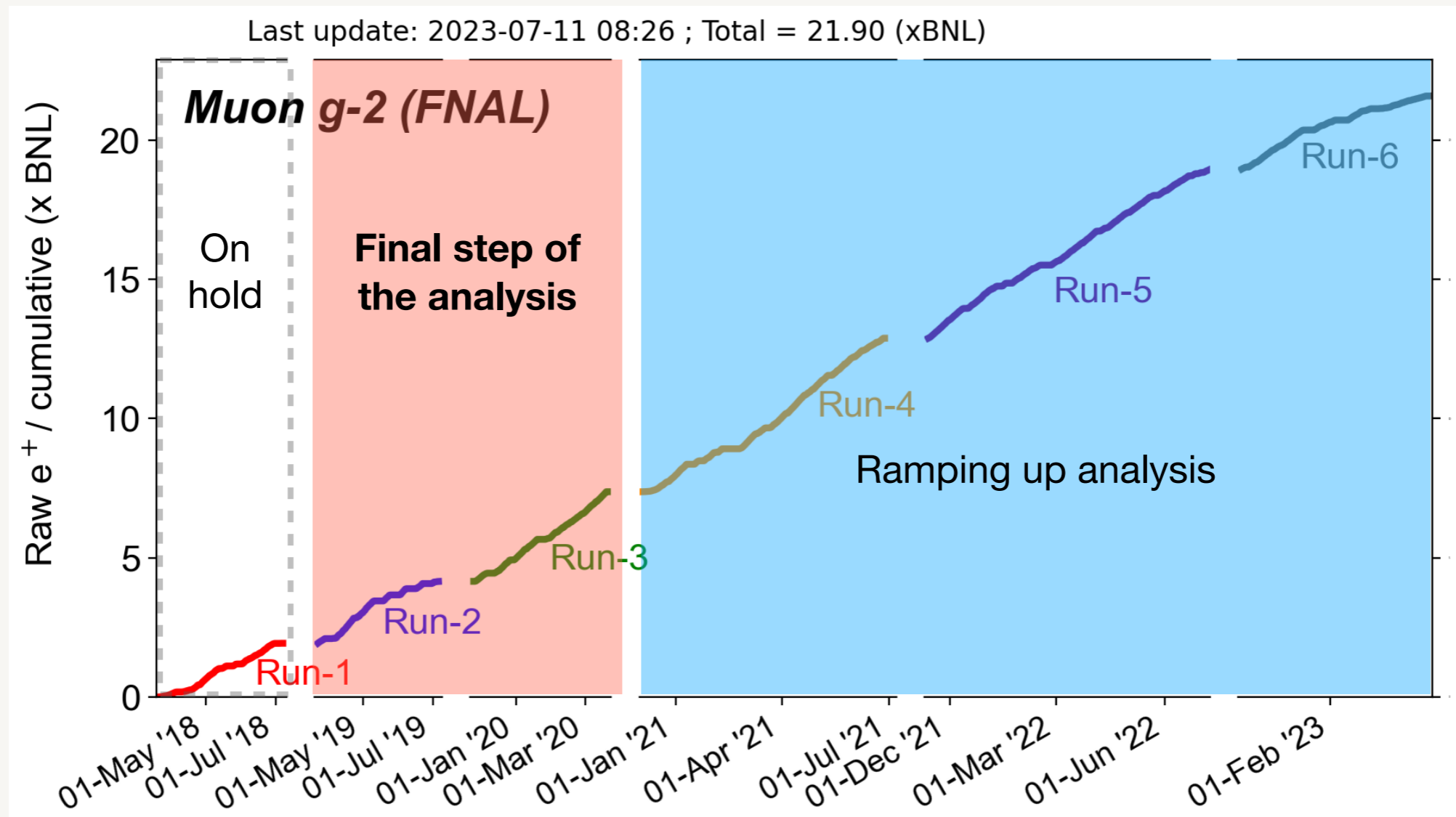
- EDM signal: average vertical angle oscillation $\pi/2$ out of phase with g-2 oscillation
- Cross-check to confirm no average vertical angle oscillation at
 - coherent betatron oscillation (CBO) frequency – the most in-and-out effect
 - random frequency
- The same approach as the main analysis: Plot vertical angle modulo another frequency and fit for oscillation at that frequency
- Unblinded fits confirm no vertical angle oscillation at those frequencies



D.P. Aguillard *et al.*, PRL 131, 161802 (2023)



Timelines for FNAL EDM analysis



- Run-1: ‘complete’ but still blinded
established analysis approach through collaboration review for Run-2 onwards analyses
- **Run-2/3**: nearly completing the analysis, new results expected next year!
collaboration review has started
- Run-4/5/6 + full dataset: analysis just started
The FNAL muon EDM search aims to improve the current best limit by an order of magnitude

- The search for the muon EDM is a unique opportunity to explore CP violation in BSM physics and has the potential to probe the role of LFU
- The FNAL muon EDM search focuses on the tracker-based approach
- Run-2/3 analysis is nearly finalised
 - new results are expected next year and will improve the BNL limit
- With the full dataset, the FNAL muon EDM search aims to improve the BNL limit by an order of magnitude