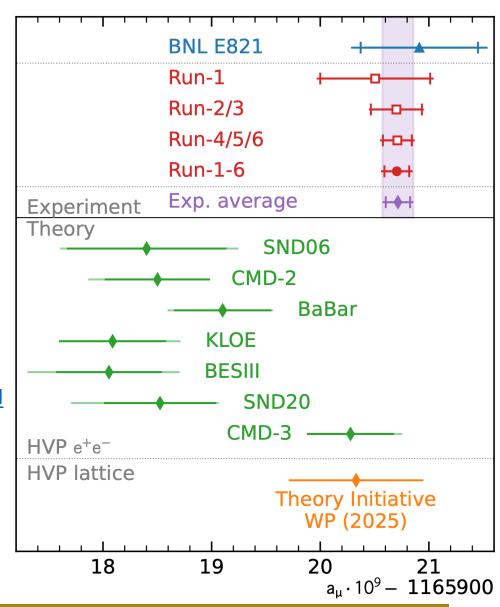


PAT LUX

Current status

- The theory situation still puzzling!
- The Muon g-2 Theory Initiative latest compilation White Paper 2025: Phys.Rept. 1143 (2025) 1-158
- WP25 (based on lattice QCD) agrees with the experiment
- HVP e^+e^- (data-driven approach) was not included for the WP25
 - tensions still to be understood
 - New result from BaBar experiment confirming previous result! <u>TI</u>
 <u>Workshop 2025</u>
- CMD3 result with data-driven approach agrees with WP25 and disagrees with other HVP



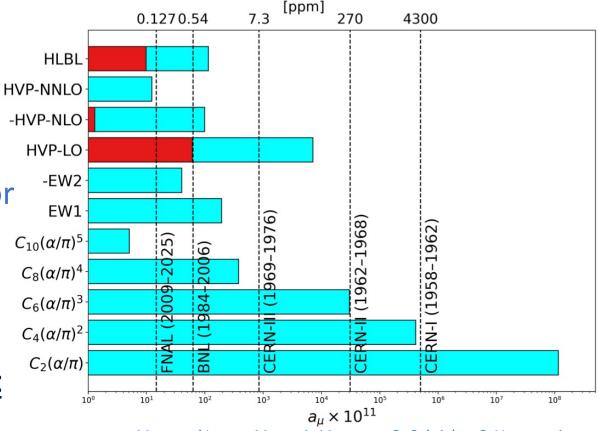


Current status

• The <u>HVP contribution</u> is still **leading** the total **uncertainty** on a_{μ} .

• The Fermilab precision is beyond the HVP contribution, but on a near future this error can be further reduced.

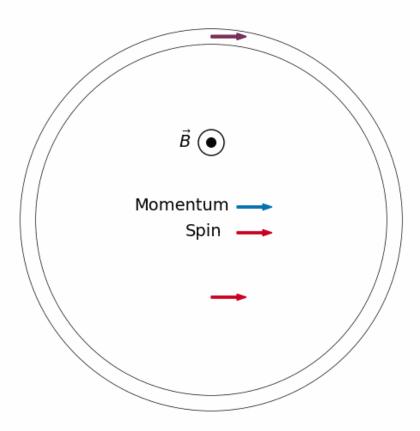
• In a new scenario where the theory puzzle is resolved, an <u>independent measurement</u> of a_u would be important.



Measured Lepton Magnetic Moment - G. Gabrielse, G. Venanzoni



Measurement principle - Fermilab



$$\vec{\omega}_a = \frac{e}{m} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^2 - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$

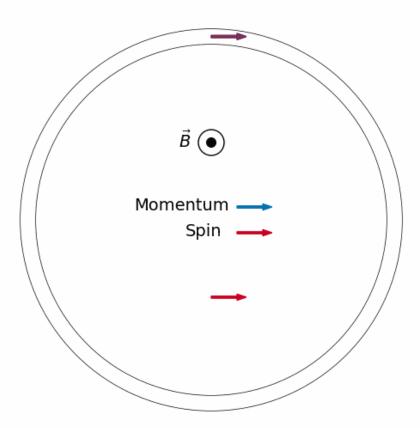
- Electric focusing (vertical confinement)
- 14 m ring diameter (B= 1. 45T)

$$\overrightarrow{\omega}_a = \overrightarrow{\omega}_s - \overrightarrow{\omega}_c = a_\mu \frac{e \overrightarrow{B}}{m}$$





Measurement principle - Fermilab



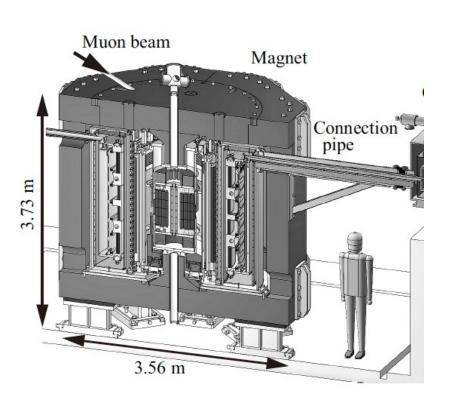
$$\vec{\omega}_a = \frac{e}{m} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^2 - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$

- Electric focusing (vertical confinement)
- 14 m ring diameter (B= 1. 45T)
- Magic momentum γ = 29.3 (p = 3.1 GeV/c)

$$\overrightarrow{\omega}_a = \overrightarrow{\omega}_s - \overrightarrow{\omega}_c = a_\mu \frac{e \overrightarrow{B}}{m}$$



Measurement principle – J-PARC



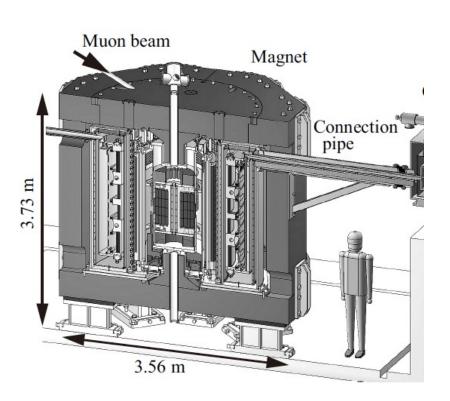
$$\vec{\omega}_a = \frac{e}{m} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^2 - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$

- 300 MeV/c momentum
- 0.66 m ring diameter (B = 3 T)

$$\overrightarrow{\omega}_a = \overrightarrow{\omega}_s - \overrightarrow{\omega}_c = a_\mu \frac{e\overrightarrow{B}}{m}$$



Measurement principle – J-PARC



$$\vec{\omega}_{a} = \frac{e}{m} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^{2} - 1} \right) (\vec{\beta} \times \vec{E}) \right]$$

- 300 MeV/c momentum
- 0.66 m ring diameter (B = 3 T)
- No electric field (E=0)

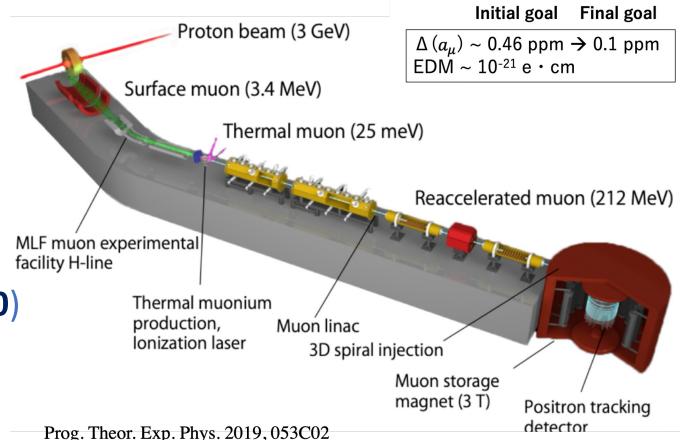
$$\overrightarrow{\omega}_a = \overrightarrow{\omega}_s - \overrightarrow{\omega}_c = a_\mu \frac{e \overrightarrow{B}}{m}$$

Both the experiment can extract a_{μ} very precisely measuring \overrightarrow{B} and $\overrightarrow{\omega}_{a}$



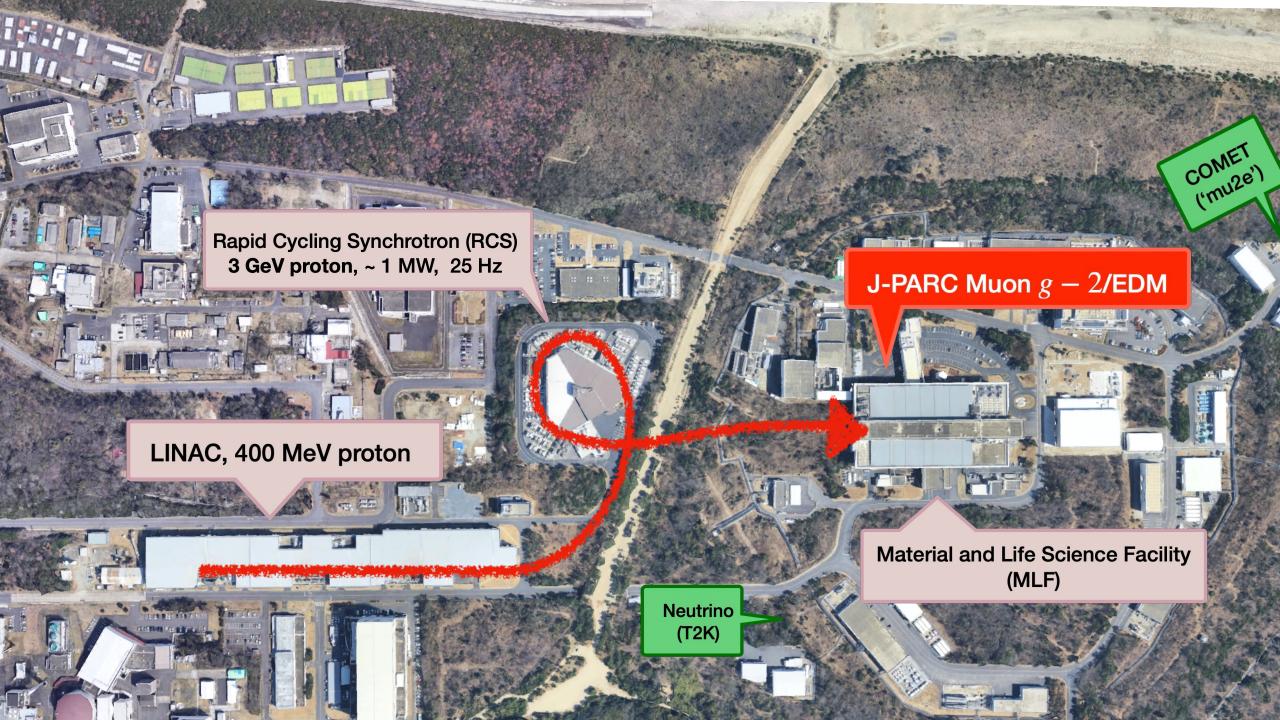
New features of E34

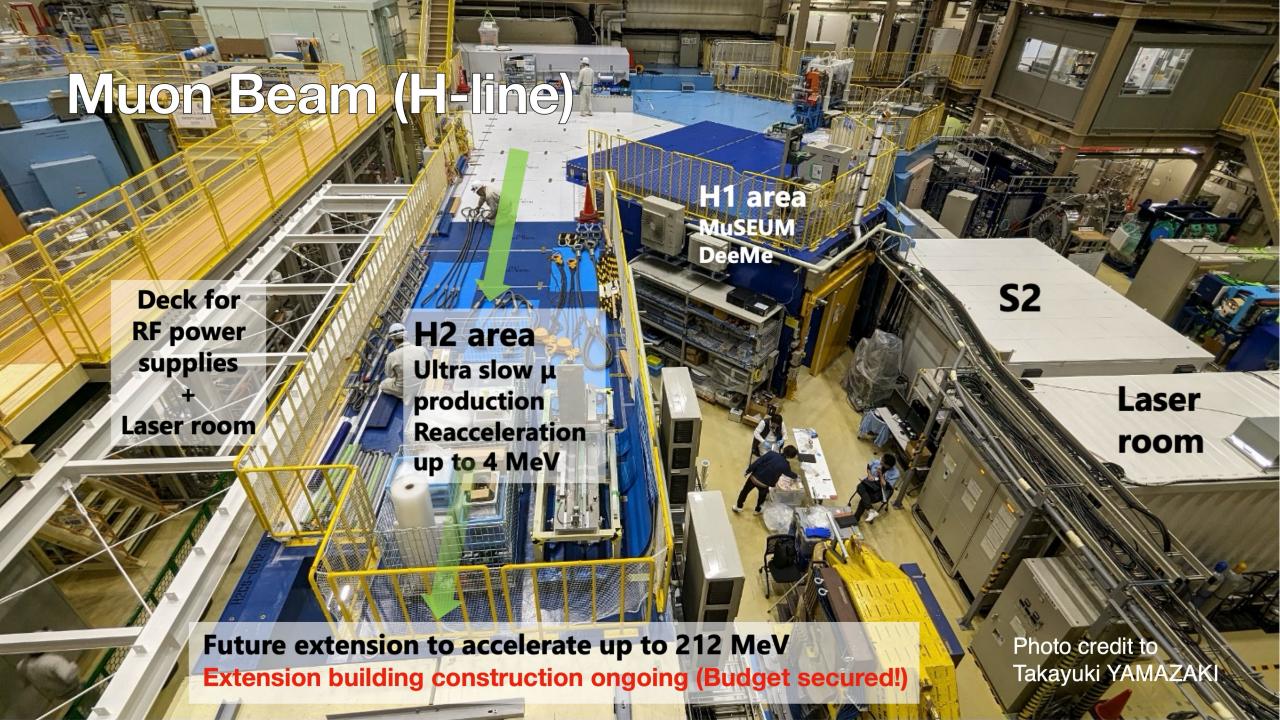
- Low emittance muon beam (1/1000)
- Muon acceleration -> 212 MeV
- No strong focusing
- 3D spiral injection:
 - Large kick in few ns
 - Good injection efficiency (x10)
- Compact storage ring (1/20)
- Tracking detector



Excellent sensitivity to muon EDM about 100 times better than the previous limit

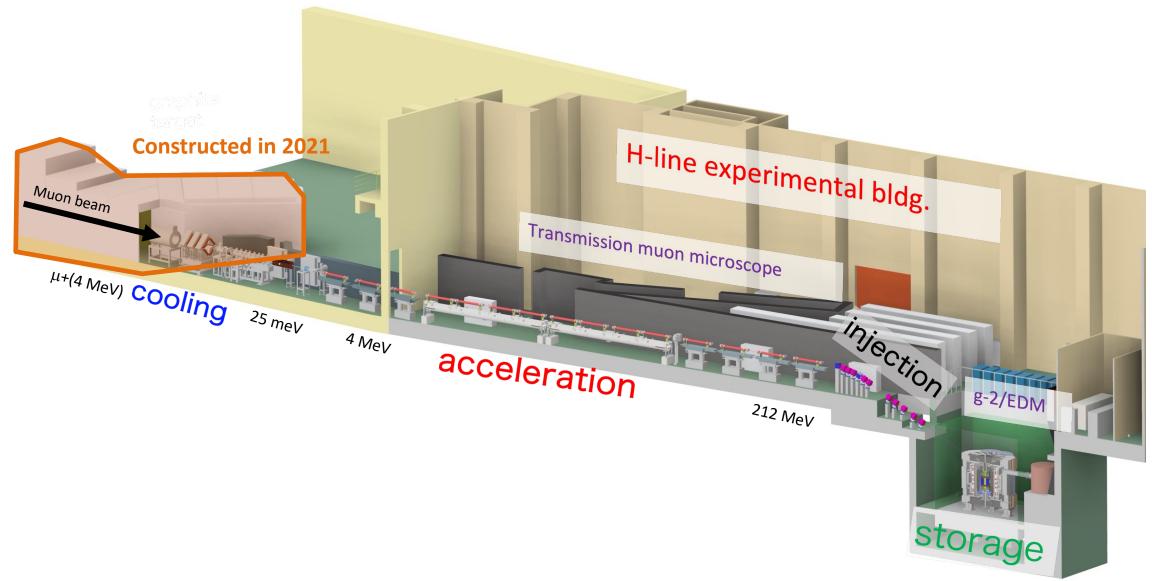






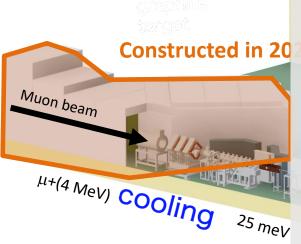


Muon g-2 at J-PARC (E34)



11/11/25 Shields, area control (2022) E.Bottalico - (MPPW 2025) 12





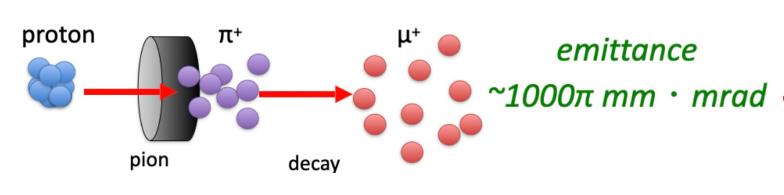


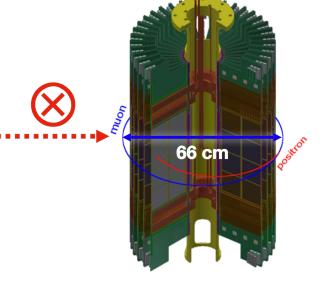
11/11/25 Shields, area control (2022)

E.Bottalico - (MPPW 2025)

13







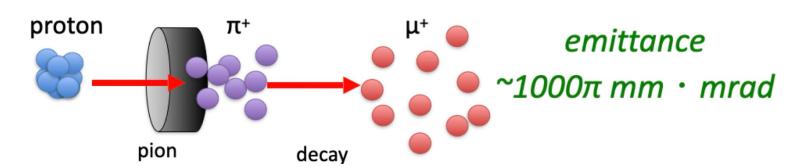
A conventional muon beam:

- can not be injected without a strong focusing → electric field;
- This leads to muon losses and background contamination from π .

Desired beam:

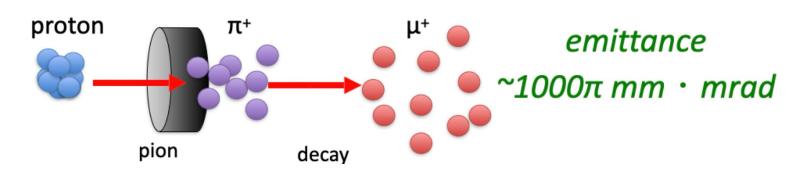
- The muon must be compact and non-divergent;
- Typically with a RMS of \sim mm \rightarrow never achieved before.



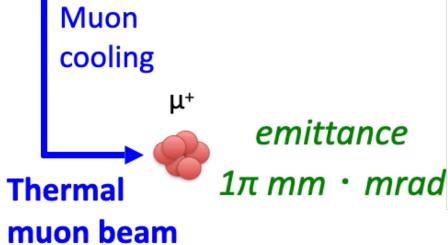










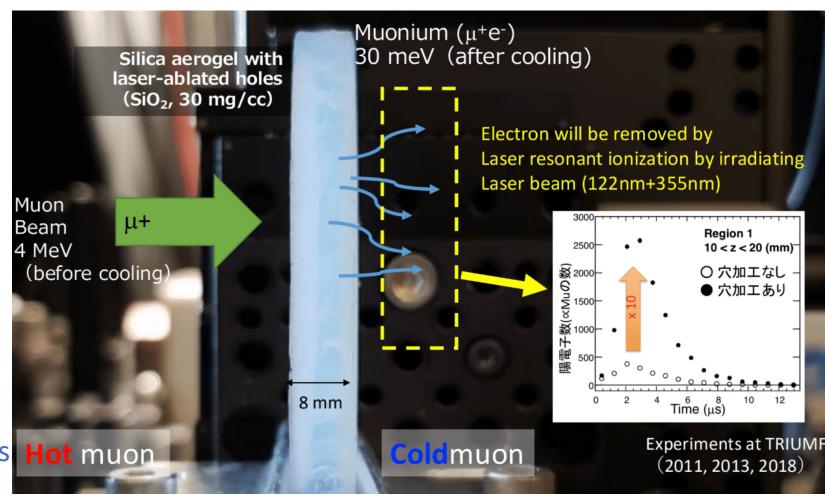




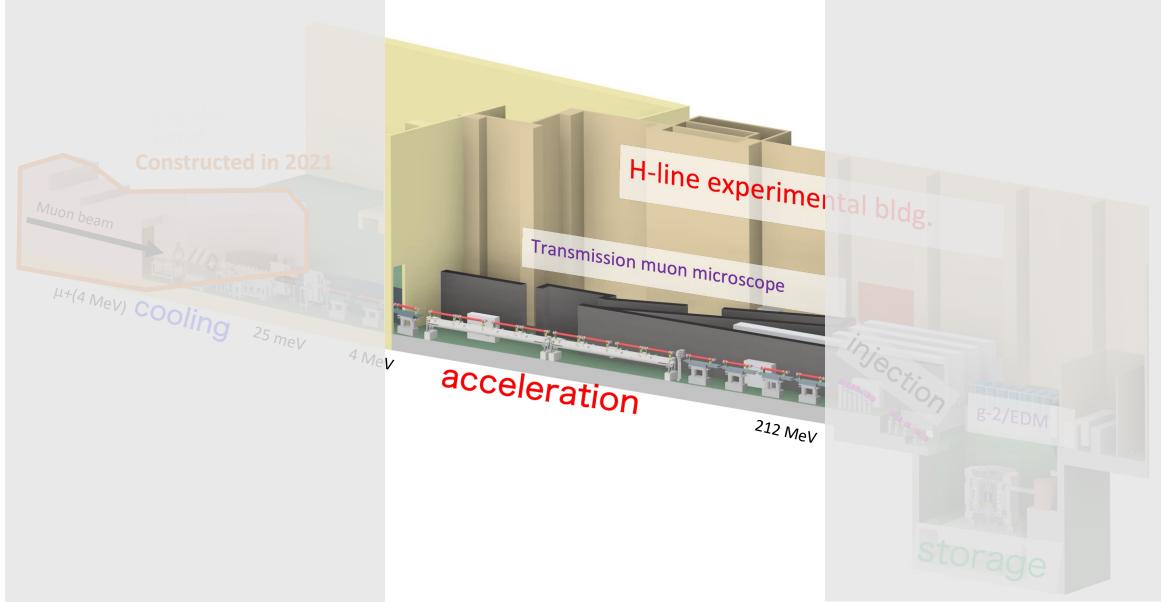


Ultra-cold muons

- Surface μ^+
- Stop in (laser ablated surface)
 Aerogel
- Diffuse Muonium (μ^+e^-) atoms into vacuum
- Ionize:
 - 1S \rightarrow 2P \rightarrow unbound
 - Max Polarization 50%
- Accelerate:
 - E field, RFQ, linear structures Hot muon
 - E= 212 MeV (p= 300 MeV/c)







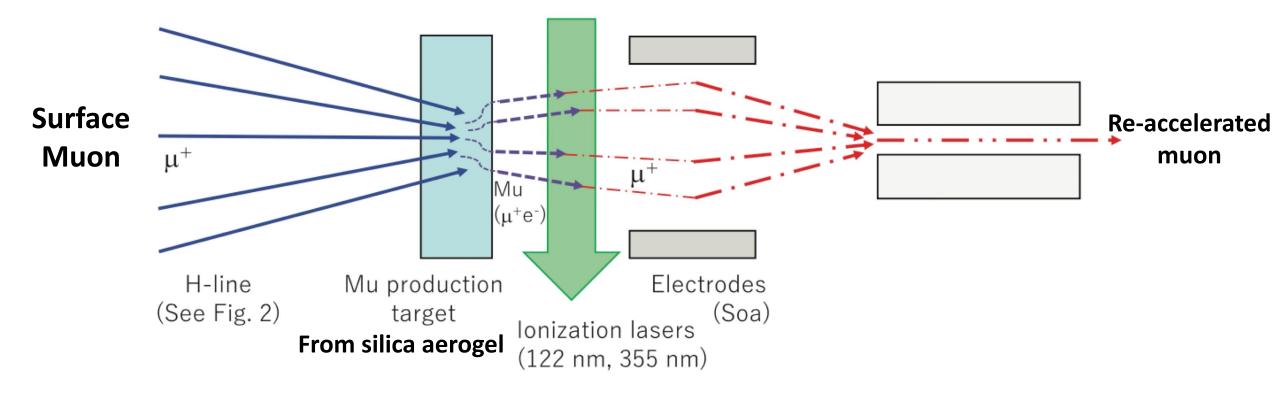
11/11/25 Shields, area control (2022)

E.Bottalico - (MPPW 2025)

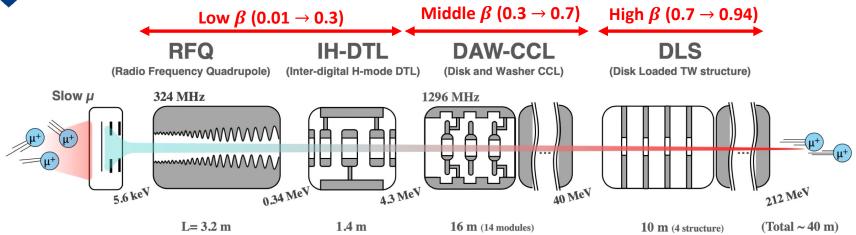
18



	Surface muon	Thermal muon	Accelerated Muon
E	3.4 MeV	30 meV	212 MeV
p	27 MeV/c	2.3 keV/c	300 MeV/c
Δρ/ρ	0.05	0.4	$4x10^{-4}$

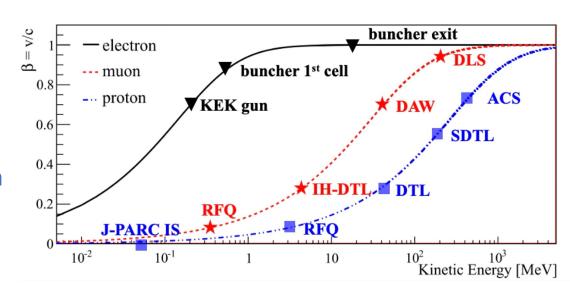




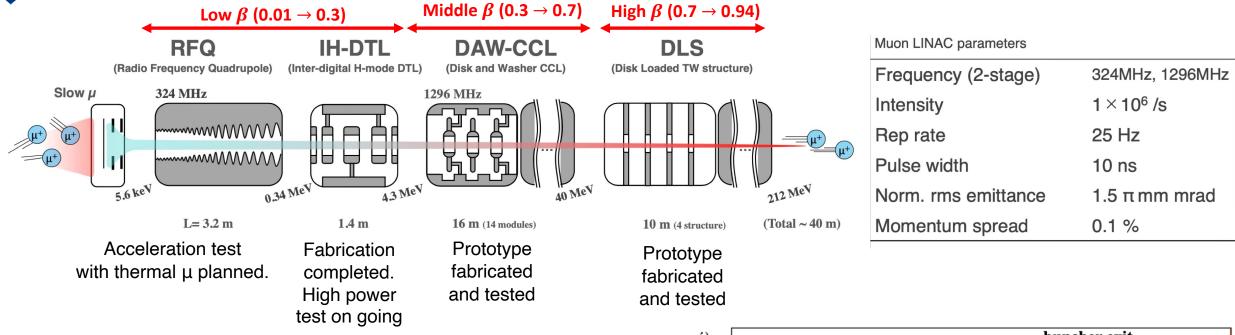


	Muon LINAC parameters			
	Frequency (2-stage)	324MHz, 1296MHz		
	Intensity	1×10^6 /s		
1	Rep rate	25 Hz		
,	Pulse width	10 ns		
	Norm. rms emittance	$1.5~\pi\text{mm}$ mrad		
	Momentum spread	0.1 %		

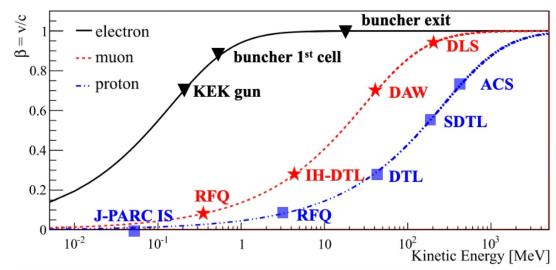
- The first muon-dedicated linac in the world!
- Muon Acceleration to 212 MeV
- 4 steps acceleration depending on eta -> total length 40 m







- The first muon-dedicated linac in the world!
- Muon Acceleration to 212 MeV
- 4 steps acceleration depending on β -> total length 40 m





Phys. Rev. Lett. **134**, 245001

Acceleration from termal energy to 100 keV by RF system

PHYSICAL REVIEW LETTERS 134, 245001 (2025)

Editors' Suggestion

Featured in Physics

Acceleration of Positive Muons by a Radio-Frequency Cavity

S. Aritome, ¹ K. Futatsukawa, ² H. Harao, ³ K. Hayasakao, ⁴ Y. Ibaraki, ⁵ T. Ichikawa, ⁵ T. Ijimao, ^{5,6} H. Iinumao, ⁷ Y. Ikedo, ² Y. Imai, ³ K. Inami, ^{5,6} K. Ishidao, ² S. Kamal, ⁸ S. Kamiokao, ² N. Kawamurao, ² M. Kimurao, ² A. Koda, ² S. Koji, ⁵ K. Kojimao, ^{5,4} A. Kondo, ⁵ Y. Kondo, ⁹ M. Kuzuba, ⁸ R. Matsushita, ¹ T. Mibeo, ² Y. Miyamotoo, ³ J. G. Nakamurao, ² Y. Nakazawao, ^{7,4} S. Ogawa, ^{10,4} Y. Okazakio, ² A. Olino, ^{11,12} M. Otanio, ² S. Oyama, ¹ N. Saitoo, ² H. Sato, ⁷ T. Sato, ⁷ Y. Sato, ⁴ K. Shimomura, ² Z. Shioya, ¹³ P. Strassero, ² S. Sugiyama, ⁵ K. Sumi, ^{5,7} K. Suzukio, ⁶ Y. Takeuchio, ^{13,8} M. Tanida, ¹³ J. Tojoo, ^{13,10} K. Ueda, ⁵ S. Uetake, ³ X. H. Xieo, ^{14,15} M. Yamada, ³ S. Yamamoto, ³ T. Yamazakio, ² K. Yamura, ⁴ M. Yoshida, ² T. Yoshiokao, ^{10,13} and M. Yotsuzuka

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Department of Chemistry, Laboratory for Advanced Spectroscopy and Imaging Research (LASIR), University of British Columbia, Vancouver, British Columbia V6T 1Z1, Canada

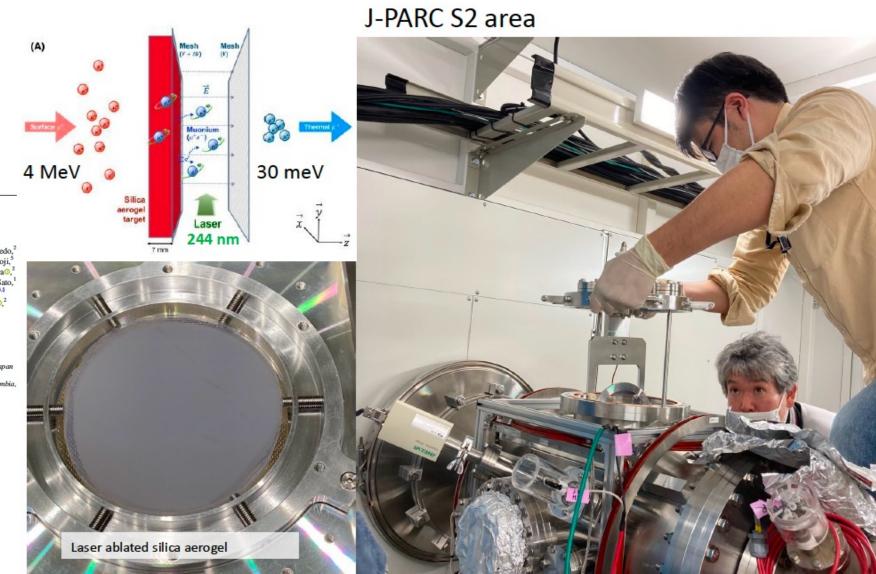
Japan Atomic Energy Agency (JAEA), Tokai, Naka, Ibaraki 319-1195, Japan
 Research Center of Advanced Particle Physics, Kyushu University, Fukuoka, Fukuoka 819-0395, Japan
 Department of Physics and Astronomy, University of Victoria, Victoria, British Columbia V8P 5C2, Canada
 TRIUMF, Vancouwer, British Columbia V6T 2A3, Canada

¹³Faculty of Science, Kyushu University, Fukuoka, Fukuoka 819-0395, Japan ¹⁴School of Physics, Peking University, Beijing 100871, China ¹⁵State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, China

(Received 16 October 2024; accepted 21 April 2025; published 16 June 2025)

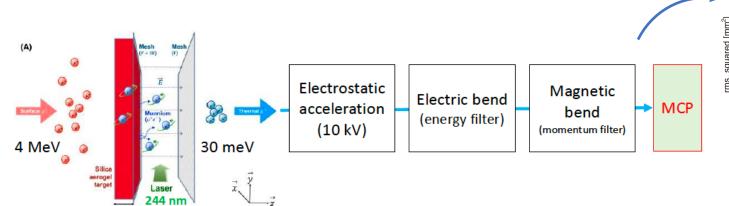
Acceleration of positive muons from thermal energy to $100\,\text{keV}$ has been demonstrated. Thermal muons were generated by resonant multiphoton ionization of muonium atoms emitted from a sheet of laser-ablated aerogel. The thermal muons were first electrostatically accelerated to $5.7\,\text{keV}$, followed by further acceleration to $100\,\text{keV}$ using a radio-frequency quadrupole with an intensity of $2\times10^{-3}\,\mu^+\text{p}$ pulse. The transverse normalized ms emittance of the accelerated muons in the horizontal and vertical planes were $0.85\pm0.25(\text{stat})^{+0.025}_{-0.15}(\text{syst})$ π mm mrad, respectively. The measured emittance values demonstrated phase-space reduction by a factor of 2.0×10^{2} (horizontal) and 4.1×10^{2} (vertical) allowing good acceleration efficiency. These results pave the way to realize the first-ever muon accelerator for a variety of applications in particle physics, material science, and other fields.

DOI: 10.1103/PhysRevLett.134.245001

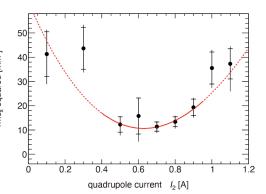




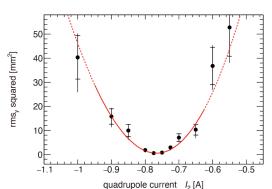
Muon Cooling demonstration:







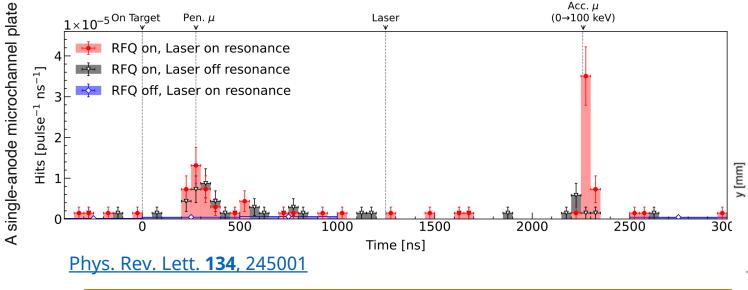
vertical

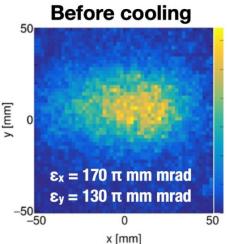


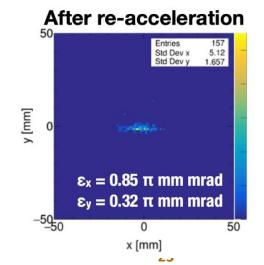
 $\varepsilon_x = 0.85 \pm 0.25(stat)^{+0.22}_{-0.13}(syst) [\pi \text{ mm mrad}]$

 $\varepsilon_y = 0.32 \pm 0.03 \text{(stat)}^{+0.05}_{-0.02} \text{(syst)} [\pi \text{ mm mrad}]$

Emittance reduction by ~10⁻³
The birth of low-emittance muon beam

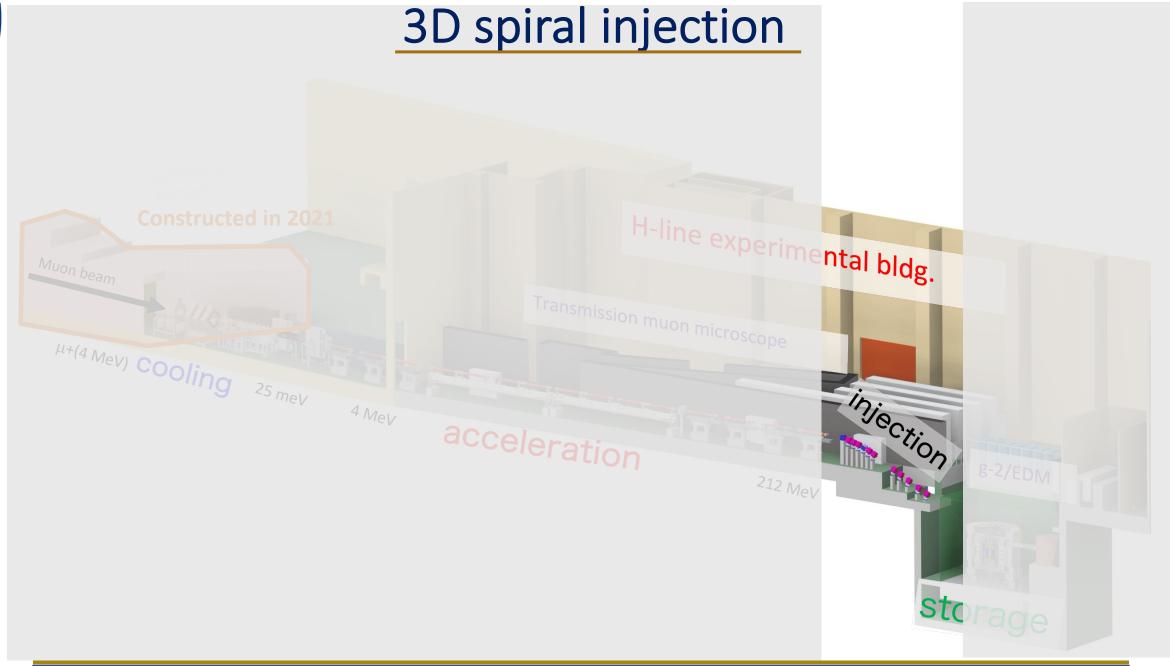








11/11/25

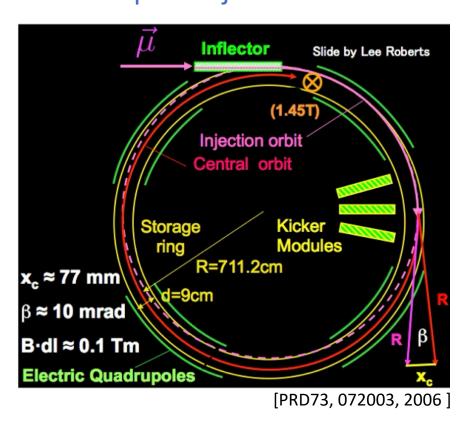


Shields, area control (2022)
E.Bottalico - (MPPW 2025)



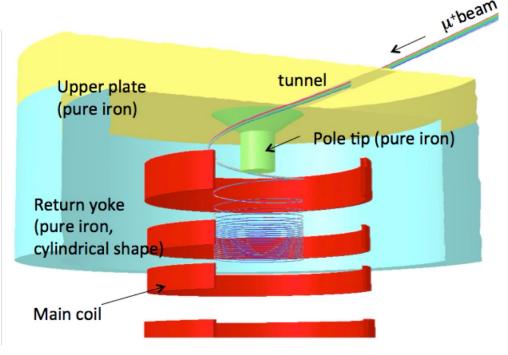
3D spiral injection

The 3D spiral injection scheme has been invented for small muon orbit



Conventional 2D injection @BNL and FNAL

- •Inflector + horizontal kicker
- Efficiency ~3-5%



[H. linuma et al., NIMA 832, 51, 2016]

Novel injection @J-PARC

- •3D spiral injection + vertical kicker
- •Efficiency > 80%
- •to be adopted for the EDM @ PSI too



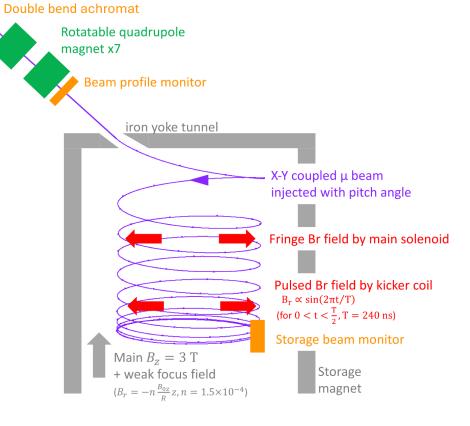
3D spiral injection

from LINAC

• Low emittance muon beam (300MeV, 0.3π mm-mrad) will be injected into the storage orbit and stored without electric focusing with good injection efficiency.

Key points

- Inject low emittance beam with appropriate X-Y coupling into solenoid magnet – to <u>compensate fringe field</u> felt by each muon
- 2. Apply appropriate radial Br-field (Fringe Br-field + kicker coil Br-field).
 - to guide muons to the uniform magnetic field region.
- 3. Store muon beam by weak focusing.





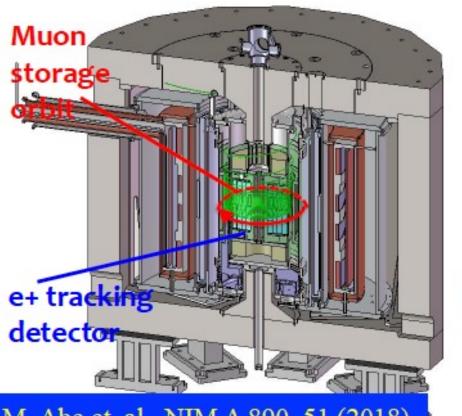


11/11/25 Shields, area control (2022)
E.Bottalico - (MPPW 2025)
27



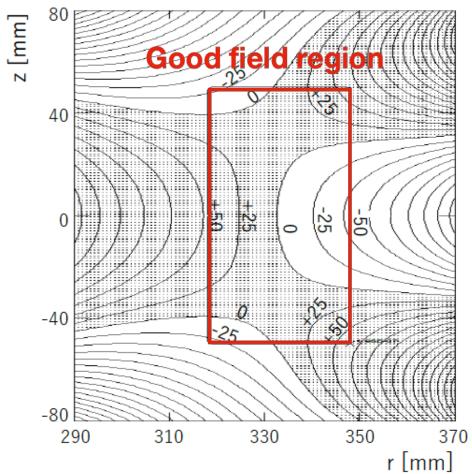
Storage Magnet

3 Tesla MRI-type superconducting solenoid magnet is under design



M. Abe et. al., NIM A 890, 51 (2018)

- Storage region :
 - radius: 33.3±1.5 cm
 - > height: ±5 cm
 - > Field strength: 3T
 - Uniformity: 0.1 ppm (Azimuthal integral)
- Injection region :
 - > Smooth field for beam injection
- Weak focus field: -5e-4 T/m of Br at maximum



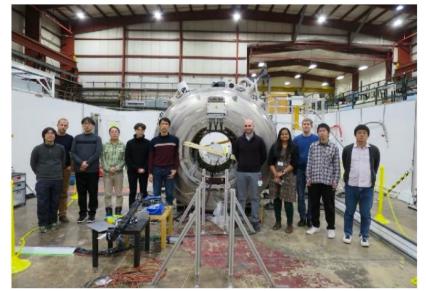
- Average magnetic field uniformity is better than 0.1 ppm
- 25 ppb/line



Storage Magnet

- Local uniformity of 1 ppm was demonstrated by the MUSEUM experiment magnet at 1.2 T;
 - Further tests will be carried out at 3 T.
- In the cross-calibration of FNAL and J-PARC field probes at ANL, ~7 ppb agreement was obtained with 15 ppb uncertainties.





MRI magnet for MuSEUM experiment

Magnetic field after shimming

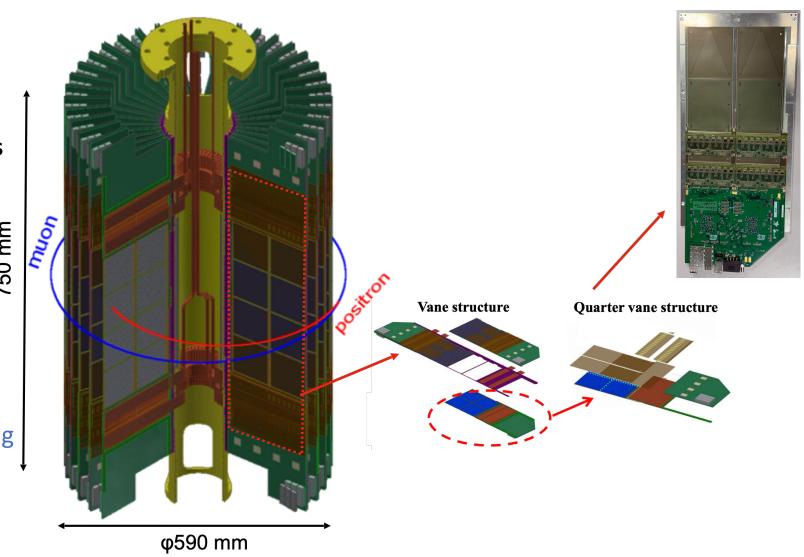
Cross calibration at ANL in January 2019



Positron Tracking Detector

"Prototype quarter-vane"

- 40 modules (vanes) each 200mm (radial) x 400mm (axial)
- Each vane consists of **16 Si sensors** (10x10 cm², 320 μ m thickness).
- Two-dimensional hit position is reconstructed from orthogonally arranged silicon strip sensor (512 strips with 190 μm pitch)
- 32 Readout ASIC w/ 5nsec sampling rate.



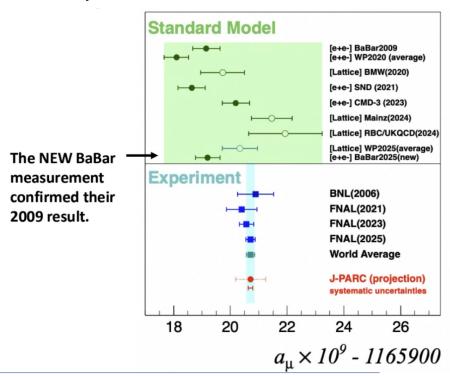
Expected sensitivity - Statistics

- A TDR muon rate $3.2 \times 10^8 \mu/\text{sec}$ at the entrance at 1 MW proton power.
- The expected intensity of stored muon is 1.3×10^5 µ/sec. Cumulative efficiency from thermal muon generation to reconstructed positron is 4.0×10^{-4}
- 2-years data taking (2×10^7 seconds, ~ 230 days) will give a total positron 5.7×10¹¹,

achieving the BNL precision of **0.45 ppm** on a_{μ} .

Table 5. Summary of statistics and uncertainties.

	Estimation
Total number of muons in the storage magnet	5.2×10^{12}
Total number of reconstructed e^+ in the energy window [200, 275 MeV]	5.7×10^{11}
Effective analyzing power	0.42
Statistical uncertainty on ω_a [ppb]	450
Uncertainties on a_{μ} [ppb]	450 (stat.)
	< 70 (syst.)
Uncertainties on EDM [$10^{-21} e \cdot cm$]	1.5 (stat.)
	0.36 (syst.)



Expected sensitivity - Systematic

The systematic uncertainties are estimated to be less than 70 ppb – smaller than the

statistical one:

Table 6. Estimated systmatic uncertainties on a_{μ} .

Anomalous spin precession (ω_a)		Magnetic field (ω_p)		
Source	Estimation (ppb)	Source	Estimation (ppb)	
Timing shift	< 36	Absolute calibration	25	
Pitch effect	13	Calibration of mapping probe	20	
Electric field	10	Position of mapping probe	45	
Delayed positrons	0.8	Field decay	< 10	
Diffential decay	1.5	Eddy current from kicker	0.1	
Quadratic sum	< 40	Quadratic sum	56	

 $\delta a_{\mu(syst)} \sim 70 \text{ ppb} \rightarrow \text{this experiment is expected to be strongly statistically limited}.$

Expected sensitivity comparison with FNAL

Here is the comparison between the Run-456 FNAL result and the project error for J-PARC

experiment:

FNAL – Run456

Quantity	Correction (ppb)	Uncertainty (ppb)
ω_a^m (statistical) ω_a^m (systematic)		114 30
C_e	347	27
$egin{array}{c} C_e \ C_p \end{array}$	175	9
\dot{C}_{pa}	-33	15
C_{dd}	26	27
C_{ml}	0	2
$\langle \omega_p' \times M \rangle$ (mapping, tracking)		34
$\langle \omega_p' \times M \rangle$ (calibration)		34
B_k	-37	22
B_q	-21	20
$\delta\omega_{a_{syst}}\sim$ 52 ppb	$\delta \omega_{p_{syst}} \sim$	57 ppb

J-PARC - TDR

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experiment:

FNAL – Run456

Correction (ppb)	Uncertainty (ppb)
	114 30
347 175 -33 26	27 9 15 27
0	27 2 34 34
-37 -21	22 26
	347 175 -33 26 0

J-PARC - TDR

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 $\delta a_{\mu(syst)} \sim 78 \; \mathsf{ppb}$

 $\delta a_{\mu(syst)} \sim 70~{
m ppb}$



- Given the strong limitation on statistics we can tweak the current set-up to increase the statistics.
- The statistical precision on the anomalous precession frequency ω_a is:

$$\frac{\Delta\omega_a}{\omega_a} = \frac{1}{\omega_a \gamma \tau P} \sqrt{\frac{2}{NA^2}}$$



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- Magnetic Field Adjustment:
 - Higher momentum requires a proportional increase in the magnetic field to maintain experiment size.



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- Magnetic Field Adjustment:
 - Higher momentum requires a proportional increase in the magnetic field to maintain experiment size.
- Effect on Anomalous Precession (ω_a):
 - A <u>stronger magnetic</u> field <u>increases</u> the <u>anomalous precession</u>
 frequency.



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- The statistical precision on the anomalous precession frequency ω_a is:

$$\frac{\Delta\omega_a}{\omega_a} = \frac{1}{\omega_a \gamma \tau P} \sqrt{\frac{2}{NA^2}}$$

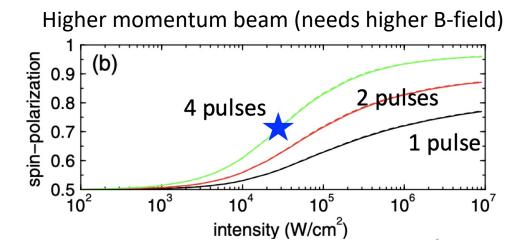
- Magnetic Field Adjustment:
 - Higher momentum requires a proportional increase in the magnetic field to maintain experiment size.
- Effect on Anomalous Precession (ω_a):
 - A <u>stronger magnetic</u> field <u>increases</u> the <u>anomalous precession</u>
 frequency.
 - ightarrow Doubling both momentum and field ightarrow x4 improvement in ω_a precision.



Polarization Contribution (P):

$$\frac{\Delta\omega_a}{\omega_a} = \frac{1}{\omega_a \gamma \tau P} \sqrt{\frac{2}{NA^2}}$$

Current polarization: 50% Possible improvement: →
 75% (realistically) → Adds an additional x1.5 gain in total precision.



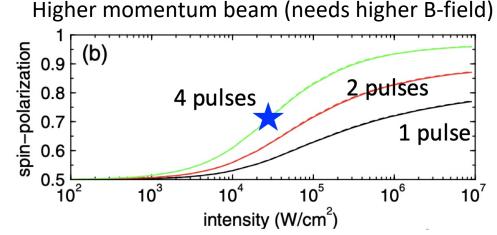
Optical pumping with train of laser pulse



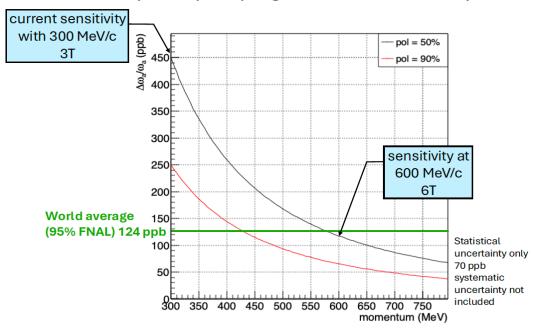
$$\frac{\Delta\omega_a}{\omega_a} = \frac{1}{\omega_a \gamma \tau P} \sqrt{\frac{2}{NA^2}}$$

- Polarization Contribution (P):
 - Current polarization: 50% Possible improvement: →
 75% (realistically) → Adds an additional x1.5 gain in total precision.

- Here is projected $\frac{\Delta \omega_a}{\omega_a}$ as function of the momentum.
- A task force has been built to check the feasibility:
 - Magnetic field;
 - Linac;
 - Polarization;
 - Other possible improvements.



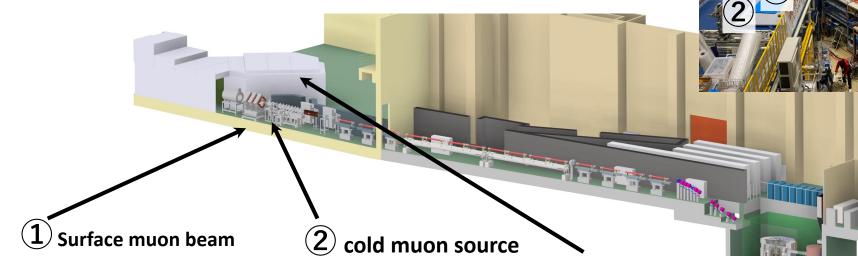
Optical pumping with train of laser pulse





Running test experiments

Three experiments are currently running at J-PARC MLF since October 29.



(S2 area & H2 area)



commissioning (H2 area)









Conclusion

- J-PARC's independent approach can provide an <u>excellent cross check</u> of Fermilab's measurement;
- J-PARC has achieved great progress recently -> First cold muon beam acceleration was an historical achievement.
- It aims for 0.45 ppm precision (~BNL level with data expected 2030+)
 - The high sensitivity study could bring to a turning point towards Fermilab precision.
- This will be another fundamental step towards our final goal:
 Measuring muon g-2 with ever-increasing precision testing the SM and probing new physics.



"The closer you look the more there is to see"





BACK-UP



Comparison with Fermilab

Drog Theor Evn Dhys 2010 052002 (2010)

	Completed	Completed	In preparation
(syst.)	$0.9 \times 10^{-19} e \cdot \text{cm}$	_	$0.36 \times 10^{-21} e \cdot \text{cm}$
EDM precision (stat.)	$0.2 \times 10^{-19} e \cdot \text{cm}$	_	$1.5 \times 10^{-21} e \cdot \text{cm}$
(syst.)	280 ppb	80100 ppb	<70 ppb
a_{μ} precision (stat.)	460 ppb	100 ppb	450 ppb
Number of detected e^-	3.6×10^{9}	_	_
Number of detected e^+	5.0×10^9	1.6×10^{11}	5.7×10^{11}
Spin precession period	4.37 /	us	$2.11~\mu \mathrm{s}$
Cyclotron period	149 r	149 ns	
Focusing field	Electric qua	Electric quadrupole	
Storage field	B = 1.4	B = 1.45 T	
Polarization	100%	6	50%
Lorentz γ	29.3	$t_{\mu}\sim$ 64.4 us	$t_{\mu} = 6.6$
Muon momentum	$3.09~{ m GeV}/c$		$300~{ m MeV}/c$
	BNL-E821	Fermilab-E989	Our experiment
	Prog. Theor. Exp.		Phys. 2019 , 053C02 (2019)



