EDMs: a theoretical review and some recent work

Maxim Pospelov

University of Minnesota/FTPI

Flambaum, MP, Ritz, Stadnik, 1912.13129 (PRD2020) Y. Ema, T. Gao, MP 2108.05398 (PRL2021) Y. Ema, T. Gao, MP 2202.10524 (PRL, to appear.)

Plan

- 1. Intro: why EDMs
- 2. CKM CP-violation and EDMs. New prediction for d_e^{equiv}
- 3. New indirect constraints on EDMs of muons.
- 4. Conclusions

Purcell and Ramsey (1949) ("How do we know that strong interactions conserve parity?" $\longrightarrow |d_n| < 3 \times 10^{-18} ecm.$)

$$H = -\mu \mathbf{B} \cdot \frac{\mathbf{S}}{S} - d\mathbf{E} \cdot \frac{\mathbf{S}}{S}$$

 $d \neq 0$ means that both P and T are broken. If CPT holds then CP is broken as well.

CPT is based on locality, Lorentz invariance and spin-statistics = very safe assumption.

search for EDM = search for CP violation, if CPT holds

Relativistic generalization

$$H_{\text{T,P-odd}} = -d\mathbf{E} \cdot \frac{\mathbf{S}}{S} \to \mathcal{L}_{\text{CP-odd}} = -d\frac{i}{2}\overline{\psi}\sigma^{\mu\nu}\gamma_5\psi F_{\mu\nu},$$

corresponds to dimension five effective operator and naively suggests $1/M_{\text{new physics}}$ scaling. Due to $SU(2) \times U(1)$ invariance, however, it scales as m_f/M^2 .

Current limits translate to multi-TeV sensitivity to M.

Current Experimental Limits

"paramagnetic EDM", Berkeley experiment

$$|d_{\rm Tl}| < 9 \times 10^{-25} e \, {\rm cm}$$
 Interpreted $|{\bf d_e}| < 1.6 \times 10^{-27}$

"diamagnetic EDM", U of Washington experiment

$$|d_{\rm Hg}| < 2 \times 10^{-28} e\,{\rm cm}$$

factor of 7 improvement in 2009! And another factor of 4 in 2016

$$|d_{\rm Hg}| < 3 \times 10^{-29} e \,\mathrm{cm}$$
 $7.4 \times 10^{-30} e \,\mathrm{cm}$

neutron EDM, ILL experiment

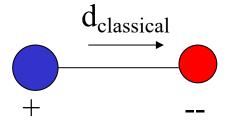
$$|d_n| < 3 \times 10^{-26} e \text{ cm}$$
 $1.8 \times 10^{-26} e \text{ cm}$

Notice that Thallium EDM is usually quoted as $d_e < 1.6 \cdot 10^{-27}$ e cm bound. It was modestly improved by YbF results. $|\mathbf{d}_e| < 1.1 \times 10^{-29}$

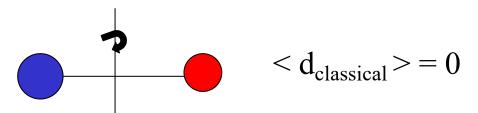
2013 ThO result by Harvard-Yale collaboration: $|\mathbf{d}_{e}| < 8.7 \times 10^{-29}$ "Confirmed" using different techniques at JILA, $|d_e| < 1.3 \times 10^{-28}$

A small comment on classical EDMs

- Fundamental EDMs are connected to spin, classical EDMs are not.
- A diatomic molecule (like ThO) will have a classical EDM.



• However, in a quantum state with fixed angular momentum classical EDMs average to zero, exactly. States with +M and –M projection of angular momentum remain degenerate (at B=0 and E \neq 0).



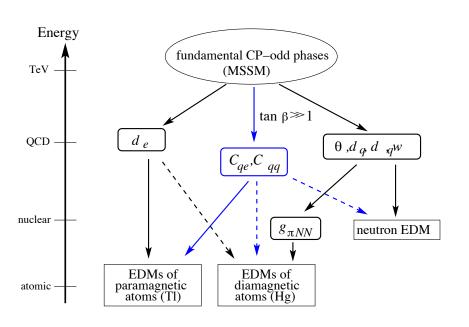
• If there is fundamental CP-violation, the electric field will induce splitting between +M and –M states, e.g. Zeeman effect but with electric field. EDM experiments are looking for E coupling to spin₅

Theory: High-Energy CP violation and EDMs

$$\mathcal{L}_{eff}^{1\text{GeV}} = \frac{g_s^2}{32\pi^2} \, \theta_{QCD} G_{\mu\nu}^a \widetilde{G}^{\mu\nu,a}$$

$$-\frac{i}{2} \sum_{i=e,u,d,s} \frac{\mathbf{d}_i}{\mathbf{d}_i} \, \overline{\psi}_i(F\sigma) \gamma_5 \psi_i - \frac{i}{2} \sum_{i=u,d,s} \widetilde{\mathbf{d}_i} \, \overline{\psi}_i g_s(G\sigma) \gamma_5 \psi_i$$

$$+ \frac{1}{3} \mathbf{w} \, f^{abc} G_{\mu\nu}^a \widetilde{G}^{\nu\beta,b} G_{\beta}^{\mu,c} + \sum_{i,j=e,d,s,b} \mathbf{C}_{ij} \, (\bar{\psi}_i \psi_i) (\bar{\psi}_j i \gamma_5 \psi_j) + \cdots$$



 One needs hadronic, nuclear, atomic matrix elements to connect Wilson coefficients to observables

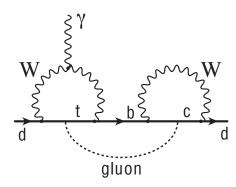
• Extremely high scales [10-100 TeV] can be probed if new physics generating EDMs violates CP maximally.

Two sources of CP-violation in SM

• Theta term of QCD: **too large EDMs** if theta is arbitrary \rightarrow new naturalness problem because of EDMs. ($d_n \sim \theta \ m_q/m_n^2$, $\theta < 10^{-10}$)

 Cabibbo-Kobayashi-Maskawa matrix and nearly maximal CP phase → still EDMs are too small to be observable in the next round of EDM experiments.

EDMs from SM sources: CKM



CKM phase generates tiny EDMs:

$$d_d \sim \text{Im}(V_{tb}V_{td}^*V_{cd}V_{cb}^*)\alpha_s m_d G_F^2 m_c^2 \times \text{loop suppression}$$

$$< 10^{-33} e \text{cm}$$

- Quark EDMs identically vanish at 1 and 2 loop levels, EW²=0 (Shabalin, 1981).
- 3-loop EDMs, EW²QCD¹ are calculated by Khriplovich; Czarnecki, Krause.
- d_e vanishes at EW³ level (Khriplovich, MP, 1991) < 10^{-38} e cm
- Long distance effects give neutron EDM $\sim 10^{-32}$ e cm; uncertain.

"Paramagnetic" EDMs:

 Paramagnetic EDM (EDM carried by electron spin) can be induced not only by a purely leptonic operator

$$d_e \times \frac{-i}{2} \overline{\psi} \sigma_{\mu\nu} \gamma_5 F_{\mu\nu} \psi$$

but by semileptonic operators as well:

$$C_S imes rac{G_F}{\sqrt{2}} \ \overline{N} N \ \overline{\psi} i \gamma_5 \psi$$

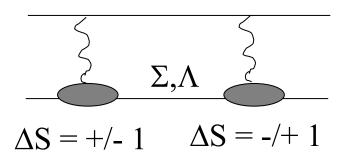
Only a linear combination is limited in any single experiment.
 ThO 2018 ACME result is:

$$|d_e| < 1.1 \times 10^{-29} \text{ e cm}$$
 at $C_S = 0$
 $|C_S^{\text{singlet}}| < 7.3 \times 10^{-10}$ at $d_e = 0$
 $d_e^{\text{equiv}} = d_e + C_S \times 1.5 \times 10^{-20} e \text{ cm}$

What is SM prediction for the electron EDM?

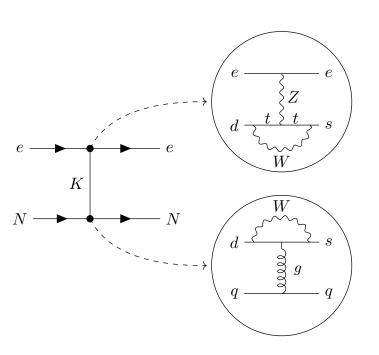
CKM CP-violation and paramagnetic EDMs

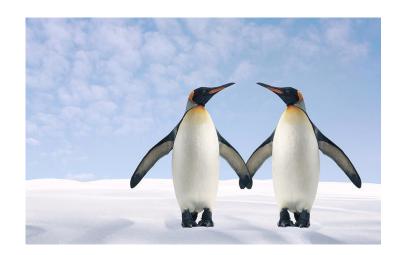
- Several groups attempted to calculate d_e (MP, Khriplovich; ...)
- The result is small ~ few 10⁻⁴⁰ e cm. (Yamaguchi, Yamanaka)
- Semileptonic (C_S) operator is more important. MP and Ritz (2012) estimated two-photon mediated EW²EM² effects and found that CS is induced at the level equivalent to ~ 10^{-38} e cm



It turns out that there are much larger contributions at EW³ order

Union of two-penguins: EW³ order





- The induced semileptonic operator is calculable in chiral perturbation theory (in m_s expansion)
- The result is large, $d_e(\text{equiv}) = +1.0 \cdot 10^{-35} \text{ e cm}$
- Same EW penguin that is responsible for $B_s \rightarrow \mu\mu$, Re $K_L \rightarrow \mu\mu$

Final result

• Combining $(m_s)^{-1}$ and $(m_s)^{-1/2}$ effects, we get

$$C_S(\text{LO} + \text{NLO}) \simeq 6.9 \times 10^{-16}$$

 $\implies d_e^{\text{equiv}} \simeq 1.0 \times 10^{-35} e \text{ cm}.$

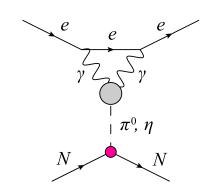
- The result EW³ much larger than the EW²EM² estimate by ~1000.
- Note that actually establishing the correct sign is tricky.
- The result is under "best possible" theoretical control, and can be improved on the lattice $\langle N|i(\bar{s}\gamma_{\mu}(1-\gamma_{5})d-\bar{d}\gamma_{\mu}(1-\gamma_{5})s)|N\rangle_{\rm EW^{1}}$

$$= \frac{f_S}{m_N} i q_\mu \bar{N} N + \frac{f_T}{m_N} q_\nu \bar{N} \sigma_{\mu\nu} \gamma_5 N.$$

Paramagnetic EDM sensitivity to theta term:

• T-channel pion exchange gives

$$\mathcal{L} = \theta \times \frac{1}{m_{\pi}^{2}} \times 0.017 \times 3.5 \times 10^{-7} (\bar{e}i\gamma_{5}e)(\bar{n}n - \bar{p}p)$$
$$= (\bar{e}i\gamma_{5}e)(\bar{n}n - \bar{p}p) \times \frac{3.2 \times 10^{-13}\theta}{\text{MeV}^{2}}.$$



implying $|\theta| < 8.4 \times 10^{-8}$ sensitivity. However, adding exchange of η_8 , $1 \to 1 - \frac{1}{3} \frac{f_\pi^2 m_\pi^2}{f_\pi^2 m_\pi^2} \times \frac{m_d - m_u}{m_d + m_u} \times \frac{A \times \sigma_N}{\frac{m_d - m_u}{2} \langle p | \bar{u}u - \bar{d}d | p \rangle \times (N - Z)}$

$$3 f_{\eta}^2 m_{\eta}^2 \cap m_d + m_u \cap \frac{m_d - m_u}{2} \langle p | \bar{u}u - dd | p \rangle \times (N - Z)$$

$$1 \to 1 - 0.88 \simeq 0.12.$$

The effect can completely cancel within error bars on nucleon sigma term σ_N .

Photon box diagrams:

Diagrams are IR divergent but regularized by Fermi momentum in the Fermi gas picture of a nucleus (intermediate N is above Fermi surface).

$$\mathcal{L} = \bar{e}i\gamma_5 e\bar{N}N \times \frac{2m_e \times 4\alpha \times \overline{d\mu} \times 6.2}{\pi p_F} = \bar{e}i\gamma_5 e\bar{N}N \times 2.4 \times 10^{-4} \times \overline{d\mu}$$
$$\overline{d\mu} = \frac{Z}{A}\mu_p d_p + \frac{A - Z}{A}\mu_n d_n = \frac{e}{2m_p} \times (1.08d_p - 1.16d_n)$$

• Nucleon EDM (theta) is very much a triplet, $d_p \simeq -d_n \simeq 1.6 \times 10^{-3} e {\rm fm} \theta$

Full answer including chiral NLO. (accidental cancellation of π^0 and η)

$$C_{SP}(\bar{\theta}) \approx \left[0.1_{LO} + 1.0_{NLO} + 1.7_{(\mu d)}\right] \times 10^{-2}\bar{\theta} \approx 0.03\bar{\theta}$$

Limit on theta term from ThO (electron EDM) experiment:

$$|\bar{\theta}|_{\mathrm{ThO}} \lesssim 3 \times 10^{-8}$$

Constraints on other hadronic Wilson coeff.

• Proton EDM, other CP-violating inputs can be limited:

System	$ d_p (e \cdot \text{cm})$	$ ar{g}_{\pi NN}^{(1)} $	$ \tilde{d}_u - \tilde{d}_d $ (cm)	$ ar{ heta} $
ThO	$2 imes10^{-23}$	$4 imes10^{-10}$	$2\times\mathbf{10^{-24}}$	3×10^{-8}
n		1.1×10^{-10}	5×10^{-25}	2.0×10^{-10}
Hg	2.0×10^{-25}	$1 \times 10^{-12} \text{ a}$	$5 \times 10^{-27} \text{ a}$	1.5×10^{-10}
Xe	3.2×10^{-22}	6.7×10^{-8}	3×10^{-22}	3.2×10^{-6}

- Current constraints on Theta_{QCD} trail d_n sensitivity by two orders of magnitude
- Given fast progress of recent years with ``paramagnetic'' EDMs, a further increase by ~ 100 will provide comparable sensitivity.

Summary thus far:

- In the SM, for paramagnetic systems, the electron EDM is not the most interesting observable, but the semi-leptonic C_S operator.
- Current constraints on Theta_{QCD} trail d_n sensitivity by two orders of magnitude, but the main sensitivity is through C_s . Given fast progress of recent years with "paramagnetic" EDMs, a further increase by ~ 100 will provide comparable sensitivity.
- CKM CP-violation is also enhanced in the C_S , giving an equivalent electron EDM as 10^{-35} e cm. Much larger than people believed, but still very far from modern experimental capabilities.
 - What about muon EDM?
 - Q1: what is the limit on muon EDM?
 - Q2: what is the reasonable size for muon EDM?

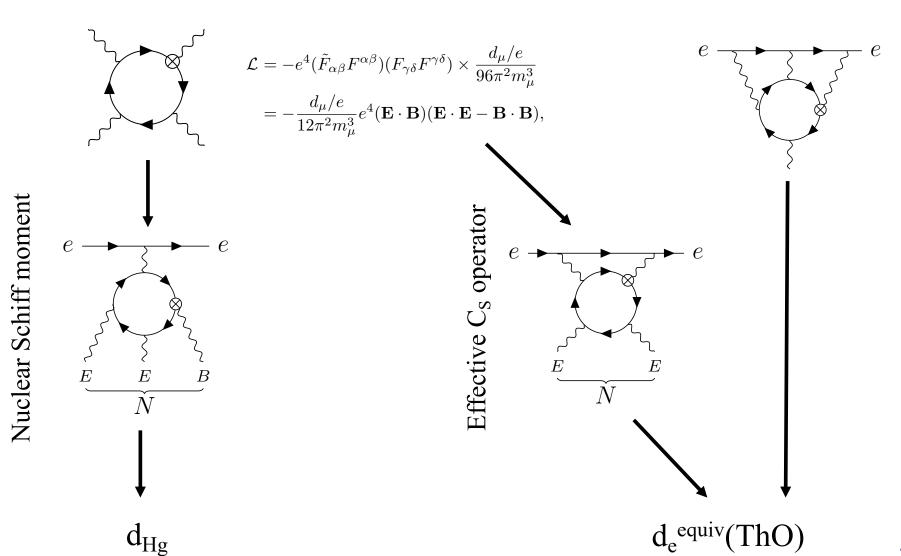
EDMs of heavy flavors

- Among Wilson coefficients of different kind, EDMs of heavy flavours d_i are interesting. i = muon, tau, charm, bottom, top.
- Muon EDM is limited as a biproduct of BNL g-2 experiment. Can be significantly improved in dedicated beam experiments (PSI, Fermilab)
- There is a creative proposal to measure MDMs and limit EDMs of charmed baryons using thin fixed target and bent crystal technology just before the LHCb experiment (E. Bagli et al, 2017).
- Heavy flavors contribute to observable EDMs via loops. Top quark EDM is limited indirectly by electron EDM via a two-loop (top-Higgs-gamma) Barr-Zee diagrams. The result is stronger than the direct measurements at LHC.

17

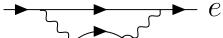
Muon EDM inside a loop

Muon loop induces E³B effects, and electron EDM at 3-loops.



New indirect constraints on muon EDM

• Owing to the fact that the electric field inside a large nucleus is not that small eE \sim Z α R_N⁻¹ \sim 30 MeV compared to m_{μ} , effects formally suppressed by higher power of m_{μ} win over three-loop electron EDM.



• New results (again, C_S provides the best sensitivity):

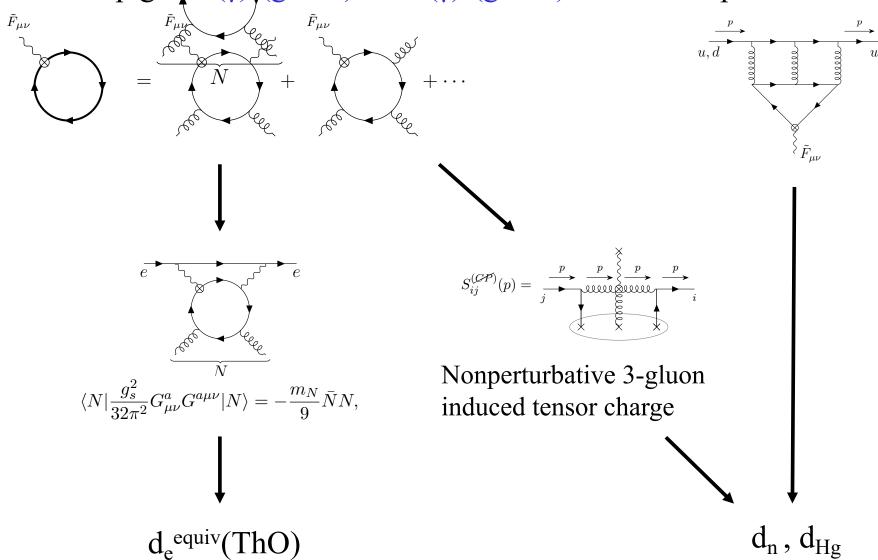
Hg EDM experiment:
$$S_{^{199}\mathrm{Hg}}/e \simeq (d_{\mu}/e) \times 4.9 \times 10^{-7} \, \mathrm{fm}^2$$
, $|d_{\mu}| < 6.4 \times 10^{-20} \, e \, \mathrm{cm}$

ThO EDM experiment:
$$d_e^{\text{equiv}} \simeq 5.8 \times 10^{-10} d_{\mu} \implies |d_{\mu}| < 1.9 \times 10^{-20} e \text{ cm}.$$

- Factor of 3 and 9 improvement over the BNL constraint, $|d_{\mu}| < 1.8 \times 10^{-19}$
- New benchmark for the muon beam EDM experiments.
- NB: 3-loop contributions calculated by Grozin et al. is revised
- Tau EDM is constrained by three-loop induced $d_{e_{e}}$.

Charm and bottom EDMs

Charm loop gives $(\gamma)^2(gluon)^2$ and $(\gamma)^1(gluon)^3$ effective operators



All EDMs are induced by charm and bottom EDMs.

New indirect constraints on c-, b- quarks EDMs

New results:

Neutron EDM experiment:
$$|d_c| < 6 \times 10^{-22} e \, \text{cm}, \quad |d_b| < 2 \times 10^{-20} e \, \text{cm},$$

ThO EDM experiment:
$$|d_c| < 1.3 \times 10^{-20} e \text{ cm}, \quad |d_b| < 7.6 \times 10^{-19} e \text{ cm},$$

Finally, benchmarks for muon EDM

Direct limit from past beam experiment:

$$|d_{\mu}| < 1.8 \times 10^{-19} \, \text{ecm},$$

■ ThO EDM experiment, indirect limit:

$$d_e^{
m equiv} \simeq 5.8 \times 10^{-10} \, d_\mu \implies |d_\mu| < 1.9 \times 10^{-20} \, e \, {
m cm}.$$
 We are here

■ EDM on the size of the current *magnetic* discrepancy:

$$d_{\mu} \sim (3*10^{-9}) * e/(2 m_{\mu}) \sim 3*10^{-22} \text{ e cm}$$

Lepton Universality of NP with cubic scaling:

$$d_{u} \sim (m_{u}/m_{e})^{3} d_{e} \sim \text{up to } 10^{-22} \text{ e cm}$$

Lepton Universality of NP with linear scaling:

$$d_{u} \sim (m_{u}/m_{e}) d_{e} \sim \text{up to } 2*10^{-27} \text{ e cm}$$

Conclusions

- EDMs are an important tool for searching for flavor-diagonal CP violation. Multi-TeV scales are probed. Further improvements likely.
- In *lots of models*, including the SM, the paramagnetic EDMs (experiments looking for d_e) are induced by the semi-leptonic operators of (electron pseudoscalar)*(nucleon scalar) type.
- CKM induces C_S . The result is large and calculable and is dominated by the EW³ order. The *equivalent* d_e is found to be $+1.0 \times 10^{-35}$ e cm. This is 1000 times larger than previously believed.
- PNew indirect limits on muon, charm and bottom provide new target for the EDM beam experiments:

$$|d_c| < 6 \times 10^{-22} e \,\mathrm{cm}, \quad |d_b| < 2 \times 10^{-20} e \,\mathrm{cm}, \quad |d_\mu| < 1.9 \times 10^{-20} e \,\mathrm{cm}.$$